

3.
Experimental
Basis of
Quantum
Physics, 4

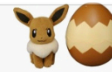
4.
Structure of
the Atom, 1

lecture 16, October 6, 2017



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Compare with similar items

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Report incorrect product information.

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Let a pro do a deep clean
Schedule



Roll over image to zoom in

We all have one, right?

housekeeping

exam 1 was last friday ;)

next one: Friday, October 27

Next Tuesday:

no HW workshop: catch-up lecture...enjoying myself too much

Honors option

Go to: <https://qstbb.pa.msu.edu/storage/PHY215/honors/>

read the MinervaInstructions1_2017_215 document



one more thing

Compton Scattering

one of the most important experiments...ever

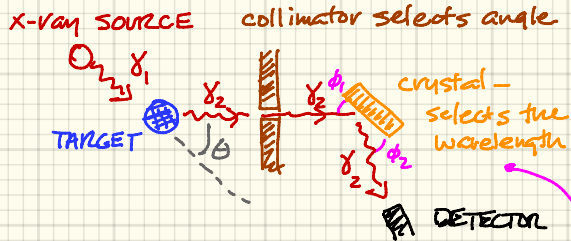


COMPTON SCATTERING

Milliken **HATED** Einstein's idea → worked for decade to kill it @ UofC
and **beautifully confirmed it** by 1913

Definite demonstration
by Arthur Holly Compton, 1923

imagine



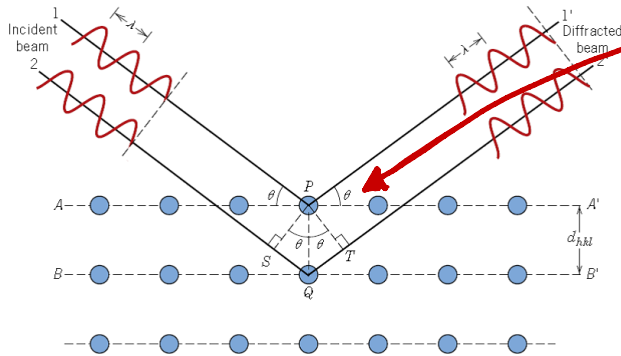
measurable: λ_2

known: λ_1, θ

"Bragg Spectrometer"
measuring ϕ 's → λ

$$\begin{array}{c} \gamma_1 + e \rightarrow \gamma_2 + e \\ \uparrow \qquad \qquad \uparrow \\ \text{at "rest"} \qquad \text{KE} \\ E_2 > \underline{<} E_1 \text{ ?} \\ \text{so } \lambda_2 > \underline{<} \lambda_1 \end{array}$$

BRAGG SPECTROMETER



$$n \lambda = 2d \sin \theta$$

so measuring $\theta \equiv$ determining λ

spacing of crystal must be $\sim \lambda$ light

NaCl, calcite, mica, quartz, etc

$\hookrightarrow d \sim 2.8 \text{ \AA}$ $\lambda (\text{Mo}) \sim 1 \text{ \AA}$

back to the story:

Before

$$\begin{array}{l} \gamma_1 \rightarrow e_1 \\ \gamma_1(\vec{q}_1) \quad e_1(\vec{p}_1) \end{array}$$

Conserve momentum:

$$\textcircled{1} \quad \vec{q}_1 + \vec{p}_1 = \vec{q}_2 + \vec{p}_2$$

$$E^2 = p^2 c^2 + m^2 c^4$$

$$E_1^2 = p_1^2 c^2$$

$$p_1 = \frac{E_1}{c} = \frac{h f_1}{c}$$

≠

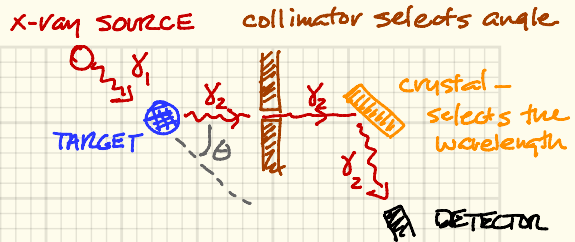
$$p_2 = \frac{h f_2}{c}$$

After

$$\begin{array}{l} \gamma_2(\vec{q}_2) \\ \theta \\ e_2(\vec{p}_2) \end{array}$$

Conserve Energy:

$$\textcircled{2} \quad E_{\gamma_1} + E_{e_1} = E_{\gamma_2} + E_{e_2}$$



TOTALLY A PARTICLE INTERPRETATION!

Billiard Balls!



TOTALLY A WAVE INTERPRETATION!

$$\vec{p}_2 = \vec{q}_1 + \vec{p}_1 - \vec{q}_2$$

$$\uparrow \\ = 0$$

$$\vec{p}_2 = \vec{q}_1 - \vec{q}_2 \quad \text{trick}$$

$$p_2^2 = \vec{p}_2 \cdot \vec{p}_2 = (\vec{q}_1 - \vec{q}_2)^2 = q_1^2 + q_2^2 - 2\vec{q}_1 \cdot \vec{q}_2$$

$$p_2^2 = \left(\frac{hf_1}{c}\right)^2 + \left(\frac{hf_2}{c}\right)^2 - 2\left(\frac{hf_1}{c}\right)\left(\frac{hf_2}{c}\right)\cos\theta \quad (3)$$

from (2)

$$E_{\gamma_1} + E_{e_1} = E_{\gamma_2} + E_{e_2}$$

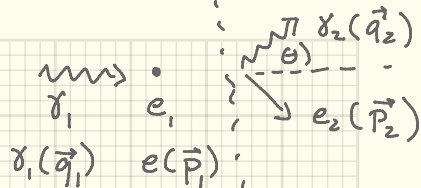
$$hf_1 + mc^2 = hf_2 + \sqrt{p_2^2 c^2 + m^2 c^4}$$

$$(hf_1 + mc^2 - hf_2)^2 = p_2^2 c^2 + m^2 c^4$$

$$(hf_1)^2 + (hf_2)^2 - 2(hf_1)(hf_2) + 2mh(f_1 - f_2) + m^2 c^4 = p_2^2 c^2 + m^2 c^4$$

$$2\left(\frac{hf_1}{c}\right)\left(\frac{hf_2}{c}\right)(1 - \cos\theta) = 2mhc\left(\frac{f_1}{c} - \frac{f_2}{c}\right)$$

measure λ ...



$$\lambda_2 - \lambda_1 = \frac{h}{mc} (1 - \cos \theta)$$

↑ ↑ ↑
measure set-up set-up

Consider back-scattering $\Rightarrow \theta = \pi$, so $\lambda_2 - \lambda_1$ largest.

$$\lambda_2 - \lambda_1 = \frac{h}{mc} (2)$$

$$= \frac{2hc}{mc^2} \quad m_e = 0.511 \text{ MeV}$$

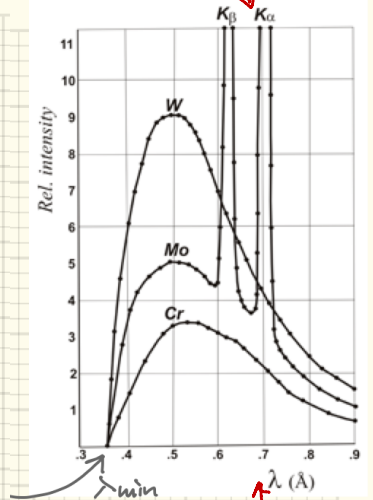
$$= \frac{(2)(1241 \text{ eV} \cdot \text{nm})}{(0.511 \times 10^6 \text{ eV})}$$

$$= 0.0049 \text{ nm} = 0.0049 \times 10^{-9}$$

$$\Delta \lambda = 0.049 \text{ \AA} \quad \text{tiny but measurable}$$

$$\text{for } \theta = \pi/2: \quad \Delta \lambda = 0.024 \text{ \AA}$$

Used K_α x-rays
from Mo



$$\lambda_1 = 0.7 \text{ \AA}$$

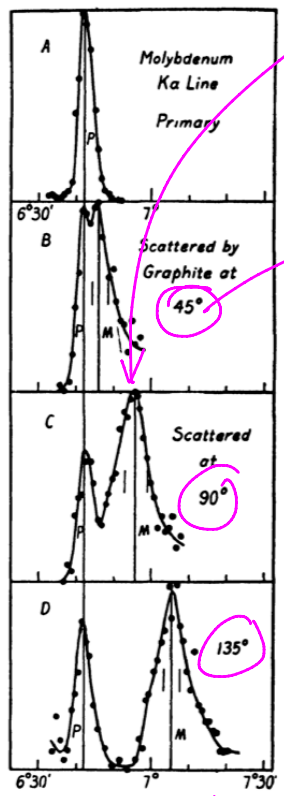


FIG. 108.

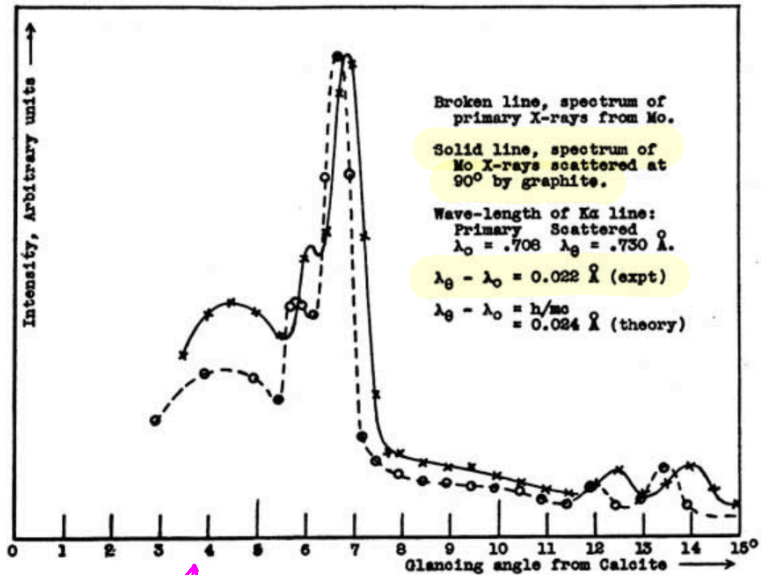


Fig. 4. Spectrum of molybdenum X-rays scattered by graphite, compared with the spectrum of the primary X-rays, showing an increase in wave-length on scattering.

original x ray

2nd peaks \rightarrow scattered x-rays \rightarrow longer λ

in $(1-\cos\theta)$ formula

Bragg Spectrometer angles $\equiv \lambda$'s

given in the fourth column of Table I. That this extrapolation is very

TABLE I

Wave-length of Primary and Scattered γ -rays

| | Angle | μ/ρ | τ/ρ | λ obs. | λ calc. |
|-----------------|-------------|------------|-------------|----------------|-----------------|
| Primary | 0° | .076 | .017 | 0.022 A | (0.022 A) |
| Scattered | 45° | .10 | .042 | .030 | 0.029 |
| " | 90° | .21 | .123 | .043 | 0.047 |
| " | 135° | .59 | .502 | .068 | 0.063 |

nearly correct is indicated by the fact that it gives for the primary beam a wave-length 0.022 A. This is in good accord with the writer's value

actually $\Delta\lambda$

I think of this as the
discovery of the photon

One more thing

$$\Delta\lambda = \frac{h}{m_e c} (1 - \cos\theta)$$

$$E = hf = \frac{hc}{\lambda} \rightarrow m_e c^2$$

$$\frac{hc}{\lambda} = m_e c^2$$

$$\frac{h}{m_e c} = \lambda_c$$

"Compton wavelength"
of electron

BEST STAND-IN FOR
THE "SIZE" OF AN
ELEMENTARY PARTICLE

$$\lambda_c = 0.002426 \text{ nm}$$

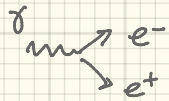
Compton wavelength

of proton:

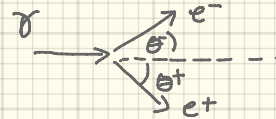
$$\lambda_c(p) = \frac{h}{m_p c} = \frac{hc}{m_p c^2} = \frac{1241 \text{ eV} \cdot \text{nm}}{938 \times 10^6 \text{ eV}}$$

$$\lambda_c(p) = 1.3 \times 10^{-6} \text{ nm} = 1.3 \times 10^{-15} \text{ m}$$

Pair production & annihilation



"pair production"



$$(1) \quad p_y = p_x^- + p_x^+ = p^- \cos \theta^- + p^+ \cos \theta^+$$

$$(2) \quad 0 = p_y^- - p_y^+ = p^- \sin \theta^- - p^+ \sin \theta^+$$

$$(3) \quad E_\gamma = E^- + E^+ = hf$$

remember $E_\gamma = p_\gamma c$

$$(4) \quad p_\gamma = \frac{E_\gamma}{c} = \frac{hf}{c}$$

$$(4) \rightarrow (1)$$

$$hf = p^- c \cos \theta^- + p^+ c \cos \theta^+ \quad (5)$$

(3)

$$hf = \sqrt{p^-^2 c^2 + m^2 c^4} + \sqrt{p^+^2 c^2 + m^2 c^4} \quad (6)$$

max hf from (5) $hf_{\max} = p^- c + p^+ c$ ← can't

But

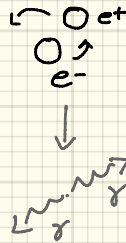
$$hf > p^- c + p^+ c$$

problem: momentum lost.



only in matter does $\gamma \rightarrow e^- e^+$

Positronium



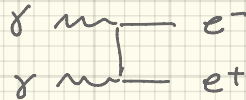
a little atom



$$E_\gamma + E_\gamma = m_e c^2 + m_e c^2$$

$$E_\gamma = m_e c^2 = 0.511 \text{ MeV}$$

BTW



does happen ... and did.

go back about a decade

Rutherford on the loose

on faculty at McGill University, 1900-1903

on nuclear decay

meanwhile

Rutherford had
made his own
career

McGill University in Montreal, 1900-1903

chemists still held to the (new) notion that atoms were indivisible
physicists were becoming convinced that atoms had structure and
maybe made of constituents

Rutherford was convinced that matter was transmutating from one
element to another...somehow

He entered into a heated debate with chemist Frederick Soddy...

“Perhaps Professor Rutherford may be able to convince us that matter as known to him is really the same matter as known to us... I feel sure that chemists will retain a belief and reverence for atoms as concrete and permanent identities, if not immutable, certainly not yet transmuted”

“I am expected to do a lot of original work and to form a research school to knock the shine out of the Yankees.”

Rutherford

to his fiancée upon his
appointment at McGill
University in Montreal, 1898

Instead...they collaborated.

Nobel Prize in Chemistry

1908

which greatly amused him

and went on

to do his best work after his Nobel...very unusual



The screenshot shows the Nobelprize.org website. At the top, the logo and tagline "The Official Web Site of the Nobel Prize" are visible. A navigation bar includes links for "Home", "A-Z Index", "FAQ", "Press", and "Contact Us". Below this is a secondary navigation bar with "Nobel Prizes", "Alfred Nobel", "Educational", "Video Player", and "Nobel Organizations". A search bar is on the right. The main content area is titled "The Nobel Prize in Chemistry 1908" and features a timeline from 1901 to 2010 with a slider set to 1908. A dropdown menu shows "Sort and list Nobel Prizes and Nobel Laureate" and "Prize category: Chemistry". The main heading is "The Nobel Prize in Chemistry 1908 Ernest Rutherford". Below this is a dropdown menu for "The Nobel Prize in Chemistry 1908" with "Ernest Rutherford" selected. A portrait of Ernest Rutherford is shown. The text below the portrait reads: "Ernest Rutherford" and "The Nobel Prize in Chemistry 1908 was awarded to Ernest Rutherford 'for his investigations into the disintegration of the elements, and the chemistry of radioactive substances'". A photo credit "Photos: Copyright © The Nobel Foundation" is below. At the bottom, a "TO CITE THIS PAGE:" section provides the MLA style citation: "The Nobel Prize in Chemistry 1908", Nobelprize.org, 8 Feb 2011, http://nobelprize.org/nobel_prizes/chemistry/laureates/1908/. The footer contains "Privacy Policy", "Terms of Use", "Technical Support", and "Copyright © Nobel Media AB 2011".

so, what's in the atom

from a 1910
perspective?

Look what people were contending with:

electrons produced at the cathode of a cathode ray tube.

electrons seemed to spontaneously pop out of some nuclei.

yet, bulk matter is not electrically charged...so there is some positive charge somewhere

JJ had a model:

“Plum-pudding” model of atom



pudding: a continuous + charge and mass distribution

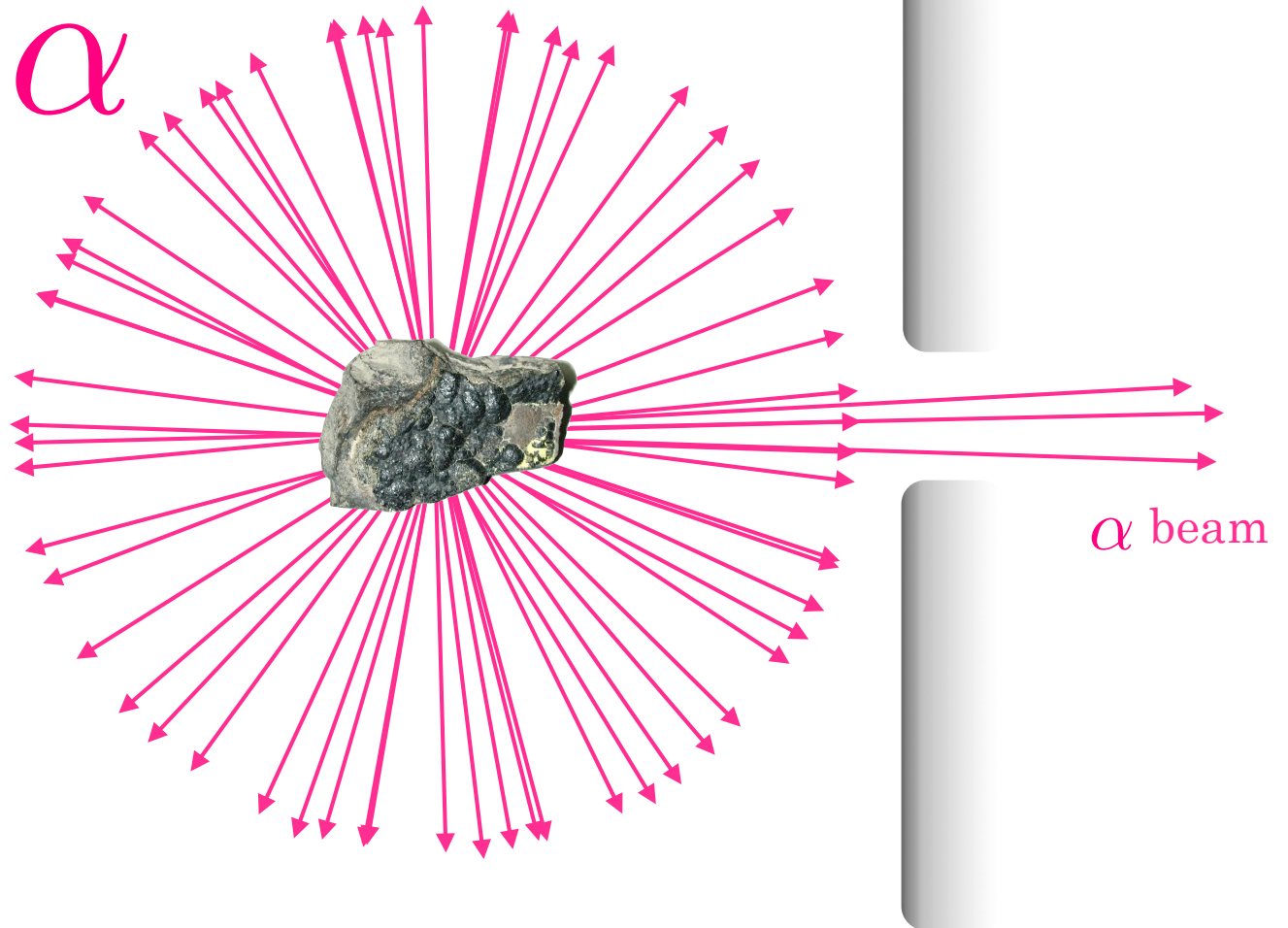
raisins: specks of – electrons

Scattering experiments...

Rutherford went back to Britain

1907, Chair of
Physics at
University of
Manchester

made "beams" of
alpha particles
using highly
radioactive
sources

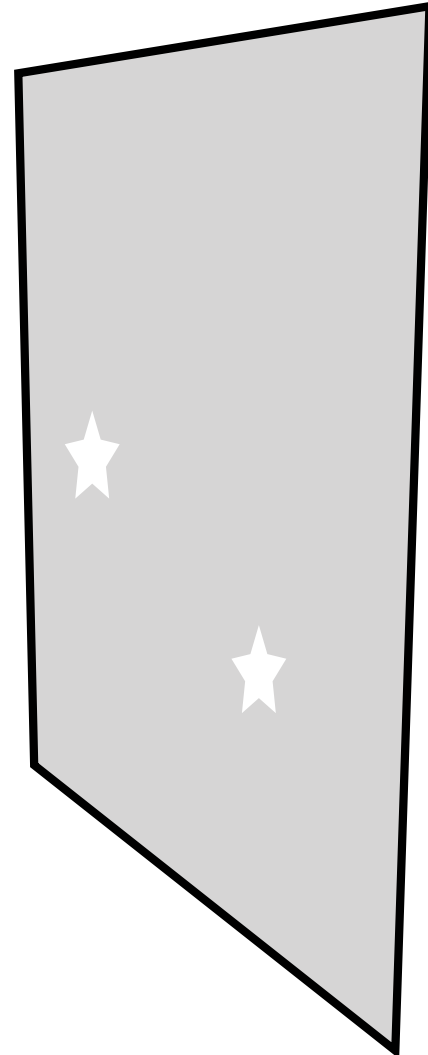


post doc

undergraduate student

Hans Geiger and Eugene Marsden studied

“scintillating” sheet
 α particle scattering from Gold 1909



1908 Geiger experiment

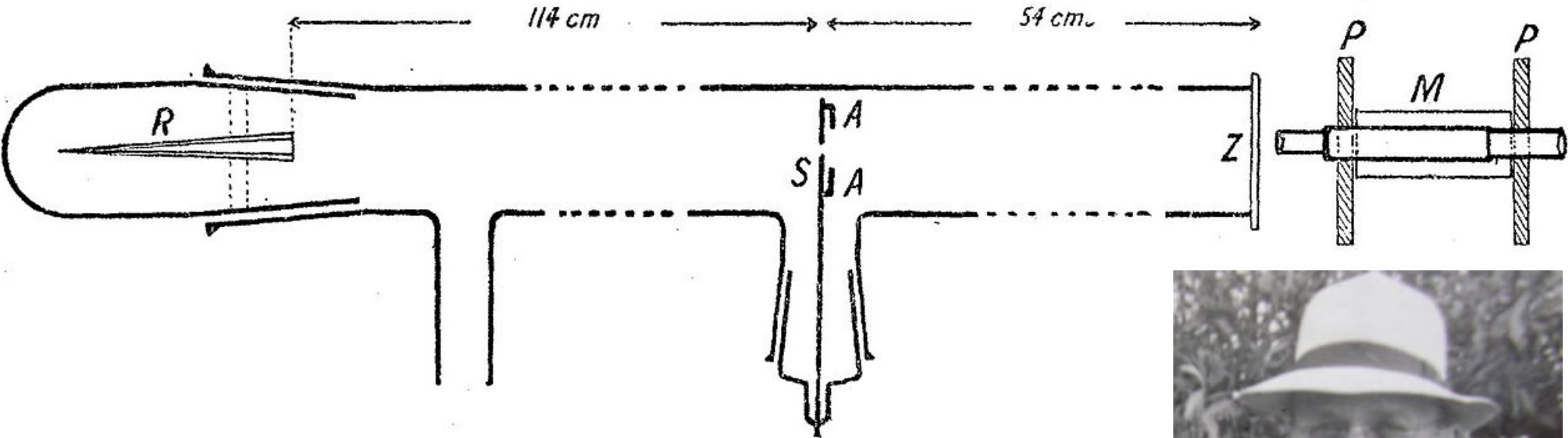


FIG. 1.



1909 Geiger-Marsden experiment

1/8000 at 90°

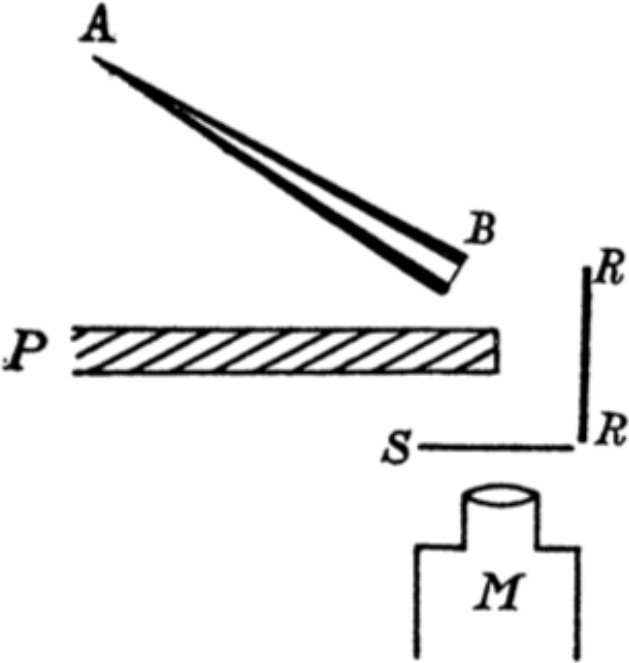


FIG. 1.

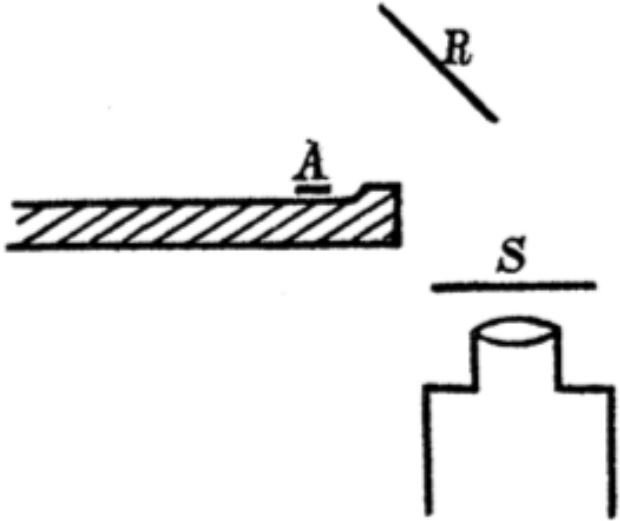
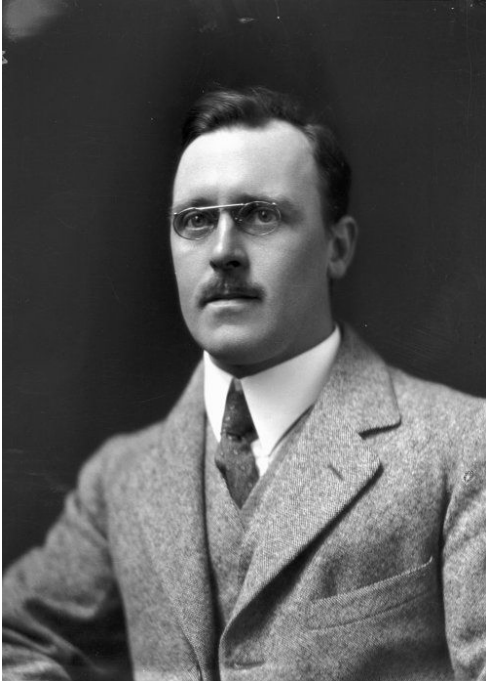
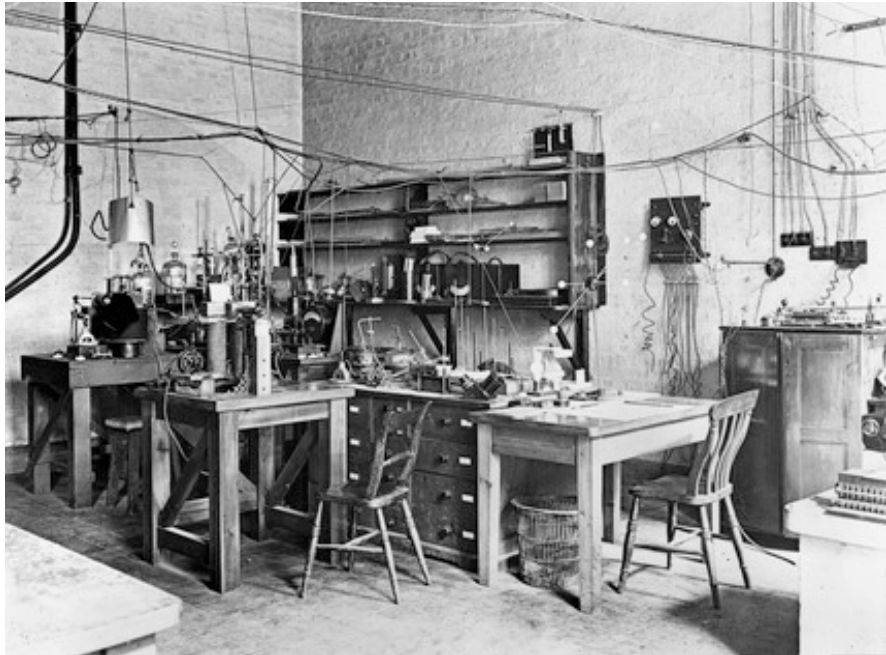


FIG. 3.

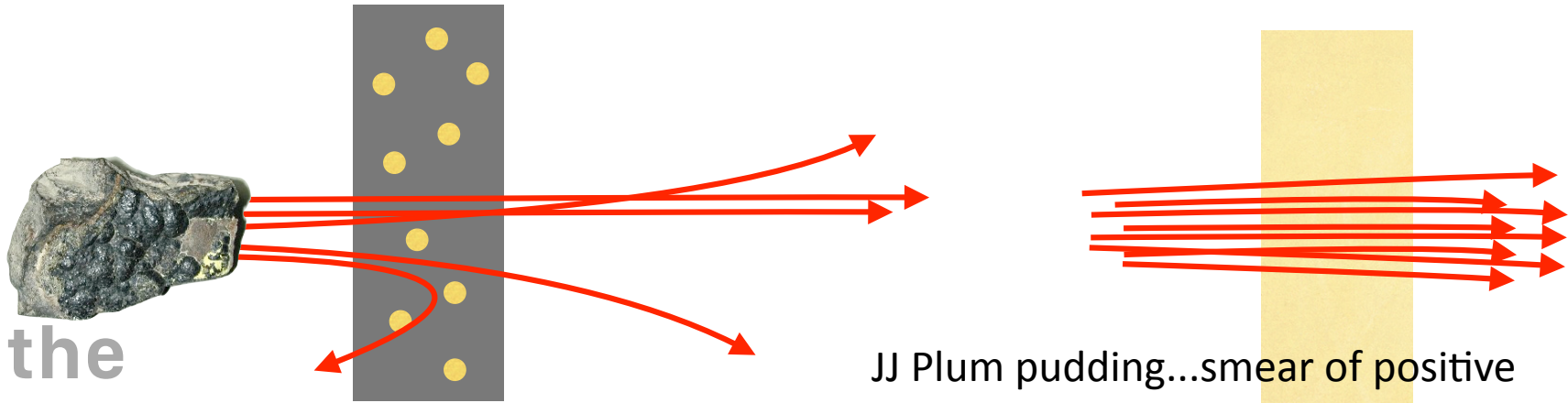




“

It was quite the most incredible event that has ever happened to me in my life. It was almost as incredible as if you fired a 15-inch shell at a piece of tissue paper and it came back at you.

He had the solution after 2 years of work



JJ Plum pudding...smear of positive charge - tiny individual deflections

the Rutherford Model of the atom:

Matter consists of **hard-cores of positive charge.**

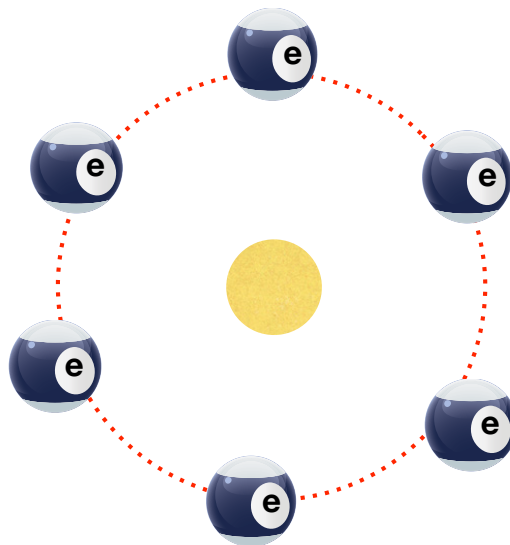
The nucleus. This matched his alpha-scattering data.

The **electrons**? Somewhere around the outside?

he found:

1911: that the Atomic Number was $+Ze$

and made a model of the atom...



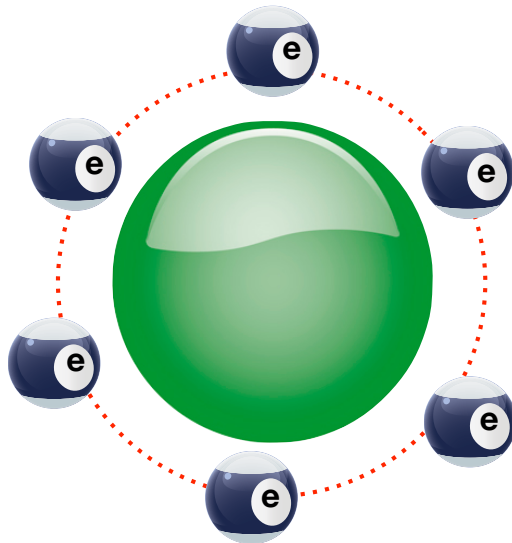
That's problematic, the electrons would accelerate...and radiate.

a spiral of death.

the minimum size of the nucleus is

3×10^{-14} m

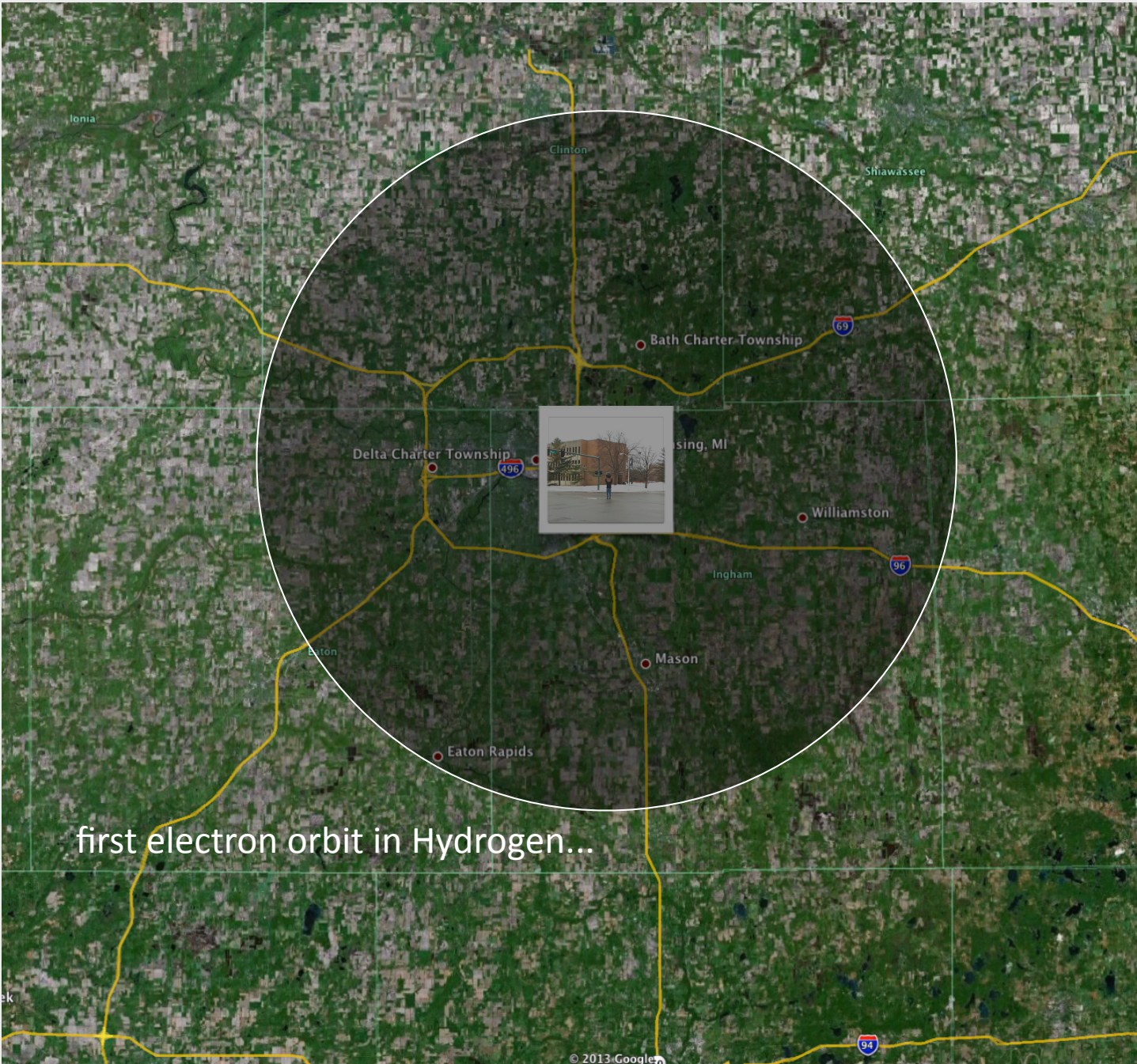
atom mostly nothing!



1 meter diameter ball

as a proton...

first electron orbit in Hydrogen...





Ernest Rutherford:

Sir Ernest, 1914

Baron, Lord Rutherford of Nelson, 1931

Died 1937, ashes interred

Westminster Abbey near Newton

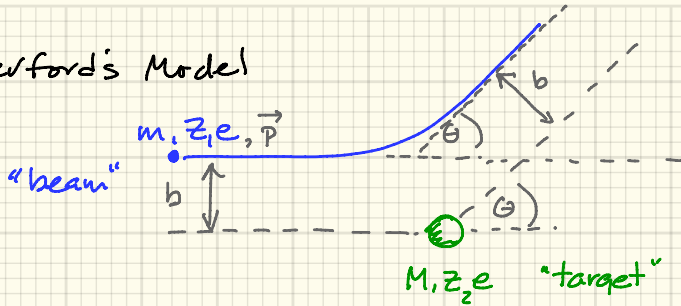
Father of Nuclear Physics:

- Discovered: the 3 nuclear decay modes
- Described nuclear decay rates...measured the Uranium chain
- Discovered the hard-core nucleus
- Modeled the atom
- First to deliberately transmute an atom
- discovered & named the proton
- Predicted the existence of the neutron...w/ Chadwick, 1935
- Predicted fission



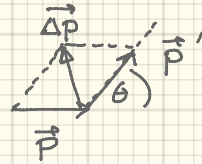


Rutherford's Model

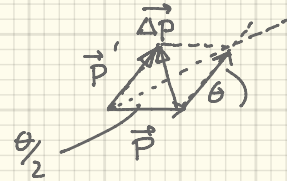


b : "impact parameter"
distance of closest approach.

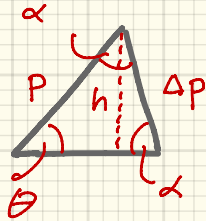
momentum:



rearrange



some trig:



$$\begin{aligned} 2\alpha + \theta &= \pi \\ \alpha &= \frac{\pi - \theta}{2} \end{aligned}$$

elastic: $|\vec{p}| = |\vec{p}'| = |m\vec{v}_0|$

left: $\frac{h}{p} = \sin\theta$
 $h = p \sin\theta$

right: $\frac{h}{\Delta p} = \sin\alpha$
 $h = \Delta p \sin\alpha$
 $= \Delta p \sin\left(\frac{\pi}{2} - \frac{\theta}{2}\right)$

$h = \Delta p \cos\theta/2$

$$\Delta p = 2mv_0 \sin \frac{\theta}{2} = \int F \cos \phi \, dt = \frac{z_1 z_2 e^2}{4\pi \epsilon_0} \int \frac{\cos \phi}{r^2} \, dt$$

Conserve angular momentum:

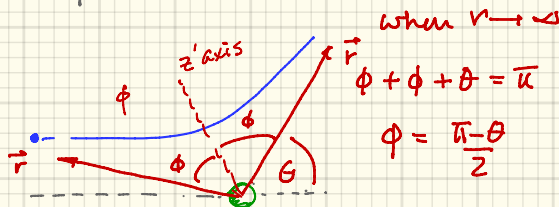
$$mrv^2 \frac{d\phi}{dt} = mv_0 b$$

$$r^2 = \frac{v_0 b}{d\phi/dt}$$

so

$$2mv_0 \sin \frac{\theta}{2} = \frac{z_1 z_2 e^2}{4\pi \epsilon_0} \int \frac{\cos \phi}{v_0 b} \frac{d\phi}{dt} \, dt = \frac{z_1 z_2 e^2}{4\pi \epsilon_0 v_0 b} \int_{\phi_i}^{\phi_f} \cos \phi \, d\phi$$

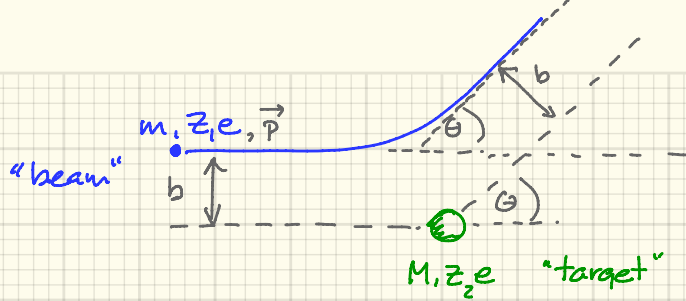
angle extremes:



$$\int_{\phi_i}^{\phi_f} \cos \phi \, d\phi = 2 \cos \frac{\theta}{2}$$

solve for b:

$$b = \frac{z_1 z_2 e^2}{4\pi \epsilon_0 m v_0^2} \cot \frac{\theta}{2}$$



$$b = \frac{z_1 z_2 e^2}{4\pi\epsilon_0 m v_0^2} \cot \frac{\theta}{2}$$

$$\theta = 0 \quad \cot \frac{\theta}{2} = \infty \Rightarrow b = \infty \text{ forward}$$

$$\theta = \frac{\pi}{2} \quad \cot \frac{\theta}{2} = 1 \quad b = \frac{z_1 z_2 e^2}{4\pi\epsilon_0 m v_0^2}$$

$$\theta = \pi \quad \cot \frac{\theta}{2} = 0 \Rightarrow b = 0 \text{ backward.}$$

Smaller $b \Rightarrow$ larger θ

What's the likelihood of scattering into a particular direction?

glad you asked.

"cross section"