

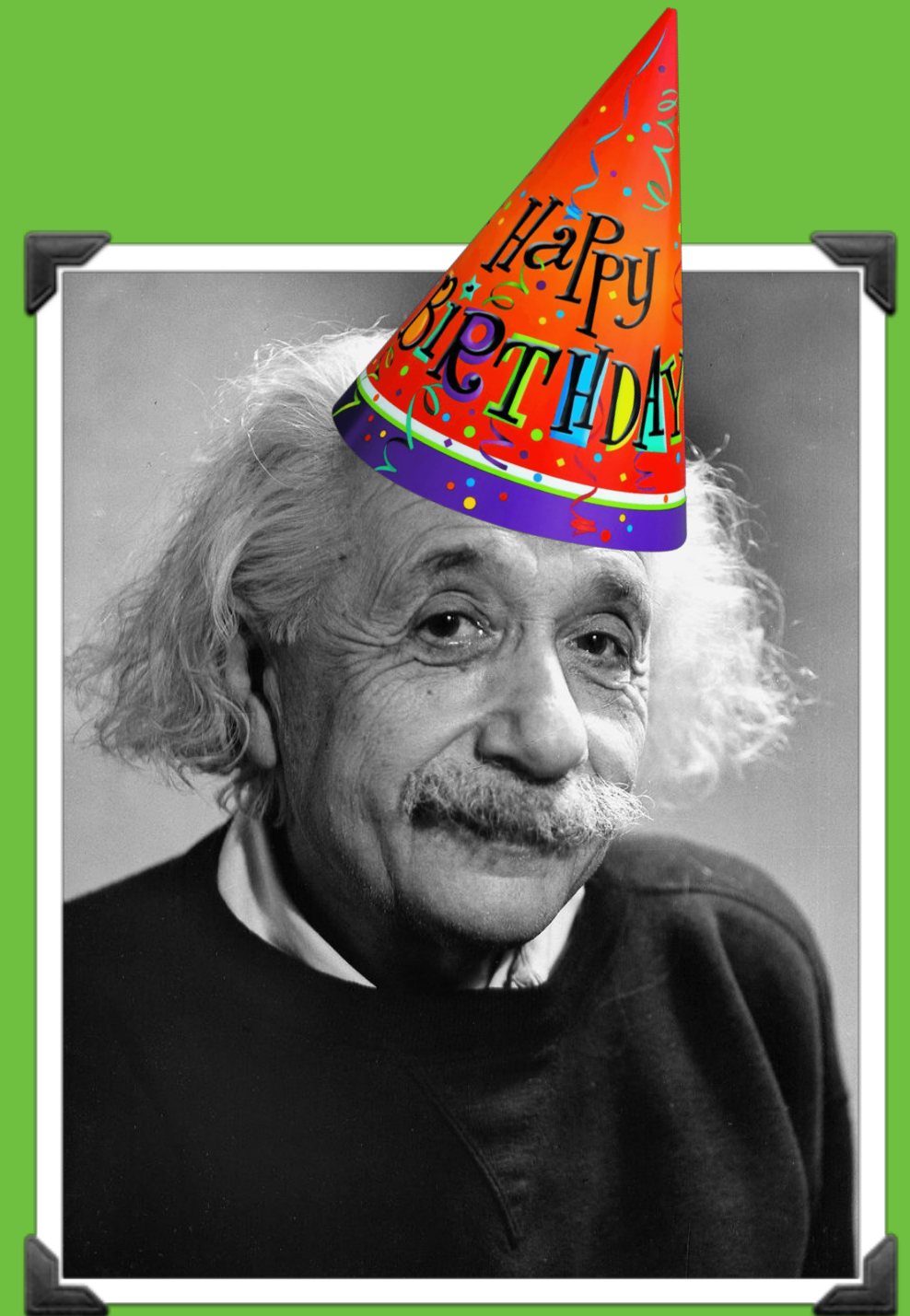
17 days until opening day

Kiss week

hi

Day 16, 14.03.2019

Einstein's General Theory
of Relativity, 2



housekeeping

Gotta come to class

question about anything?

I'll make a movie for you:



Madame Curie movie - we have a quorum in favor
right now: looks like Monday, March 18

Pizza FB poll established. Closes Sunday night.

Section 2 folks:

Project has begun in phases:

Document 1: software, introduction, tutorial: due March 22

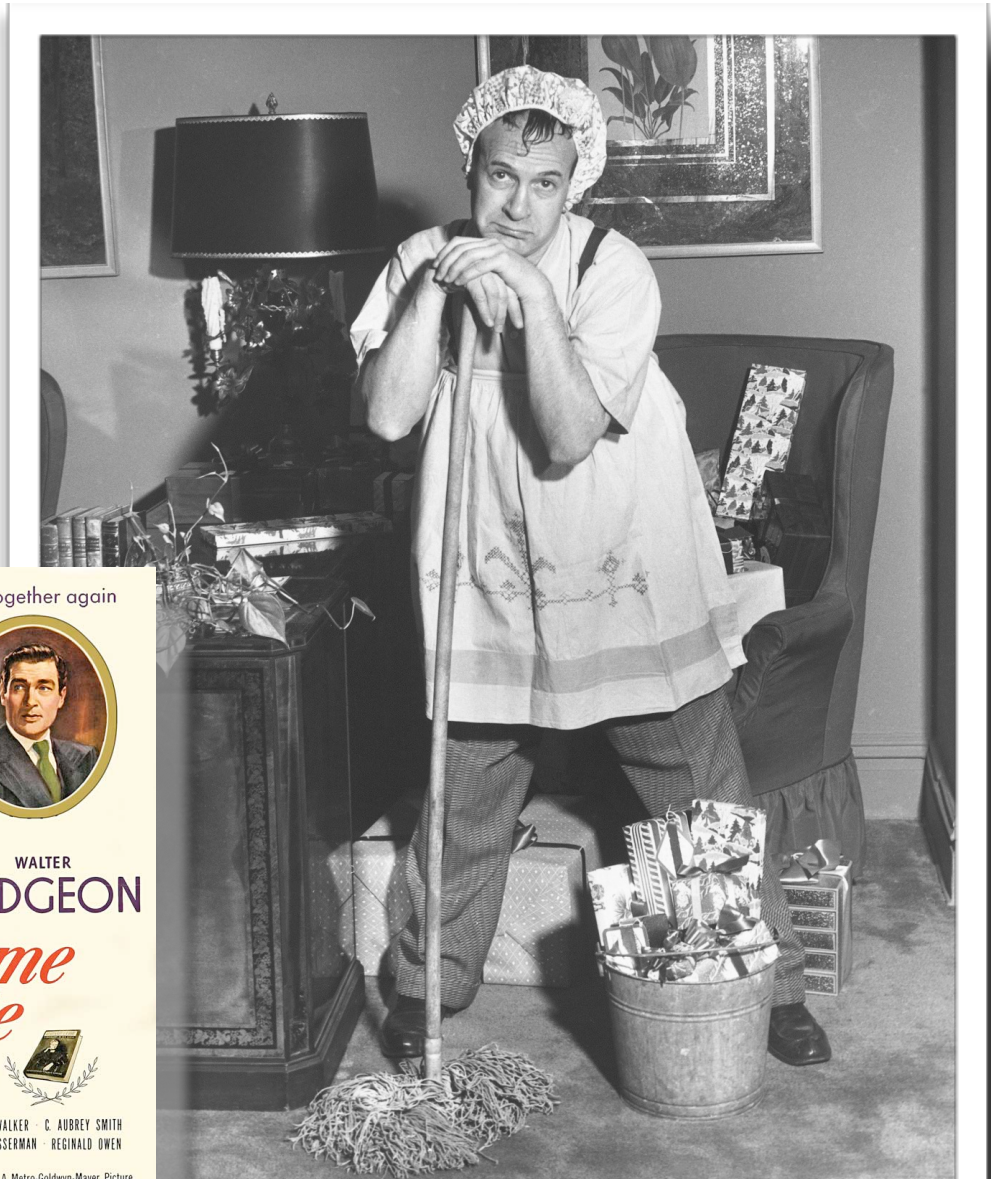
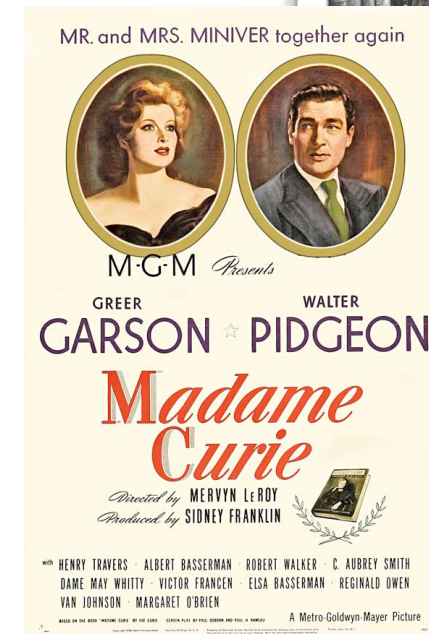
Document 2: your individual dataset and project instructions: due Final Exam

https://qstbb.pa.msu.edu/storage/QS&BB2019/Homework_Projects/honors_project_2019/MinervaInstructions1_2019.pages.pdf

MasteringAstronomy, finally after 3 emails and phone calls:

Course ID: MABROCK41459; free code: WSSPCT-BLIDA-INANE-TOGUE-RIGOT-UNRWA
check it! let me know if it is now working...

Grades to date: Projects, quizzes, notes in a pdf in the slides area
the rest of your grades are in LON-CAPA or MasteringPhysics



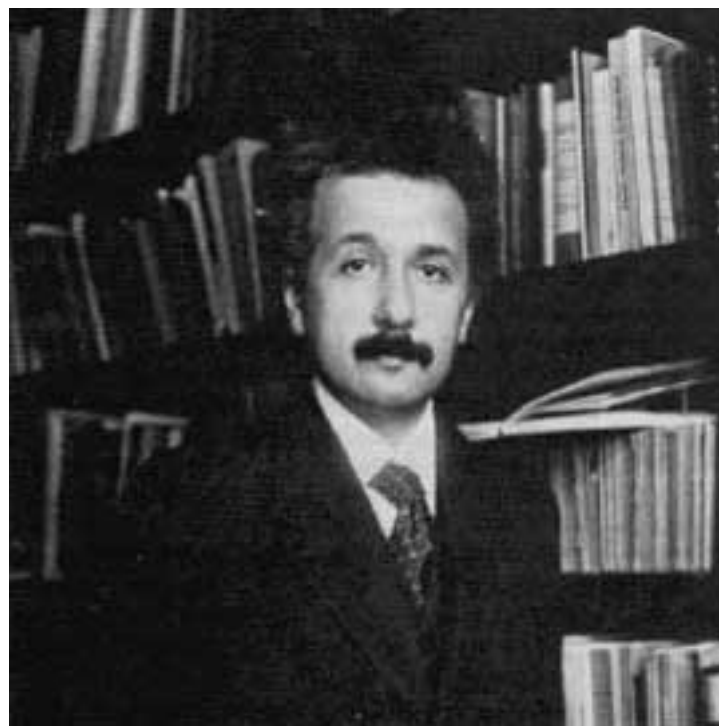
March 2019

Sunday	Monday	Tuesday	Wednesday	Thursday	Friday	Saturday
24	25	26	27	28	1	2
3	4	5	6	7	8	9
← spring break →						HW6
10	11	12	13	14	15	16
		lecture		lecture	HW6 due	HW7
17	18	19	20	21	22	23
	6pm, watch FB for room	lecture		lecture	HW7 due	HW8
24	25	26	27	28	29	30
		lecture		lecture	HW8 due	HW9
31	1	2	3	4	5	6
		lecture		lecture	HW9 due	



**KEEP
CALM
AND
LET'S
REVIEW**

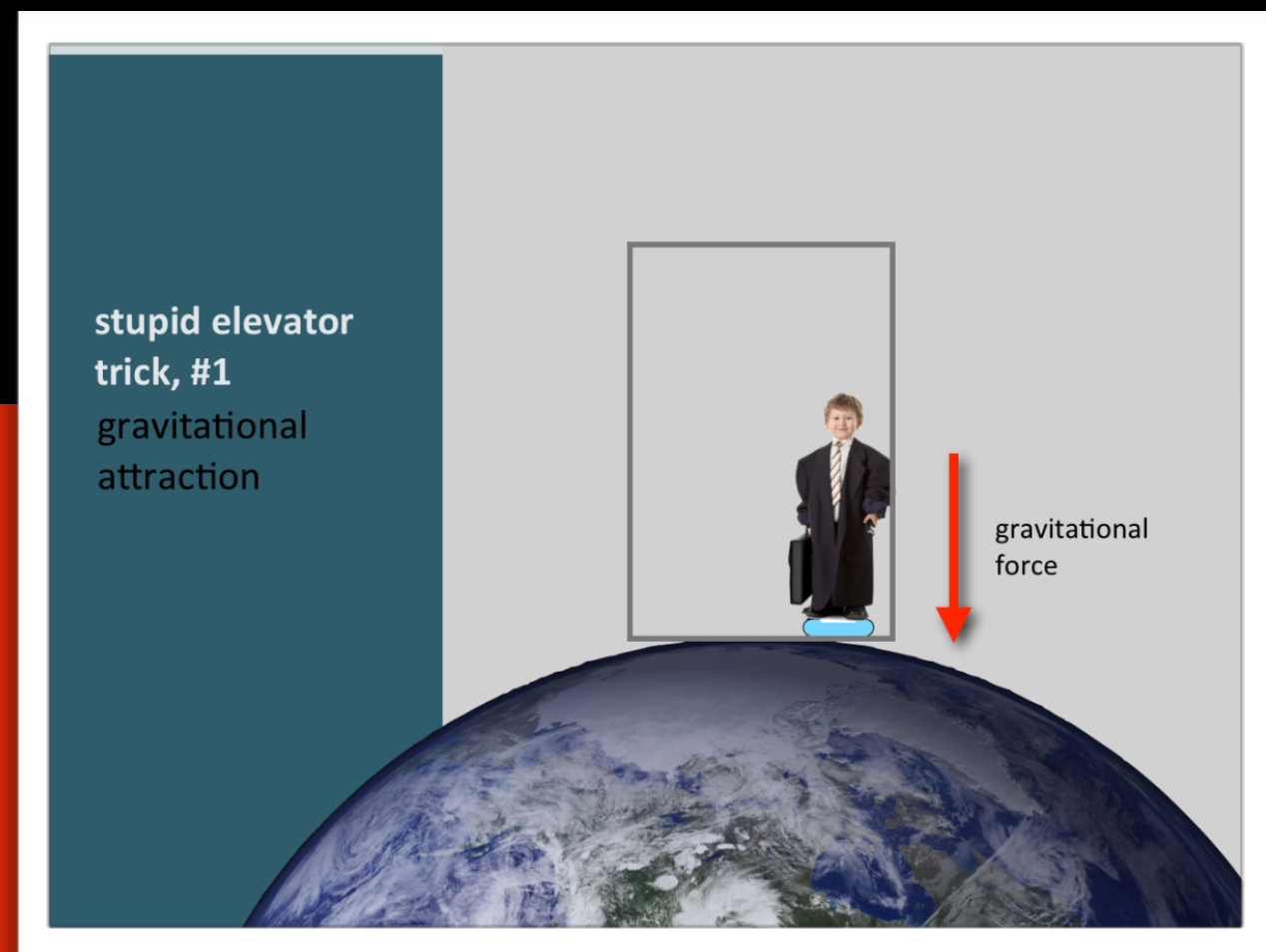
‘‘principle of equivalence’’



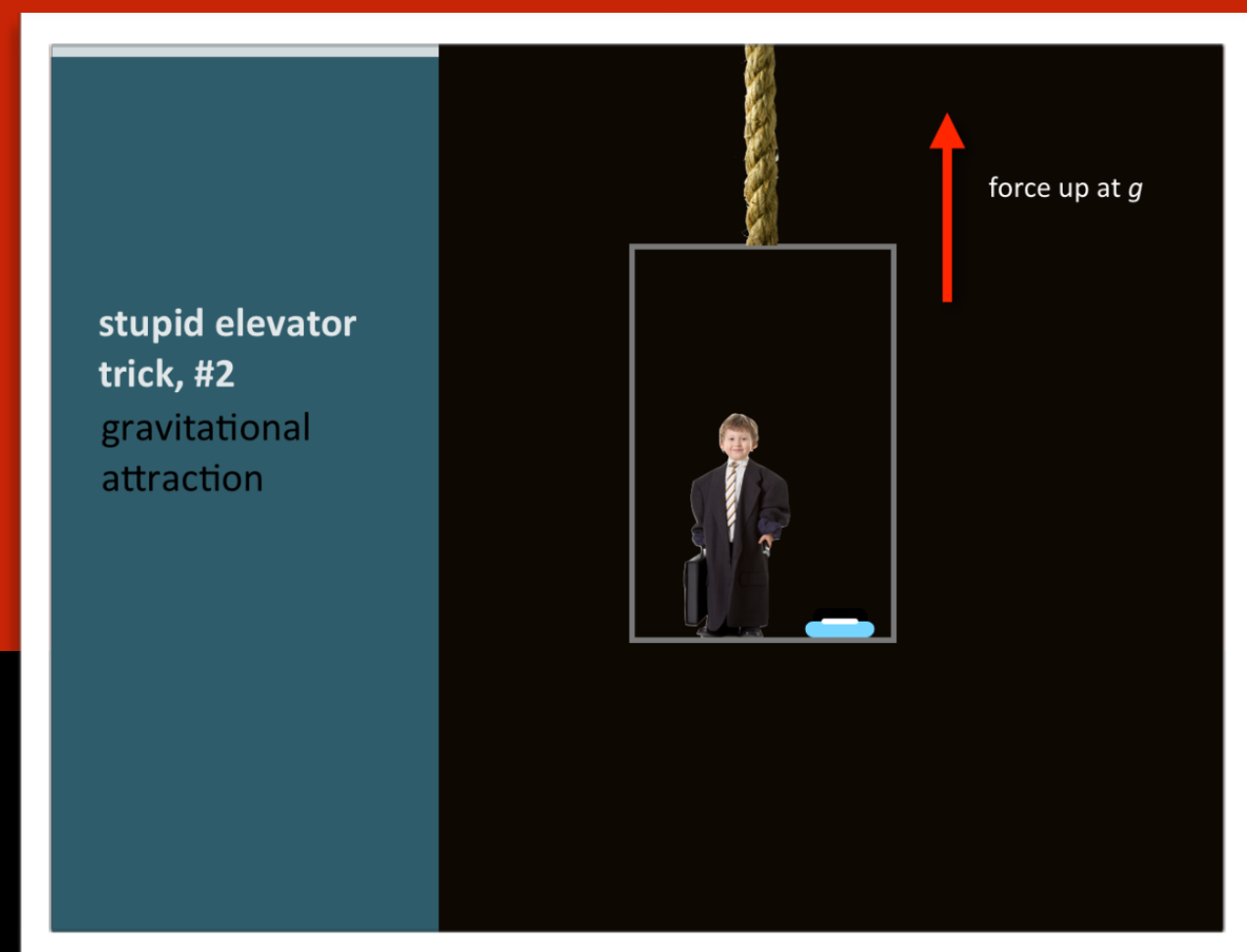
Equivalence Principle

his first aha moment

there's something the same about
acceleration and gravitation



identical



The Equivalence Principle demands that

If some phenomenon happens in a gravitational field,
then it must happen in an accelerated frame.

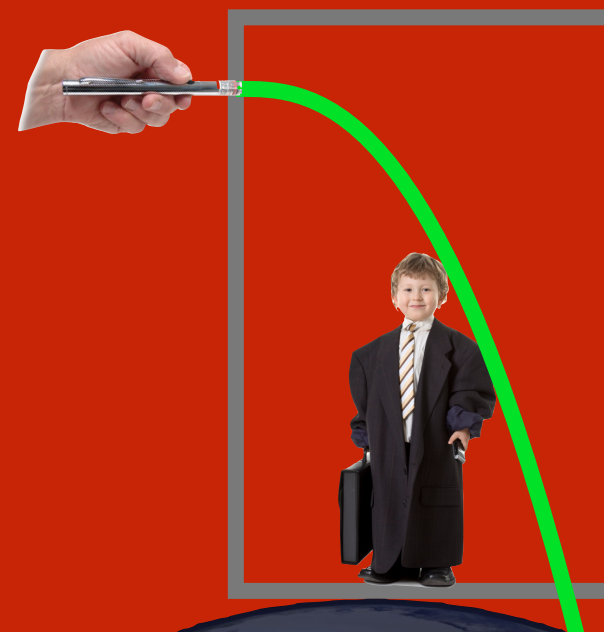
and

If some phenomenon happens in an accelerated frame field,
then it must happen in a gravitational field.

acceleration
warps space

from the Equivalence
Principle

gravity
should
warp space



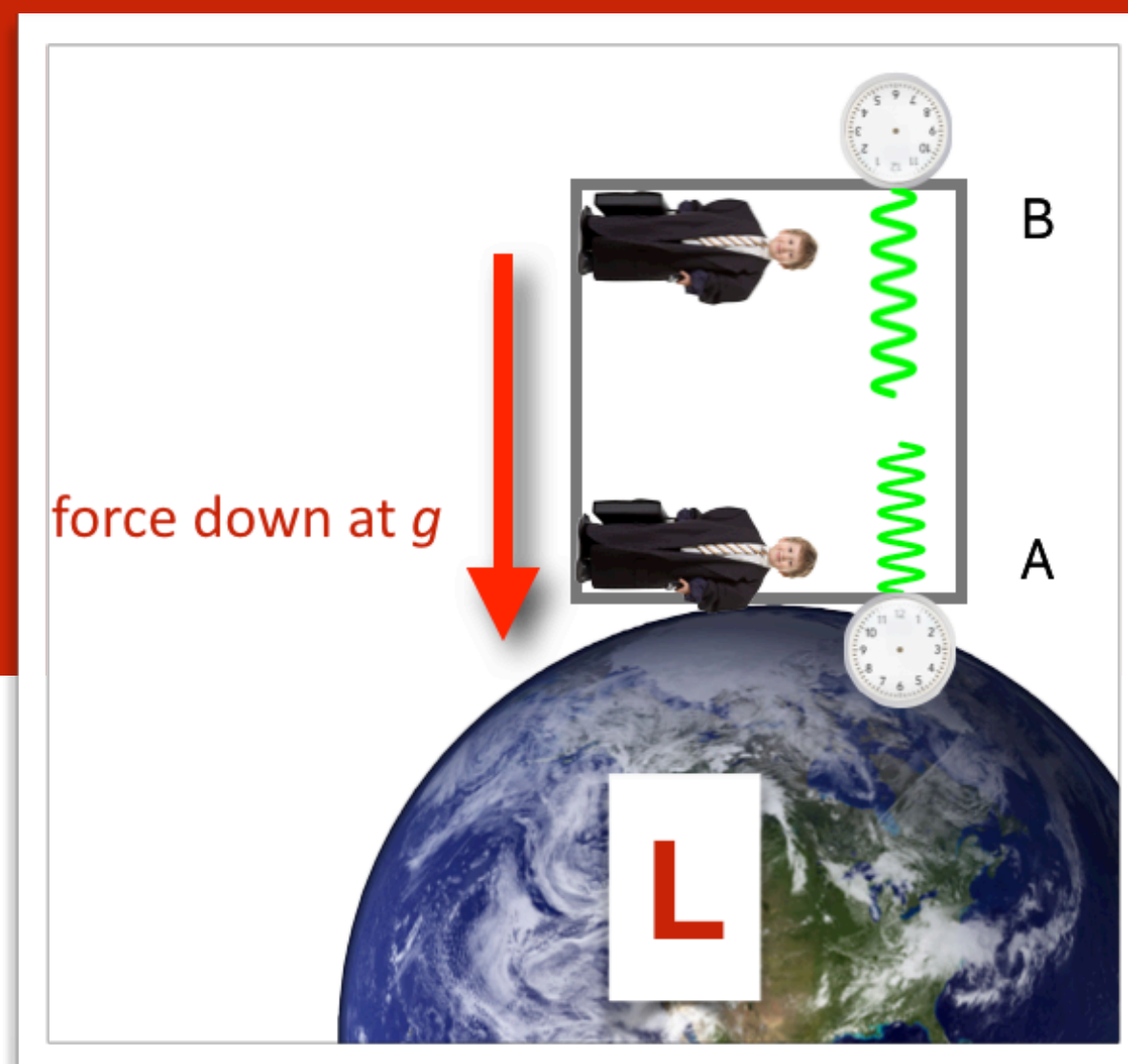
a beam of light in a high
gravitational field

should appear to bend

acceleration
warps time

from the Equivalence
Principle

gravity
should
warp time



a clock in a high
gravitational field

should appear to run slower than a clock in a weaker
gravitational field

"gravitational red shift"

gravitating bodies..masses:

warp both space and time.

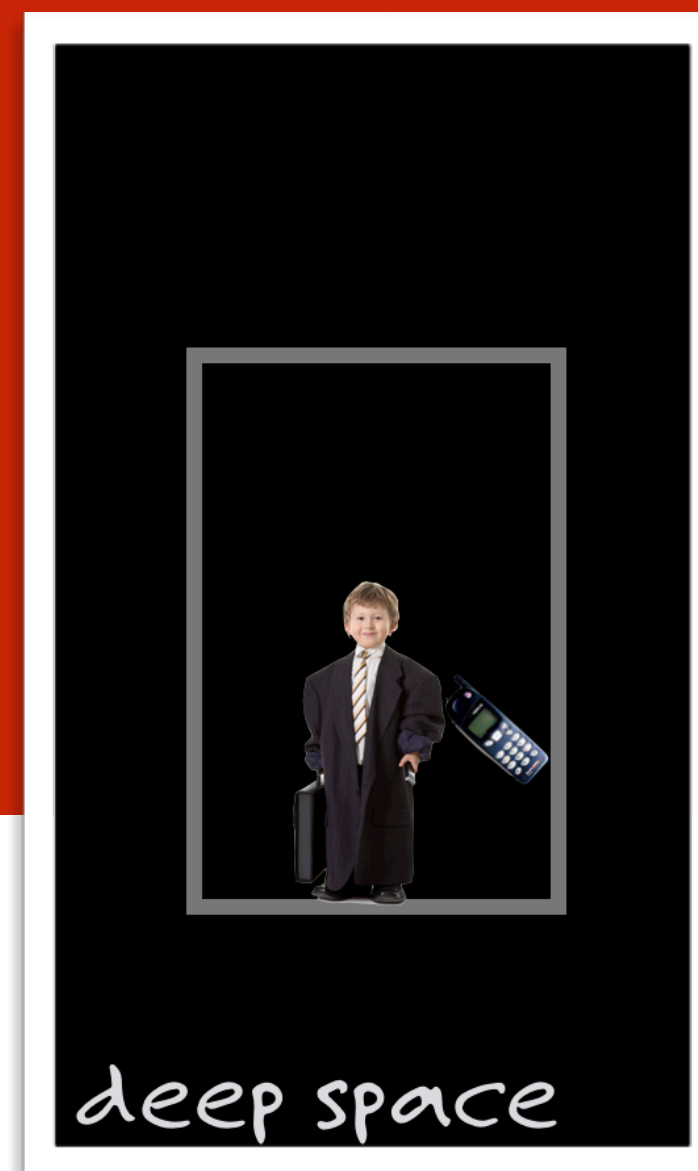
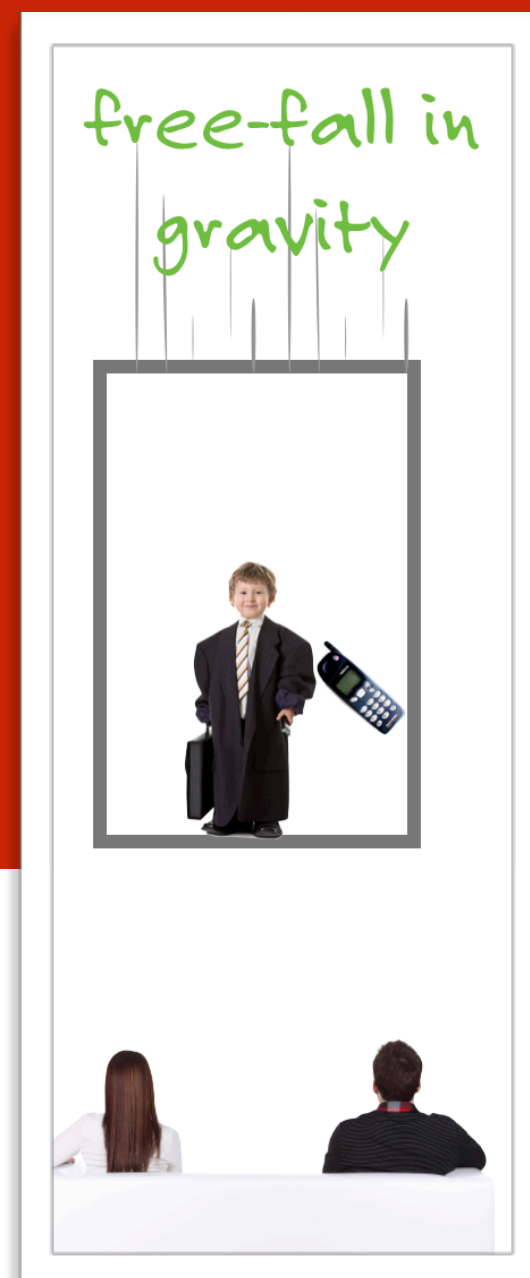
They warp: **spacetime**

furthermore!

free fall

in a gravitational
field eliminates
gravity

indistinguishable



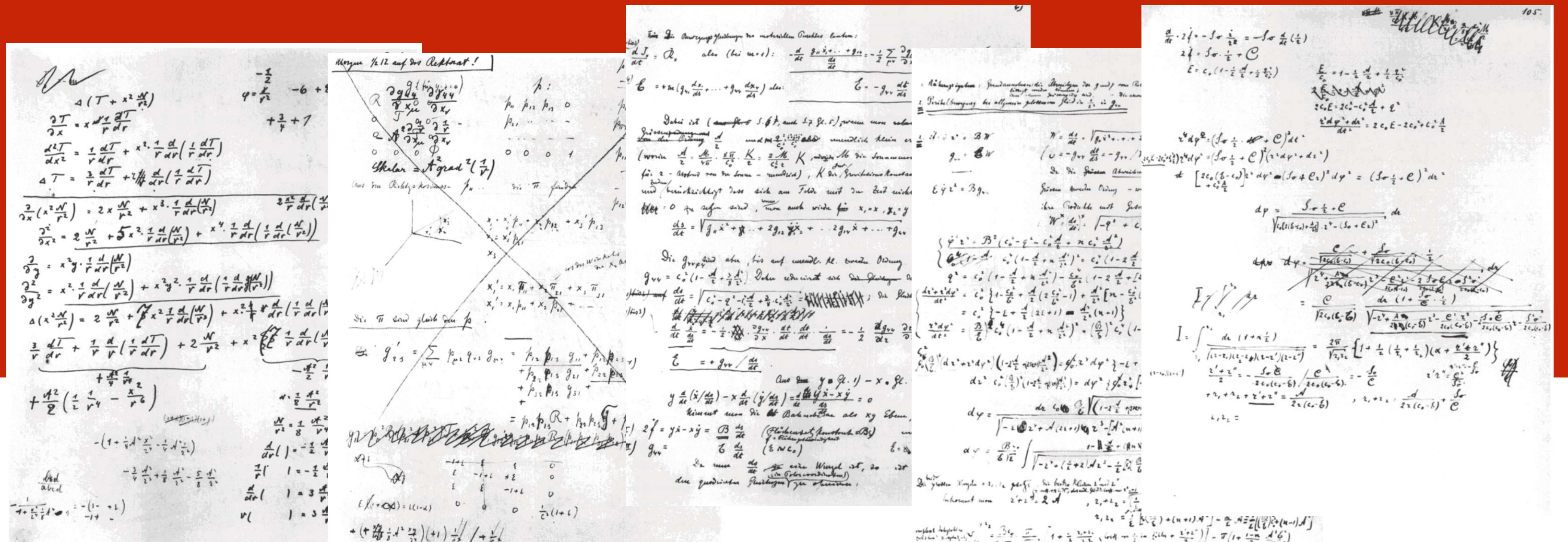
empty
outer space
without any
gravitational
fields

the free-fall recognition
became:

Maybe gravity is not a force at all?

modeling this was heroic

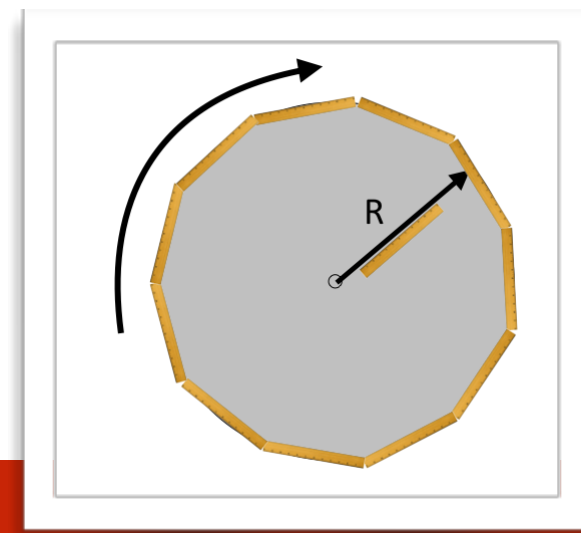
the most technically challenging piece of physics ever



there should be observable consequences to
the Equivalence Principle

and Einstein knew it

and calculated them - half a decade of Newton-like concentration



Einstein had to learn that geometry & energy-mass

interact & that space and time respond

After his "happy thought": 5 years for him to figure it out



he had to go back to
school...privately with
his buddy Marcel
Grossman

tests of general relativity

There are a handful of
“classic tests”

of these ideas:

that space and time are warped by
gravitation

Pound Rebka Gravitational Red Shift

The perihelion of Mercury's Orbit

Light bending around the Sun

“Gravitational Lensing”

“The Hafele-Keating experiment”

“Binary Pulsar period”

Black Holes

light beam

what about time?

use a clock

Gravitational Red Shift is built

into your phone's GPS

if you get where you want to go, you just

confirmed General Relativity

force up at g

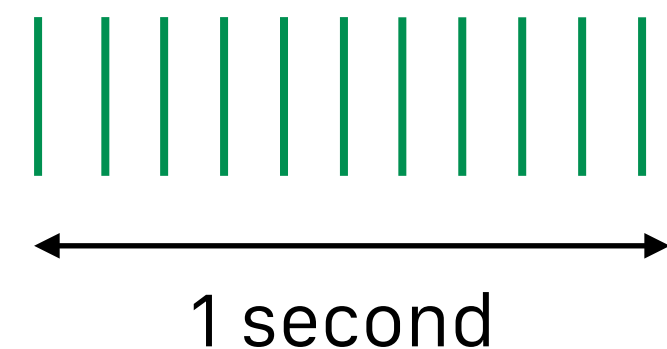
B receives at say 5 ticks per second



B would say that A's clock is longer between ticks:

Runs Slower

A sends at say 10 ticks per second



“Advance of the Perihelion of the Orbit of Mercury”

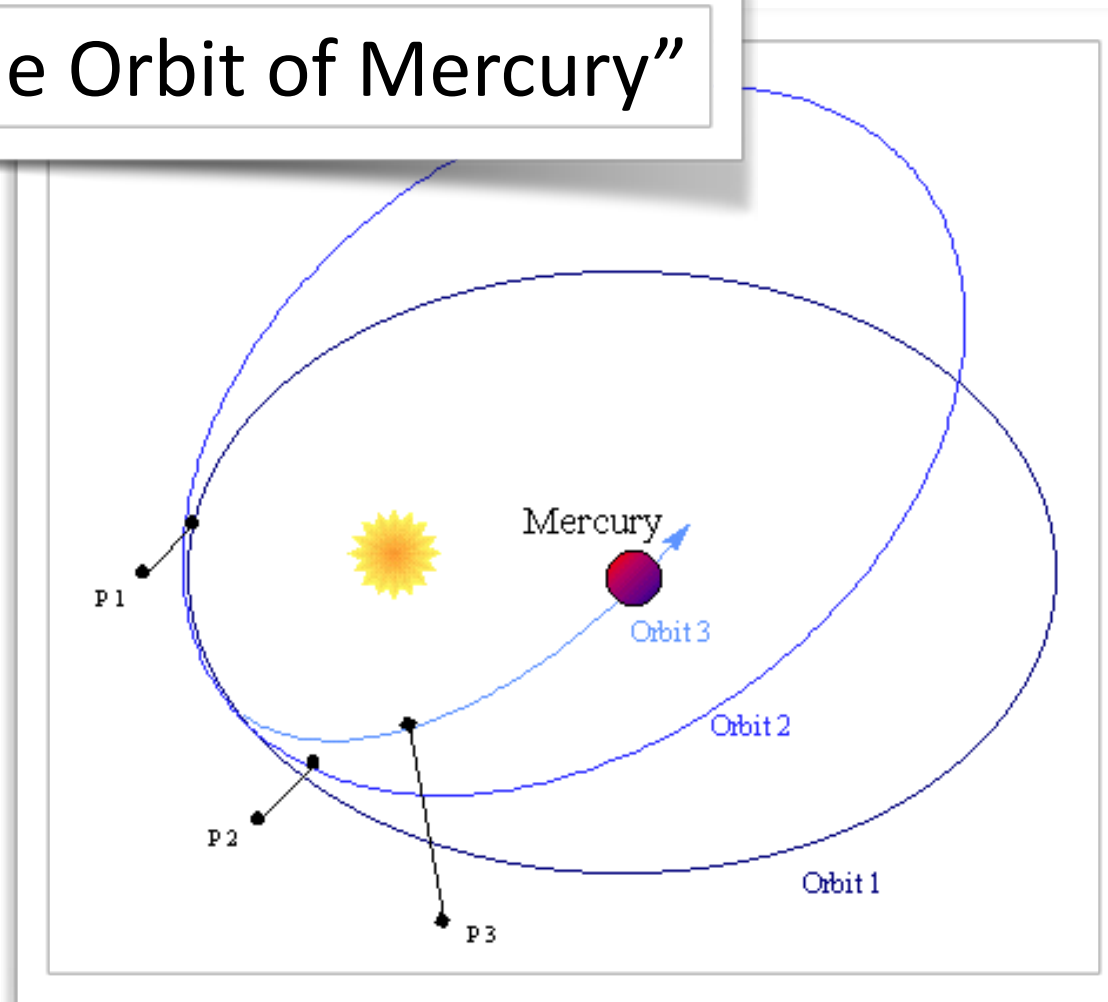
Vulcan?

Mercury

misbehaves

“advance of the
perihelion”

Einstein
calculated it
including the
sun's warping of
space



point of closest approach of
the orbit advances by 43
seconds of arc per century



1916: Got precisely the right amount.

Heart palpitations when he scribbled the result on his paper...

the mother of all experiments

the "solar eclipse" experiment

Google

solar eclipse experiment

Q

AllVideosImagesNewsShoppingMoreSettingsTools

About 6,480,000 results (0.49 seconds)

Videos



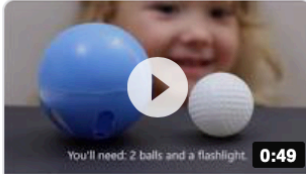
Solar eclipse experiments

KSDK News
YouTube · Aug 18, 2017



Astronomy 4 Kids:
Lunar and solar eclipses

Astronomy4Kids
YouTube · Sep 11, 2015



Solar Eclipse Activity for Kids

Trisha Stanley
YouTube · Aug 1, 2017

People also ask

What is the solar eclipse experiment?

What famous theory was proven during the 1919?

Who proved Einstein's theory of relativity?

How can I see a solar eclipse?

Feedback

A Picture-Perfect Solar Eclipse Experiment - Sky & Telescope

<https://www.skyandtelescope.com/...news/a-picture-perfect-solar-eclipse-experiment/>

Feb 16, 2018 - In the August 2016 issue of Sky & Telescope, I explained that I was going to set up an **experiment** to measure the gravitational deflection of ...

How a Total Solar Eclipse Helped Prove Einstein Right About ...

<https://www.space.com/37018-solar-eclipse-proved-einstein-relativity-right.html>

May 29, 2017 - The event will be a great opportunity to revisit a groundbreaking **experiment** that occurred during a total **solar eclipse**, and helped confirm Albert ...

Solar eclipse of May 29, 1919 - Wikipedia

https://en.wikipedia.org/wiki/Solar_eclipse_of_May_29,_1919

A total **solar eclipse** occurred on May 29, 1919. With the duration of totality at maximum eclipse of 6 minutes 51 seconds, it was the longest **solar eclipse** since ...

Greatest eclipse: 13:08:55 **Duration:** 411 sec (6 m 51 s)
Nature: Total **Max. width of band:** 244 km (152 mi)

Solar Eclipse Model | Science project | Education.com

<https://www.education.com> › Entire library › Science projects › First Grade › Science

Check out this fun science fair project idea for 1st grade: a **solar eclipse** model that demonstrates total, ... In this **experiment**, you'll use an apple as the sun.

The Solar Eclipse and Eddington's Experiment - Department of Physics

<https://www.cmu.edu/physics/news-events/news-archive/.../eclipse-eddington.html>

Aug 15, 2017 - At 1:45 on Monday afternoon, August 21, the moon will begin blocking the light coming to us from the Sun. Over the next half hour, the skies will ...

"Solar Eclipse Experiment"

light

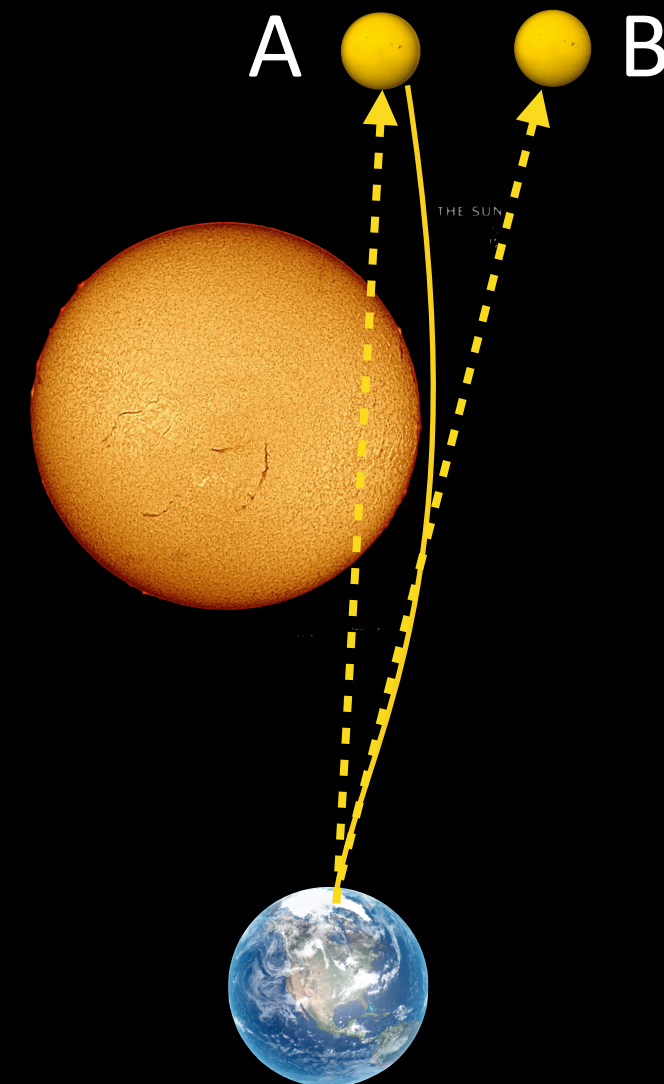
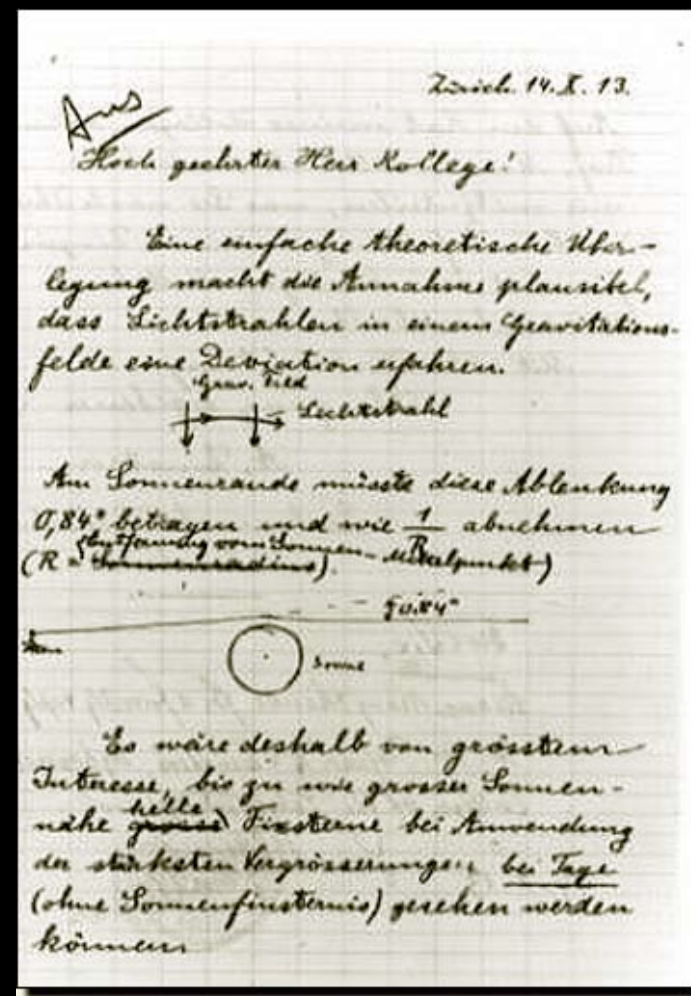
obeys the
strong
Equivalence
Principle

the laser
pointer...for real



The star is actually at A

The deflection should be
about $1/4$ milli-degree



But it would
appear to be
at B

1911 calculation – initially wrong, only the $E=mc^2$
component...

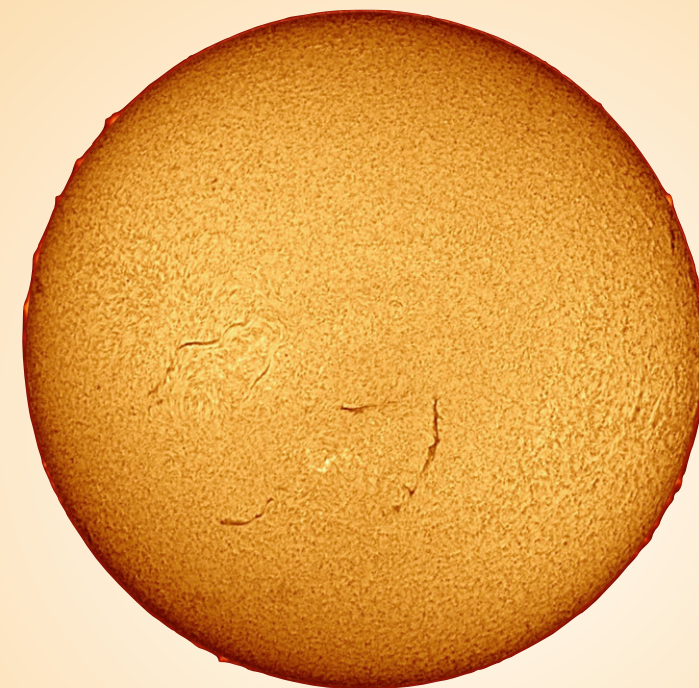
In 1915 he changed his 1911 calculation to
include the warping of space...worth x2

eclipse experiment May 29, 1919

Sir Arthur
Eddington led 2
teams:

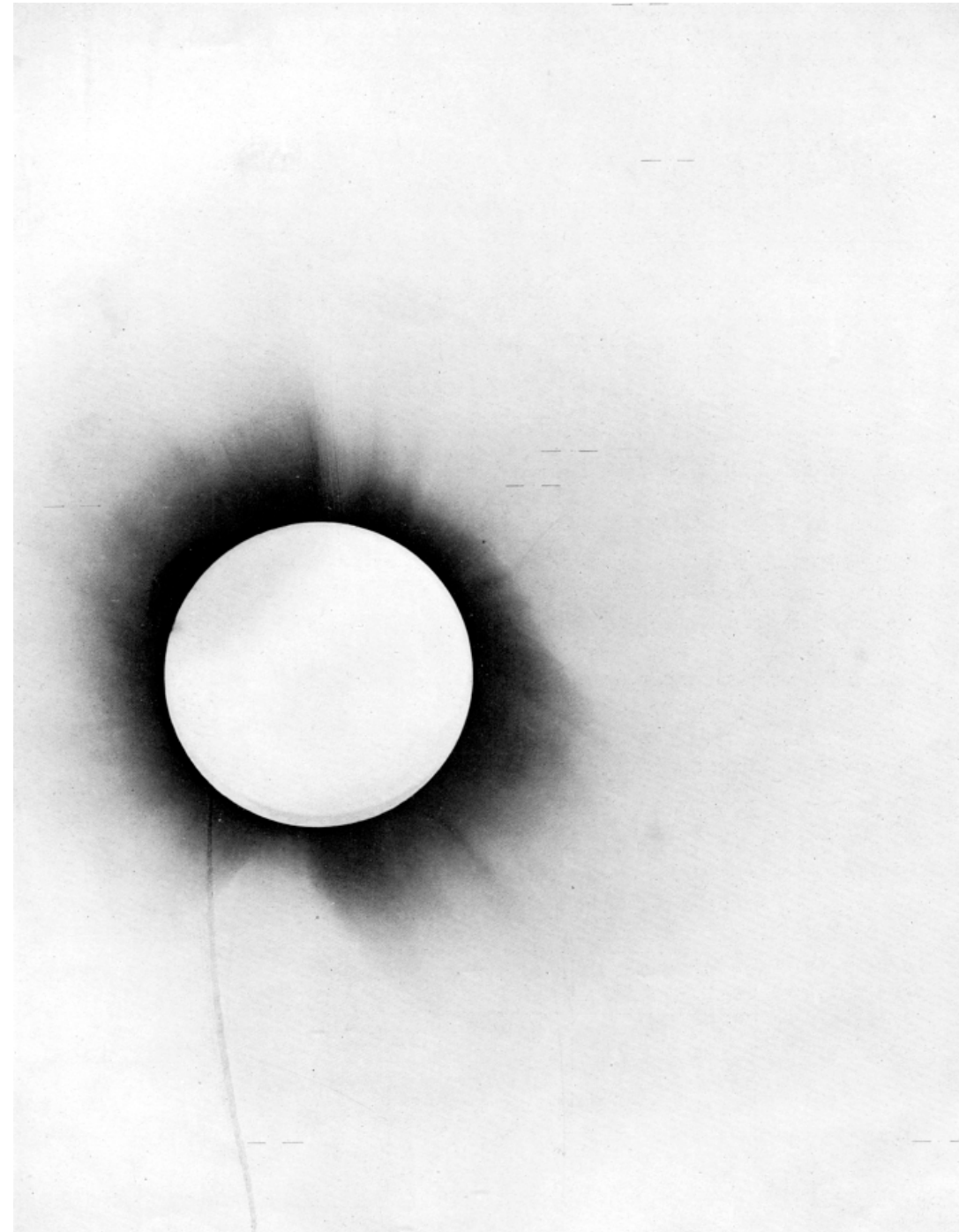
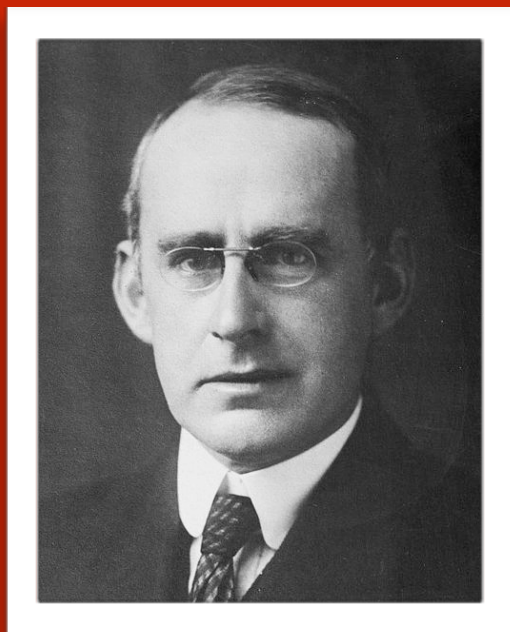
Gulf of Guinea

& Brazil



there was
some
cloudiness!

Eddington had 10
seconds to get a
photograph



1/16 plates had usable data

Eddington announced the result

November 6, 1919 at the Royal Astronomical Society
meeting

Einstein woke up in Berlin the next morning and was famous.

eclipse announcement at scientific meeting, 11/06/19:

instant celebrity, 11/07/19

cover of December 14, 1919 issue of
Berliner Illustrirte



caption: "A new great figure in world history: Albert Einstein, whose investigations signify a complete revision of our concepts of Nature, and are on a par with the insights of a Copernicus, a Kepler, and a Newton."

LIGHTS ALL ASKEW IN THE HEAVENS

Men of Science More or Less
Agog Over Results of Eclipse
Observations.

EINSTEIN THEORY TRIUMPHS

Stars Not Where They Seemed
or Were Calculated to be,
but Nobody Need Worry.

A BOOK FOR 12 WISE MEN

No More in All the World Could
Comprehend It, Said Einstein When
His Daring Publishers Accepted It.

Special Cable to THE NEW YORK TIMES.
LONDON, Nov. 9.—Efforts made to put in words intelligible to the non-scientific public the Einstein theory of light proved by the eclipse expedition so far have not been very successful. The new theory was discussed at a recent meeting of the Royal Society and Royal Astronomical Society, Sir Joseph Thomson, President of the Royal Society, declares it is not possible to put Einstein's theory into really intelligible words, yet at the same time Thomson adds:

"The results of the eclipse expedition demonstrating that the rays of light from the stars are bent or deflected from their normal course by other aerial bodies acting upon them and consequently the inference that light has weight form a most important contribution to the laws of gravity given us since Newton laid down his principles."

Thompson states that the difference between theories of Newton and those of Einstein are infinitesimal in a popular sense, and as they are purely mathematical and can only be expressed in strictly scientific terms it is useless to endeavor to detail them for the man in the street.

the Times golf editor

New York Times,
November 10, 1919

One of the speakers at the Royal Society's meeting suggested that Euclid was knocked out. Schoolboys should not rejoice prematurely, for it is pointed out that Euclid laid down the axiom that parallel straight lines, if produced ever so far, would not meet. He said nothing about light lines.

Some cynics suggest that the Einstein theory is only a scientific version of the well-known phenomenon that a coin in a basin of water is not on the spot where it seems to be and ask what is new in the refraction of light.

Albert Einstein is a Swiss citizen, about 50 years of age. After occupying a position as Professor of Mathematical Physics at the Zurich Polytechnic School and afterward at Prague University, he was elected a member of Emperor William's Scientific Academy in Berlin at the outbreak of the war. Dr. Einstein protested against the German professors' manifesto approving of Germany's participation in the war, and at its conclusion he welcomed the revolution. He has been living in Berlin for about six years.

When he offered his last important work to the publishers he warned them there were not more than twelve persons in the whole world who would understand it, but the publishers took the risk.

New York Times, December 3, 1919

EINSTEIN EXPOUNDS HIS NEW THEORY

It Discards Absolute Time and
Space, Recognizing Them Only
as Related to Moving Systems.

IMPROVES ON NEWTON

Whose Approximations Hold for
Most Motions, but Not Those
of the Highest Velocity.

INSPIRED AS NEWTON WAS

But by the Fall of a Man from a
Roof Instead of the Fall
of an Apple.

Copyright, 1919, by The New York Times Company
Special Cable to THE NEW YORK TIMES.

BERLIN, Dec. 2.—Now that the Royal Society, at its meeting in London on Nov. 6, has put the stamp of its official authority on Dr. Albert Einstein's much-debated new "theory of relativity," man's conception of the universe seems likely to undergo radical changes. Indeed, there are German savants who believe that since the promulgation of Newton's theory of gravitation no discovery of such importance has been made in the world of science.

When THE NEW YORK TIMES correspondent called at his home to gather from his own lips an interpretation of what to laymen must appear the book with the seven seals, Dr. Einstein him-



now recovered from exhaustion and photogenic: 1920

Gravitational Lensing - an off-hand prediction of Einstein



www.spacetelescope.org

Foreground objects can distort, and magnify
distant background galaxies.



gravitational lensing now a tool

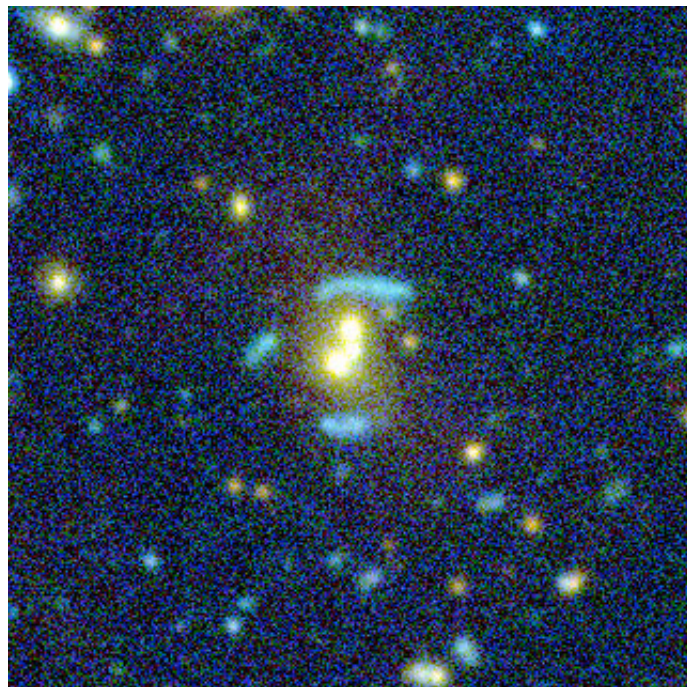
no longer a discovery!

studying dark
matter:
looking for
Massive
Astrophysical
Compact Halo
ObjectS

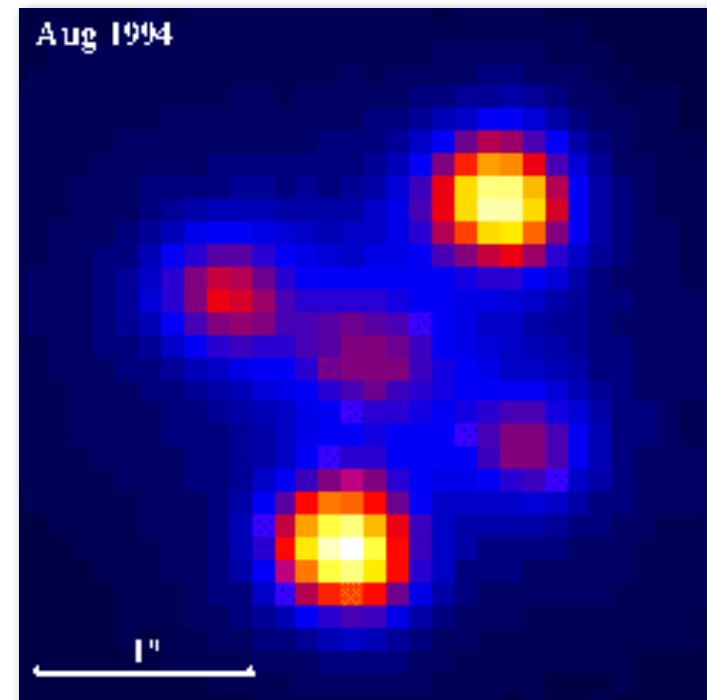
“Gravitational Lensing”

MACHOS

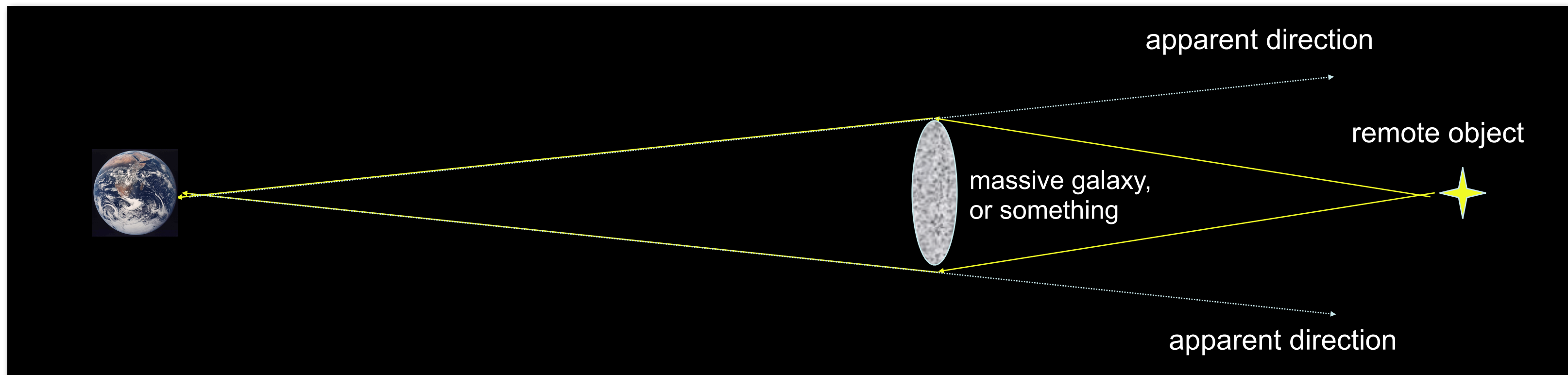
Credit: Canada-France-Hawaii
Telescope Corporation 2006.



“Einstein Cross” - 4 images of a quasar



Gravitational Lens
Galaxy Cluster 0024+1654
Hubble Space Telescope · WFPC2



Second view of this:

“The Hafele-Keating experiment”

an atomic clock was carefully carried around the world in 1972 and carefully calibrated and compared with ground-based clocks

There are a number of corrections: accelerations, decelerations, the rotation of the orbit, the fact that the earth is not inertial - but relativity was absolutely correct

Predicted Effect	Flying East	Flying West
GTR (Gravitation)	+ 144 ± 14 ns	+ 179 ± 18 ns
STR (Velocity)	- 184 ± 18 ns	+ 96 ± 18 ns
Total	- 40 ± 23 ns	+ 275 ± 21 ns
measured:	- 59 ± 10 ns	+273 ± 7 ns

redone twice more in airplanes and rockets/satellites



J. Hafele and R. Keating

about half of their effect was due to the gravitational difference between Earth and the flight's altitude

spacetime in general relativity

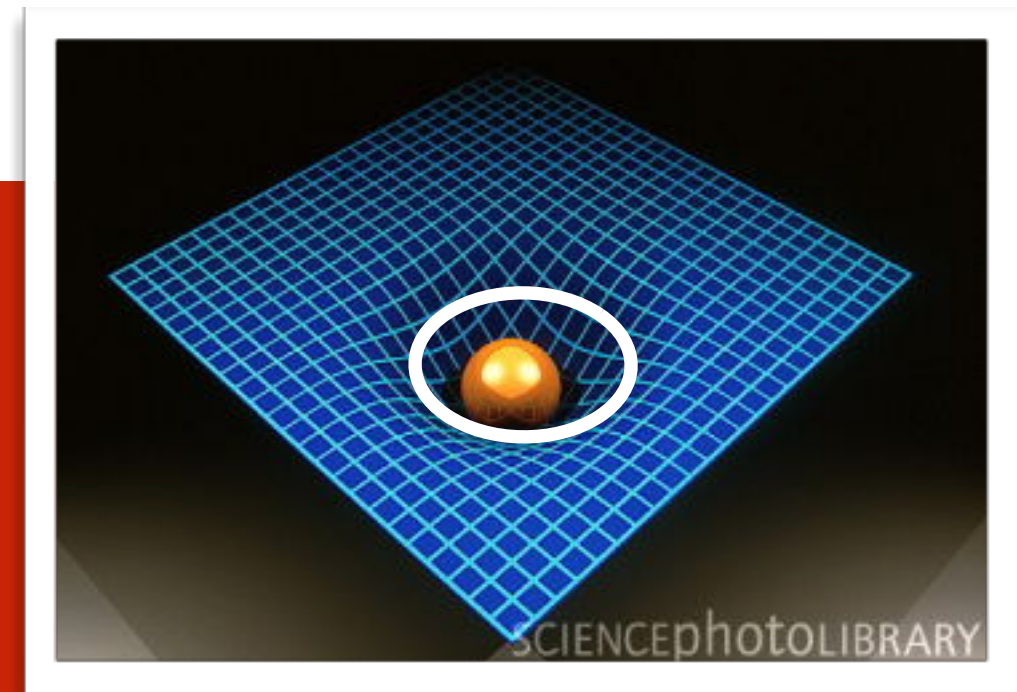
Earth's orbit is then just us following the shortest distance around the sun...not a gravitational force

Einstein got rid of
gravitational forces in GR

Masses warp spacetime...

Since the shortest distance between two spacetime points is a light-path, this "maps" the shape

In GR gravity is not a force, but a "topography" of spacetime that forces objects to take the shortest curved path in spacetime



okay .

Spacetime might
be curvy, bumpy,
..."warped"

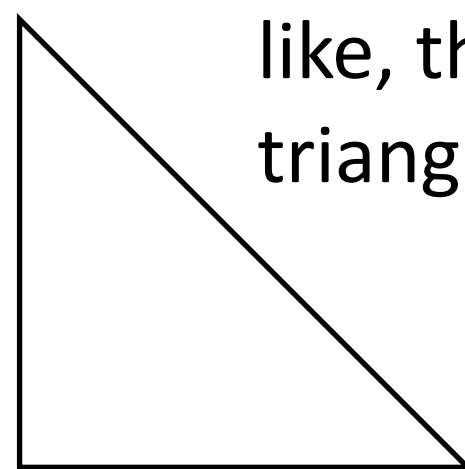
a "non-Euclidean
geometry"?

Euclid's Geometry starts with 4 terms and 4+1 postulates:

Point, Line, Plane, Space

1. A straight line can be drawn between any two points
2. A finite line can be extended infinitely in both directions
3. A circle can be drawn with any center and any radius
4. All right angles are equal to each other
5. Given a line and a point not on the line, only one line can be drawn through the point parallel to the line

a System of a series of proofs, each building on the previous, to a whole system of mathematics



like, the sum of the interior angles of any triangle is 180°

like, Pythagoras' Theorem

like, actually... a lot of algebra problems before algebra was invented

Einstein's mathematics of GR

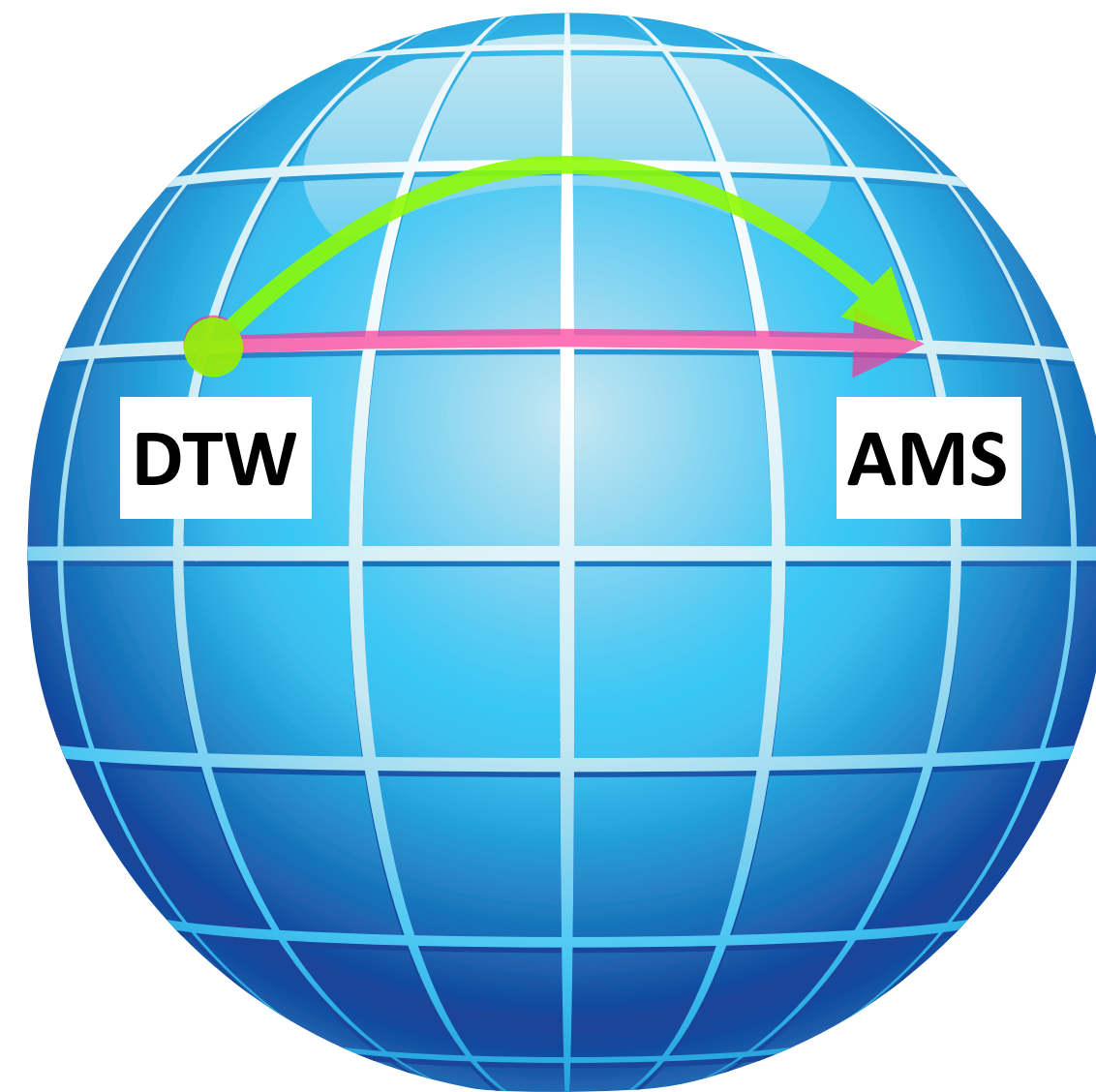
led him to have to consider non-Euclidean Geometries
which were still timidly being studied by mathematicians

not so far-fetched

we live in such a geometry

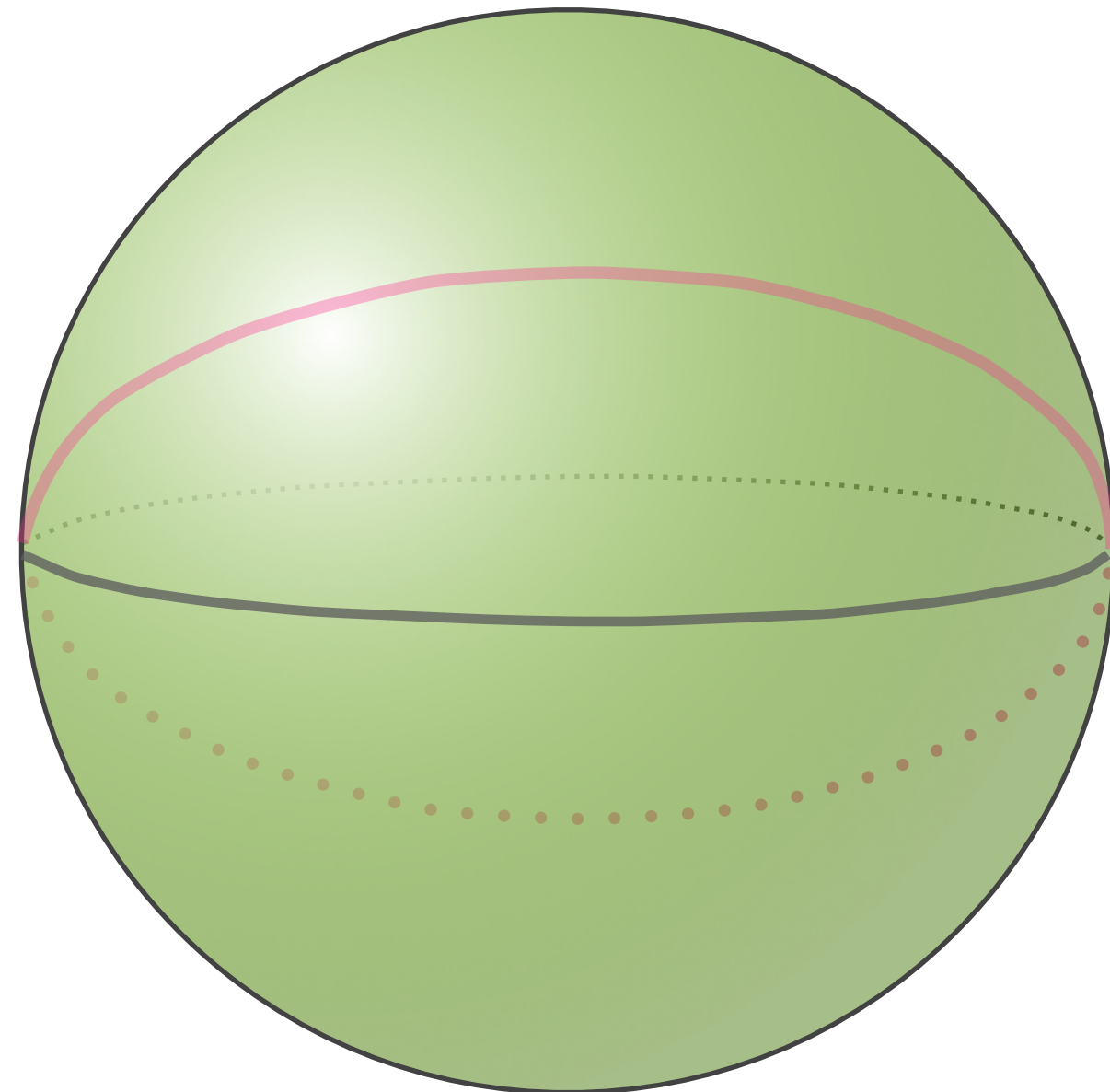


what's a
“straight
line”



on a sphere?

shortest distance
between 2 points



Euclid's 5th Postulate

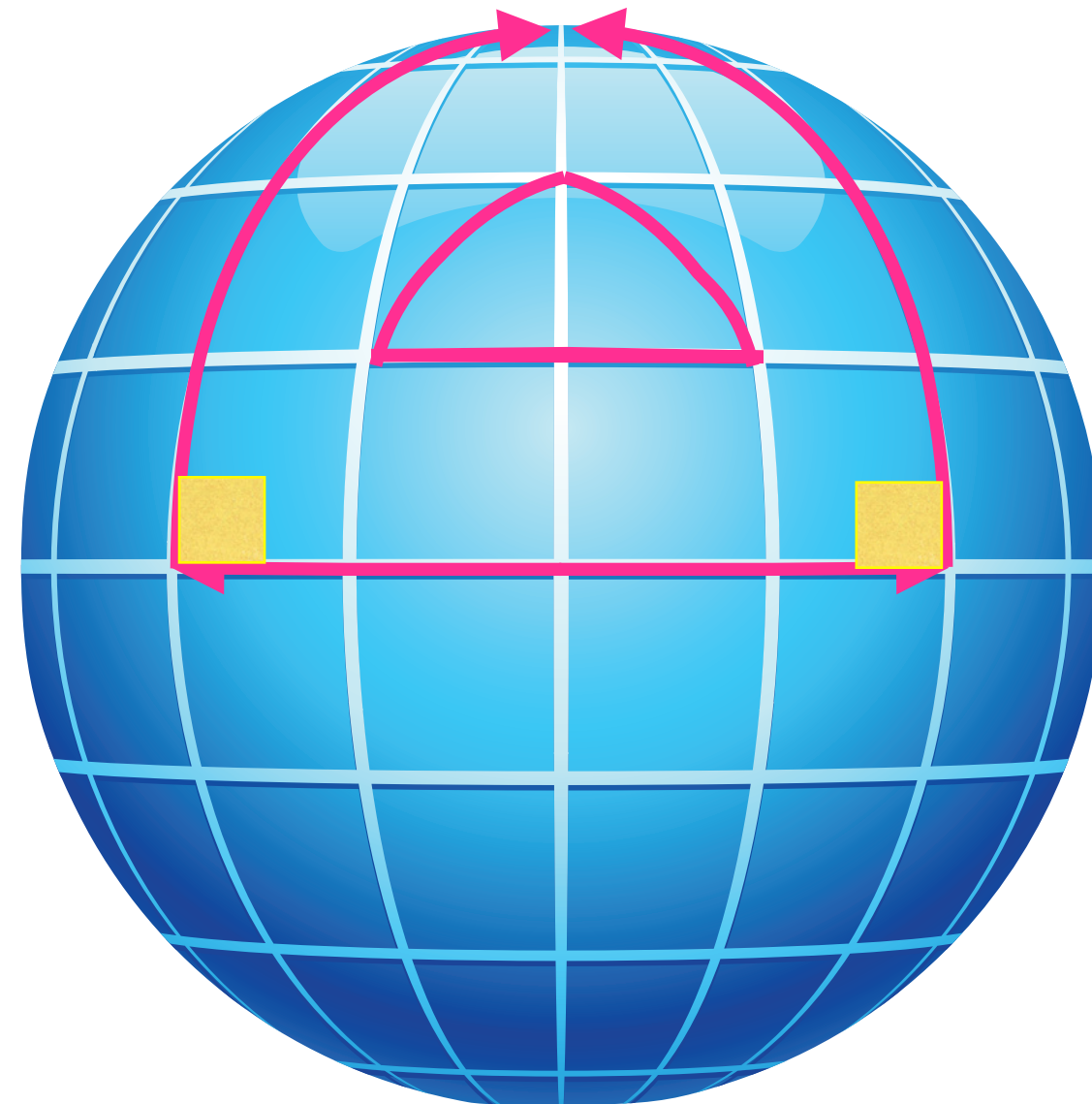
parallel lines
never meeting?

only in a flat space

sum of interior
angles in a triangle
 $= 180^\circ$?

only in flat space

on sphere $> 180^\circ$



‘‘warping’’

means that geometry

spacetime geometry

mixes with mass, energy, and pressure

General Relativity

Einstein's GR
equation

complicated
mathematics

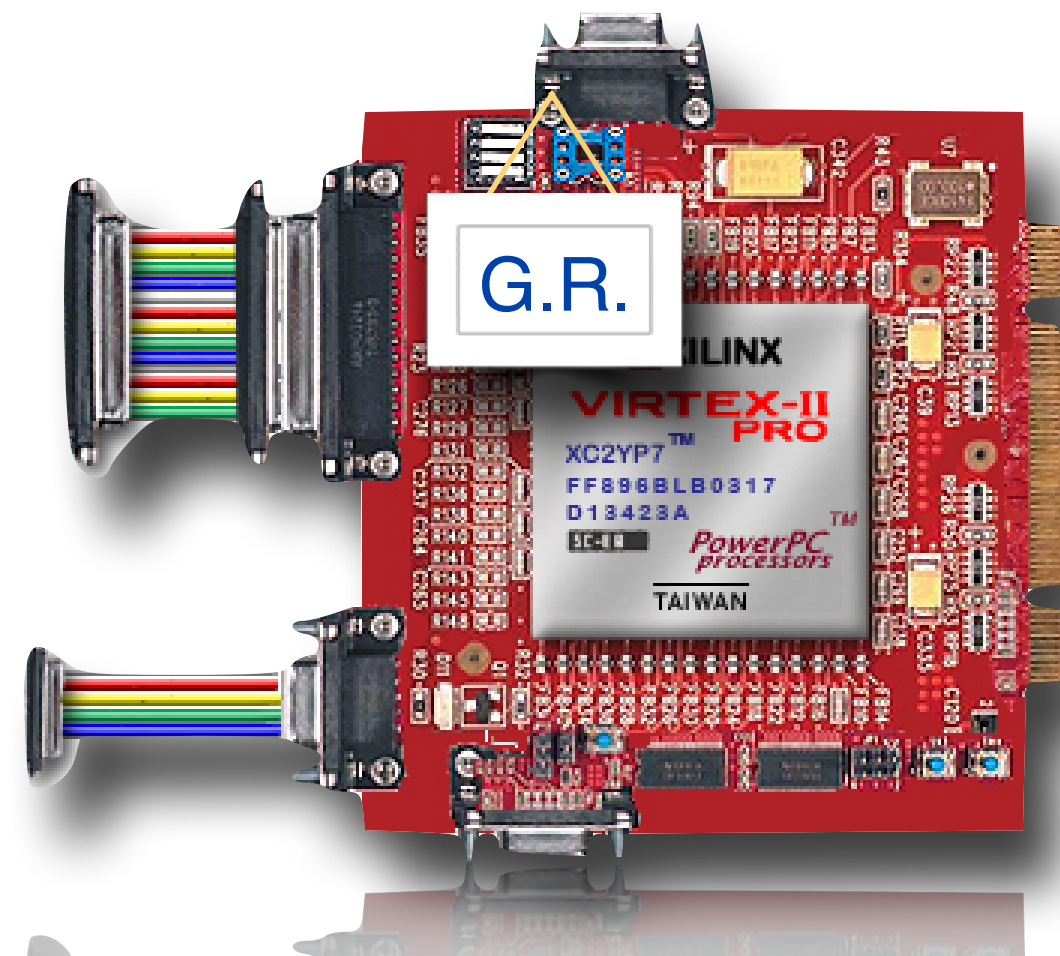
geometry of
spacetime



mass-energy,
pressure,
&
momentum

$$R_{\mu\nu} - \frac{1}{2}Rg_{\mu\nu} = \frac{8\pi}{c^4}T_{\mu\nu}$$

we'll call it: " $G = T$ "



Einstein grossly
underestimated

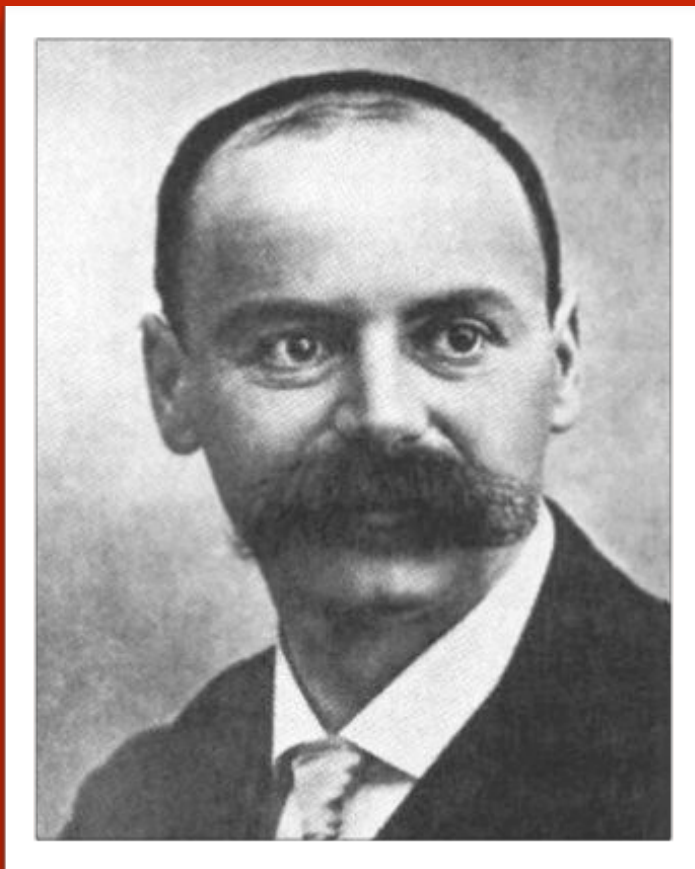
the richness of his theory

he knew he'd exhausted the possible solutions to
the GR equations

He was wrong...and irritable about it

wrong.
Almost
immediately:

from the
foxhole, 1915



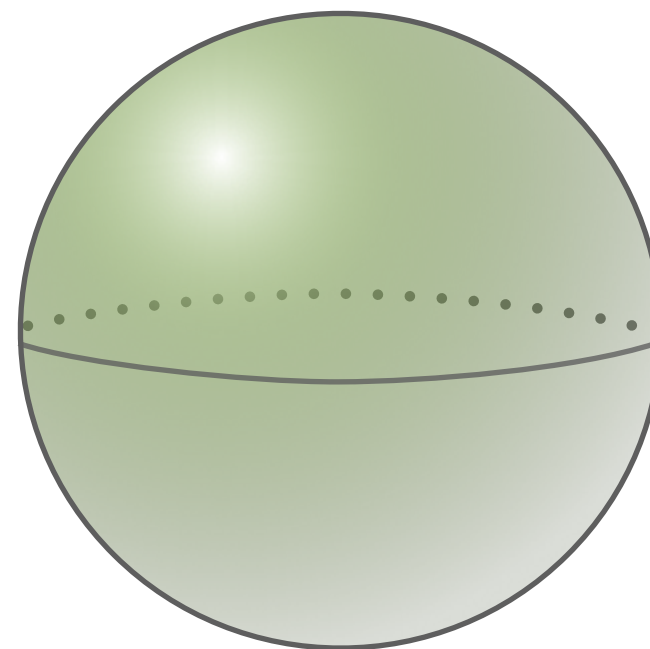
Karl Schwarzschild, 1873-1916

Yes. I mean *from* a foxhole.

The **first exact solution** to GR...Einstein had used some approximations for light-bending, etc.

The equations of spacetime outside of a spherical mass.

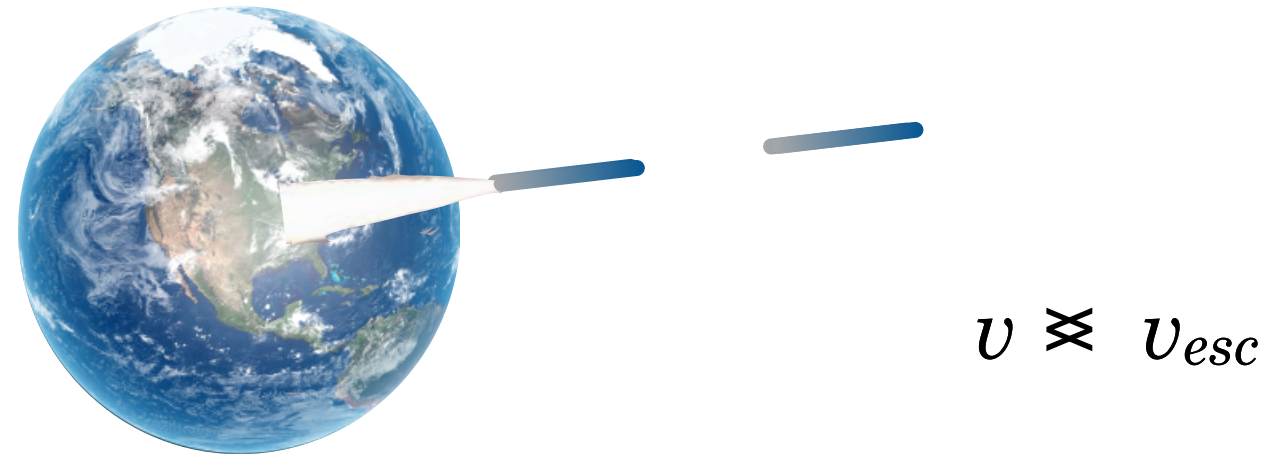
a big mass.



escape

Suppose a rocket is shot straight up... when it goes “ballistic” (no propulsion)...what happens?

It depends.



More initial velocity, the more likelihood that the rocket will escape the pull of the Earth’s gravity.

This happens when the kinetic energy = potential energy

$$v_{esc} = \sqrt{\frac{2GM_E}{R_E}}$$

From Earth: 11.2 kilometers per second...~25,000 mph

what about light?

suppose the
question is not:

"What's the escape
velocity from a
sphere of mass M ?"

BUT

"What's the radius of a mass M for which the escape velocity
is $= c$?"

$$v_{\text{esc}} = \sqrt{\frac{2GM_E}{R_E}} \longrightarrow c = \sqrt{\frac{2GM}{R_S}}$$

R_S called the Schwarzschild Radius

$$R_S = \frac{2GM}{c^2}$$

It seemed to be a magic radius...

the
Schwarzschild
Radius falls
out of his
solution to
G.R.

it's not likely

R_S is incredibly small

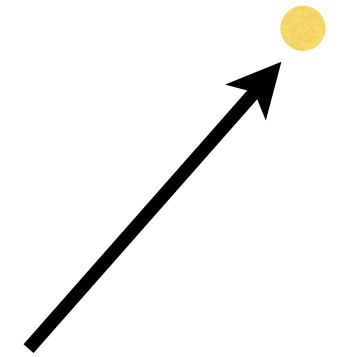
*and density,
incredibly high*

All of the mass of:



1.6 B meters

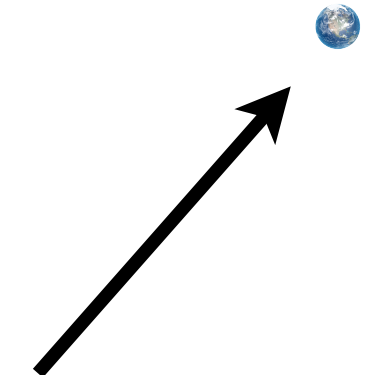
inside of R_S :



$R_S = 3000 \text{ m}$



12 M meters



$R_S = 1 \text{ cm}$

Impossible, right?...thought to be a disaster for the theory.

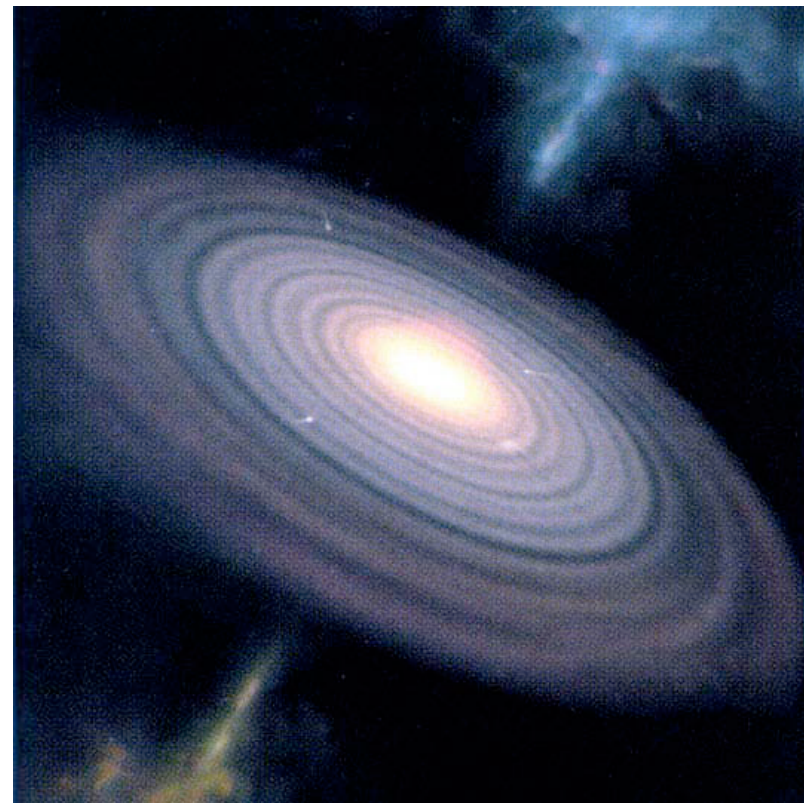
everyone
fretted over
this for
more than a
decade

1932, Georges
Lemaître found
that a slight
change of
coordinate axes

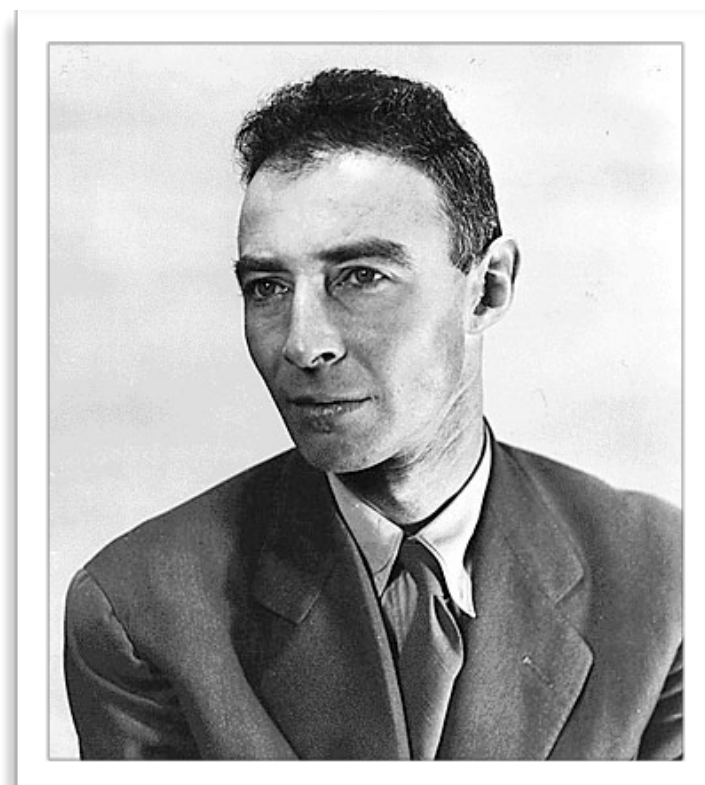
changed the problem
completely

Black Holes

The Schwarzschild Radius was not a flaw in the theory
simply an insult from Nature!



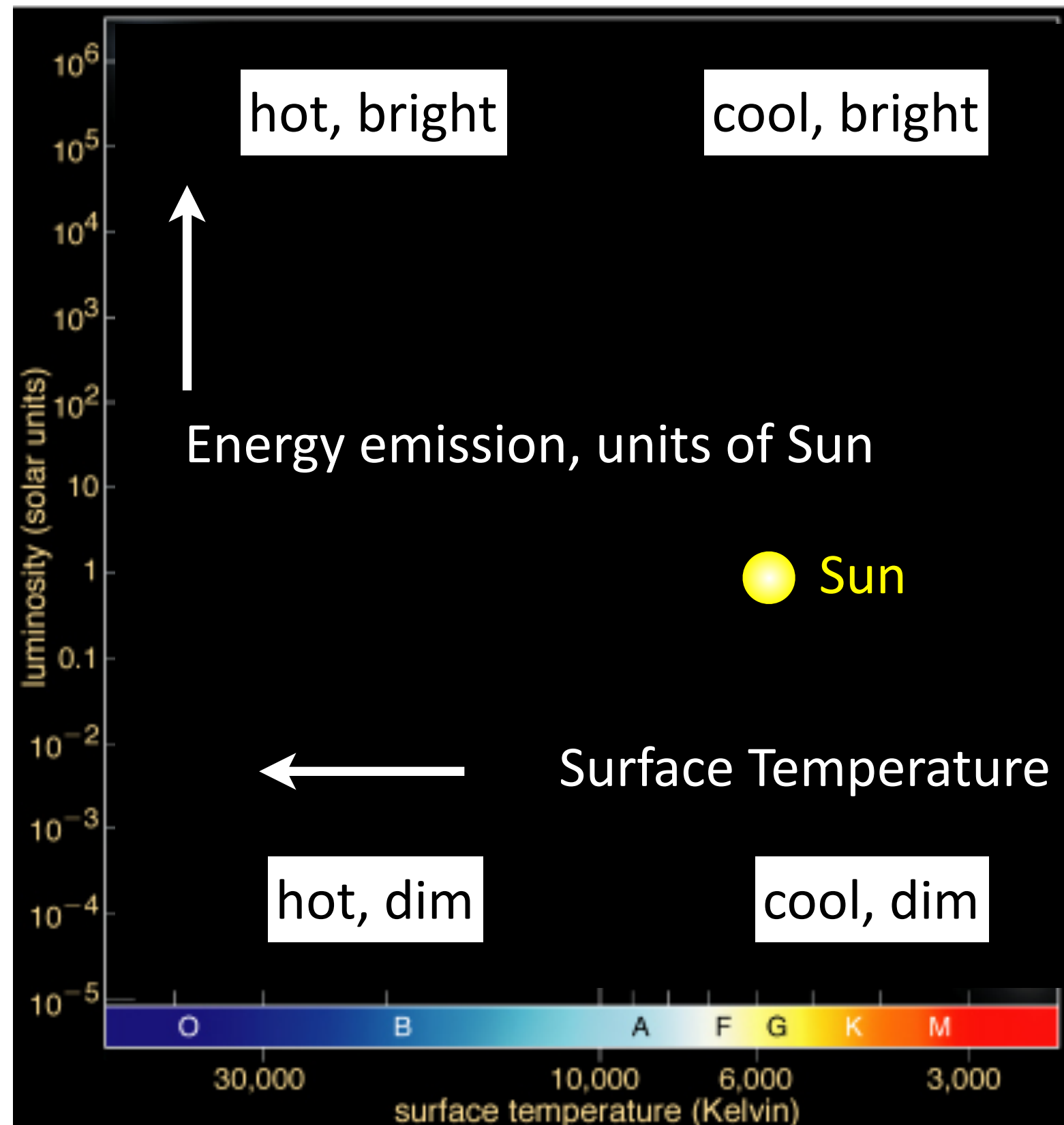
Einstein calculated that the
normal formation of a star of
gravitational accretion could never
form in so small a volume...and
stars get bigger not smaller, right?



1939: Robert Oppenheimer &
Hartland Snyder showed how.

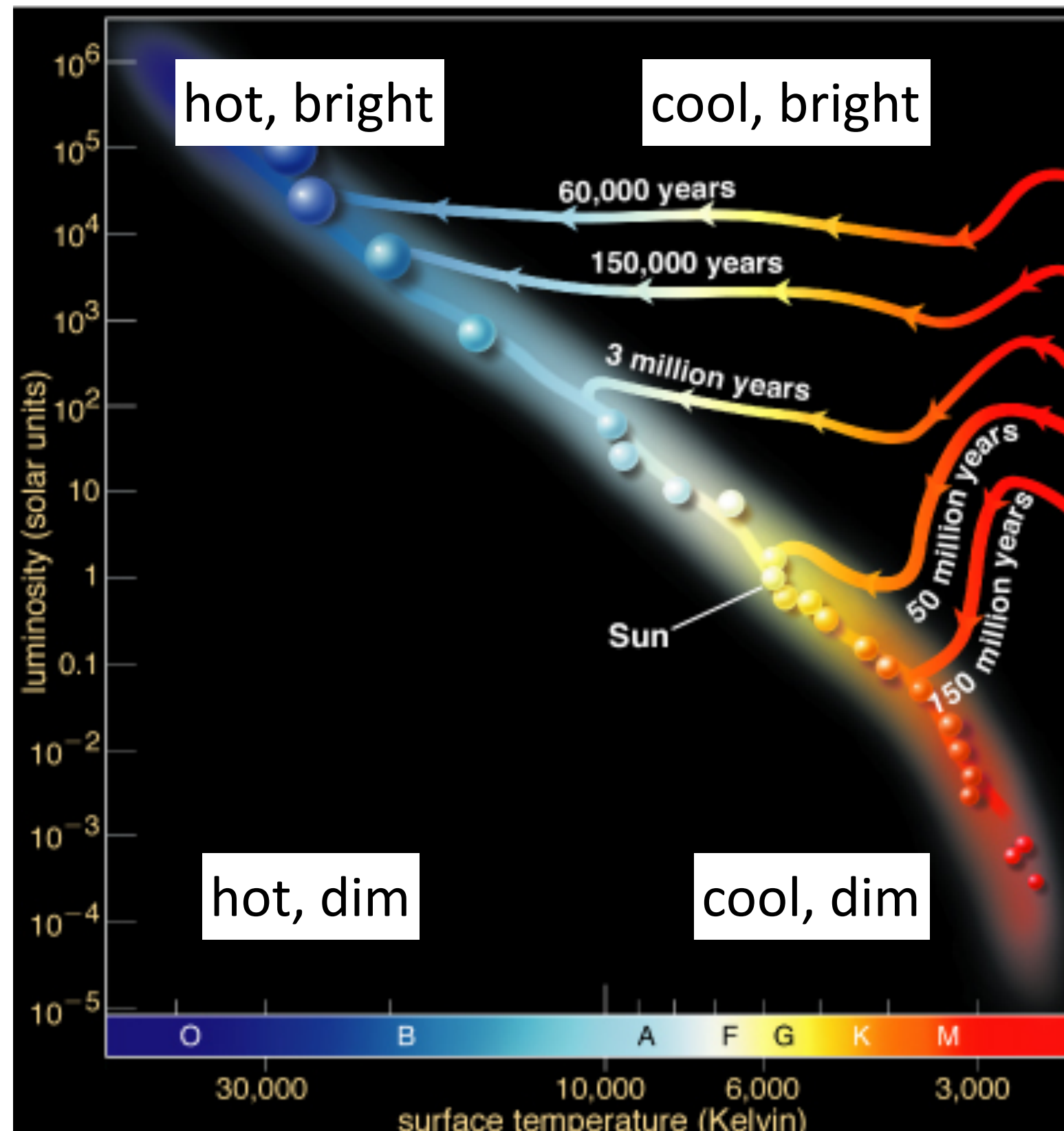
5¢ worth
of
stellar
physics
no charge

Hertzprung-Russell Diagram...aka H-R Diagram



5¢ worth
of
stellar
physics
no charge

Hertzprung-Russell Diagram...aka H-R Diagram



balls of
Hydrogen
brought
together by
gravity

The "main"
sequence

stars radiate energy – that's their job!

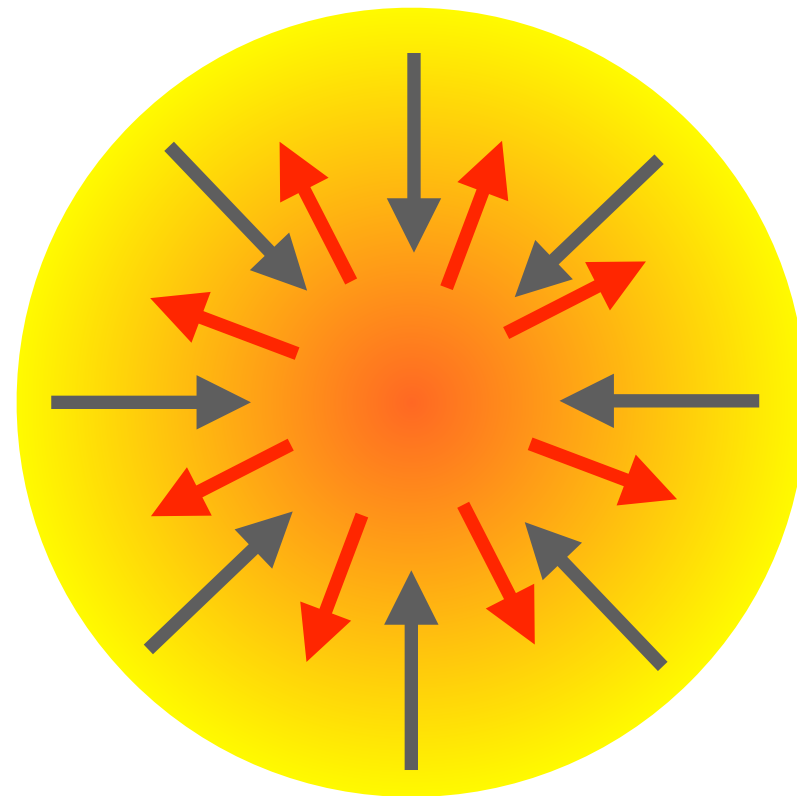
being stable is their challenge...

a balancing act

inward pressure
from gravity

vs

outward pressure
from radiation



gravity pulls core/atmosphere: **in**

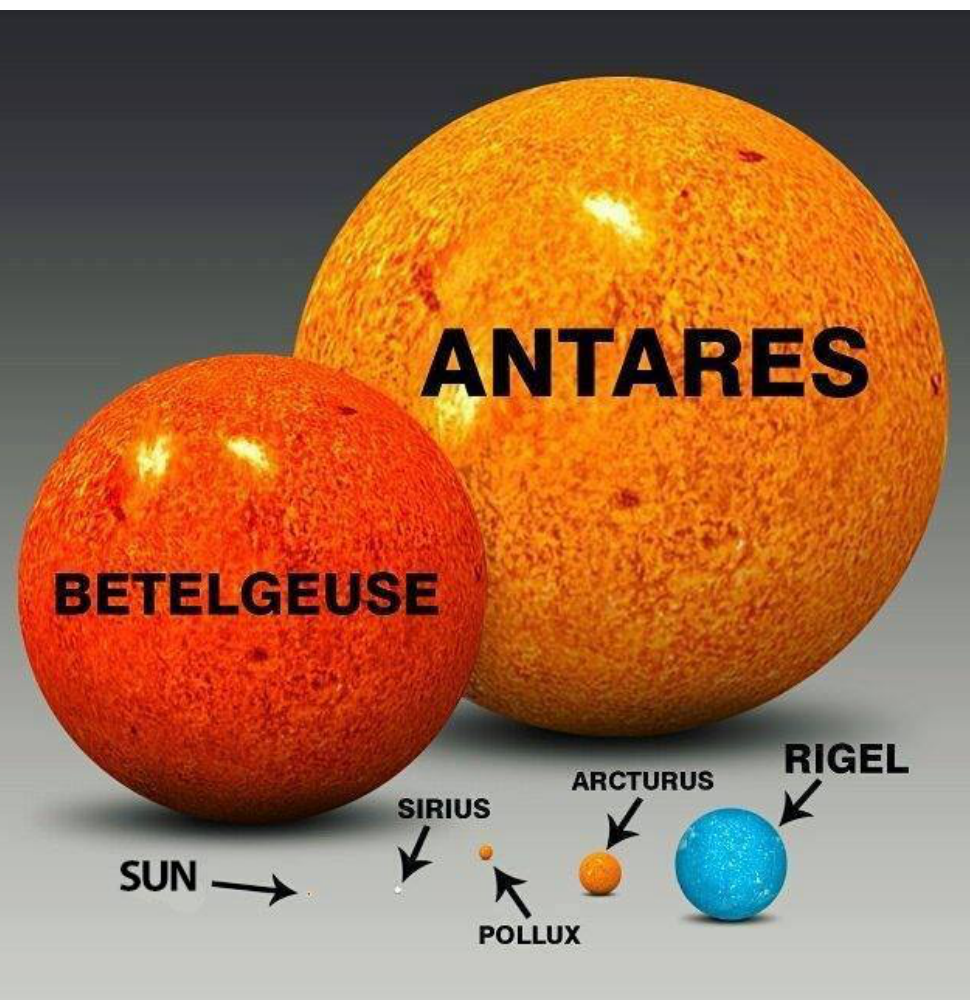
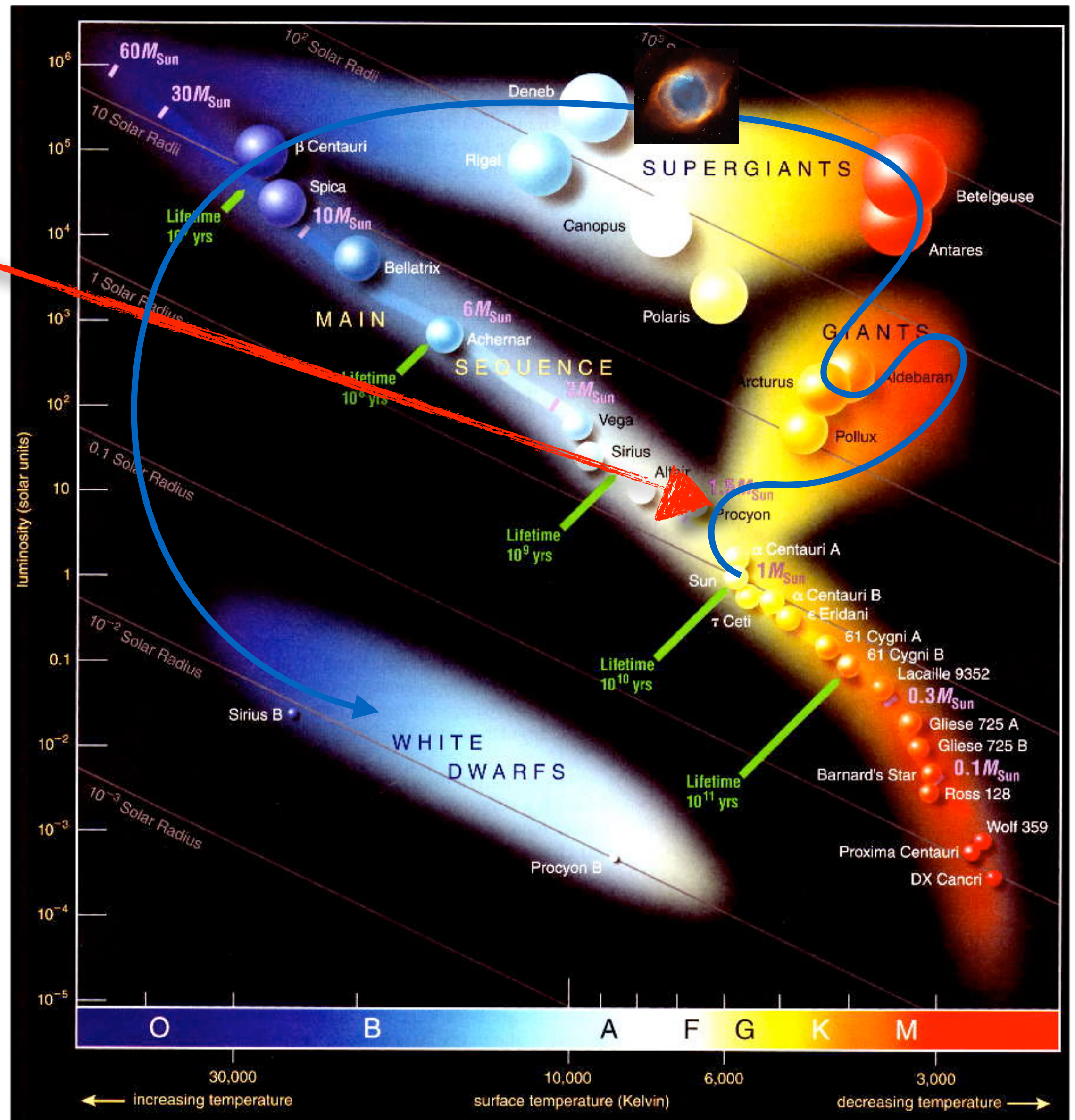
Radiation pressure from nuclear
fusion in core: **out**

H begins to “burn” to He

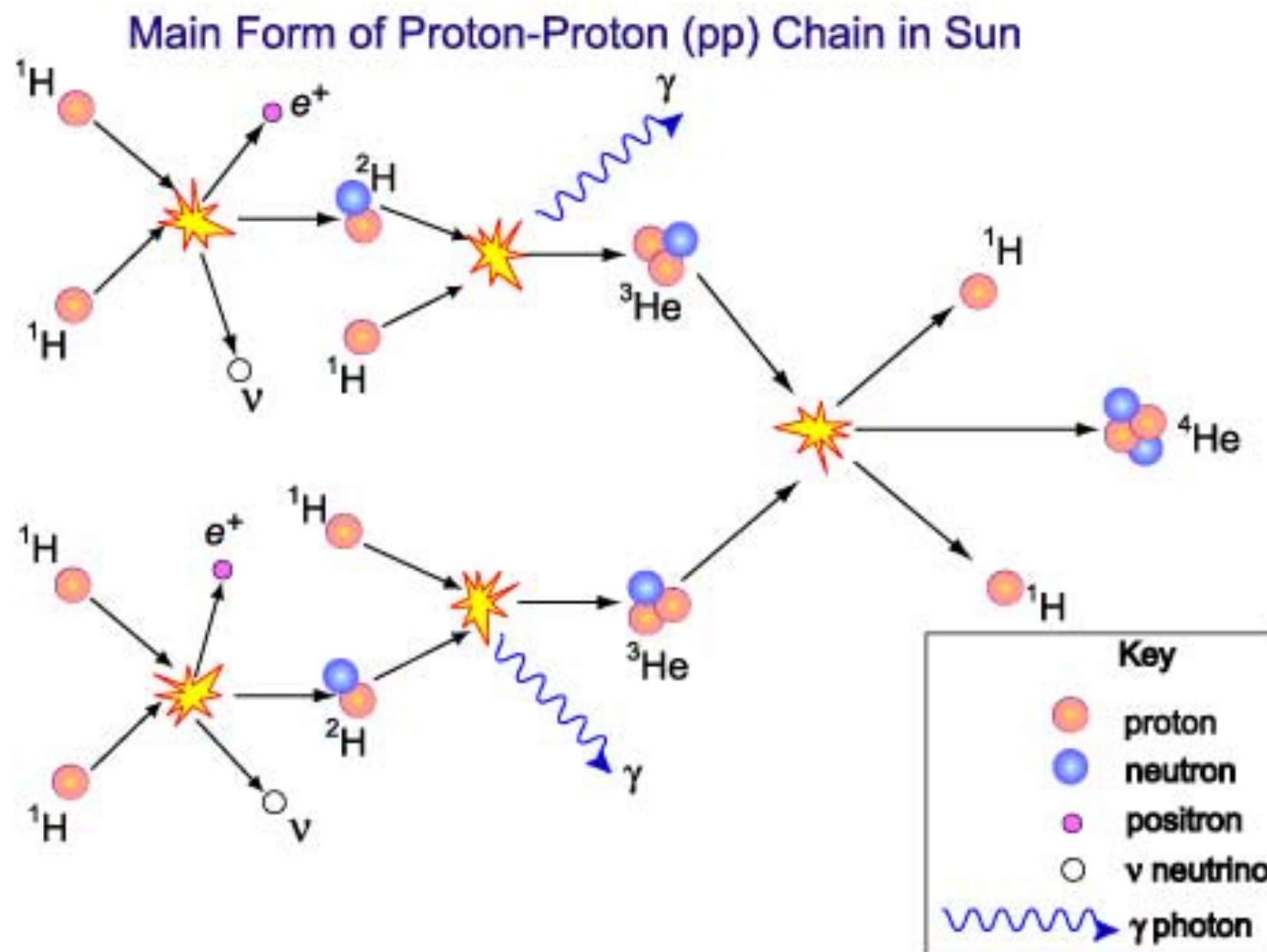
A star’s fate is determined by how massive it is.

a balancing
act

SUN-LIKE?
 $H \rightarrow He$



pp cycle



a balancing act

SUN-LIKE?

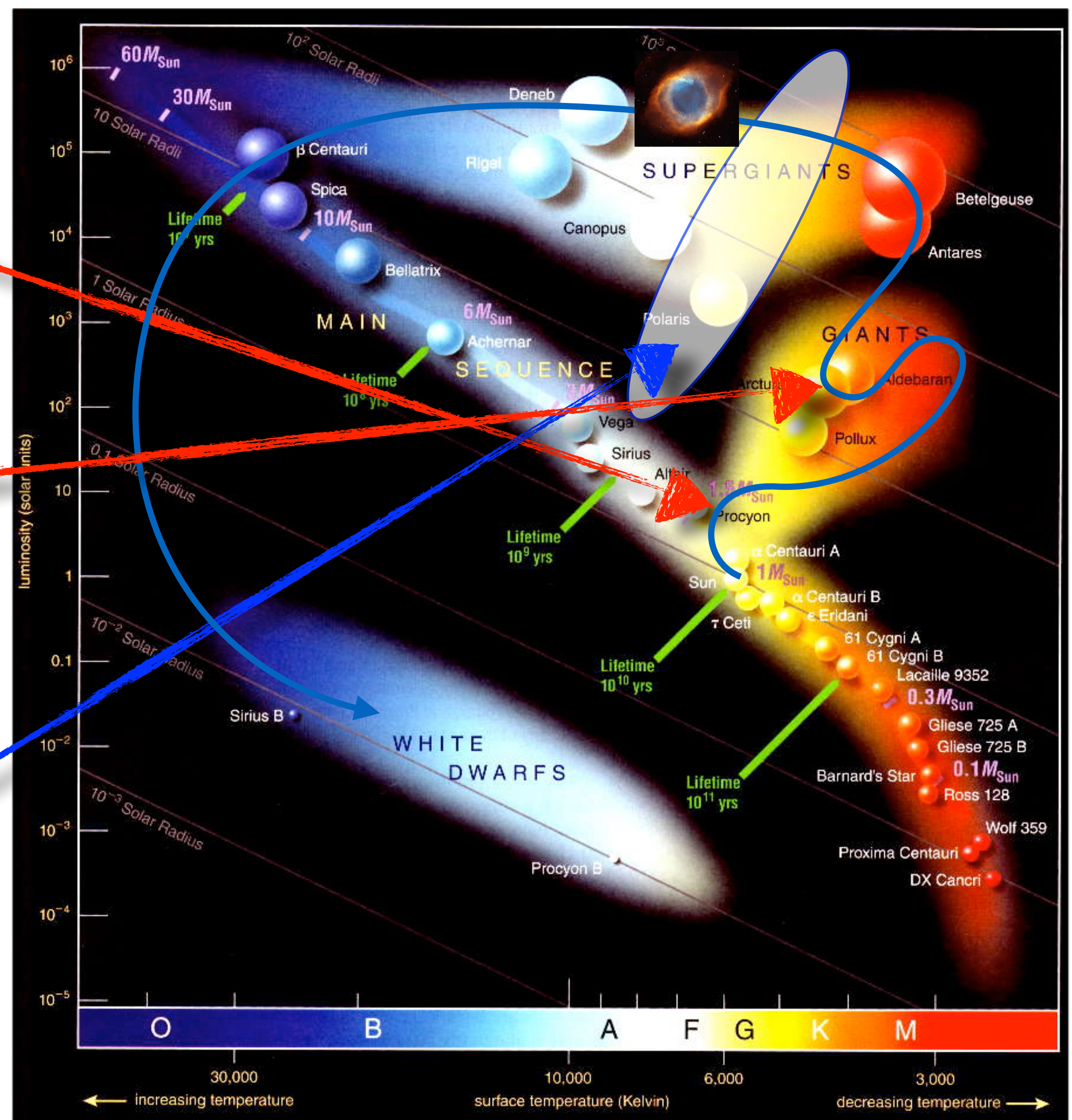
$$H \rightarrow He$$

SUN-LIKE?

$$\text{He} \rightarrow \text{C} + \text{O}$$

source of Carbon for life

REGION OF
INSTABILITY
pulsating stars



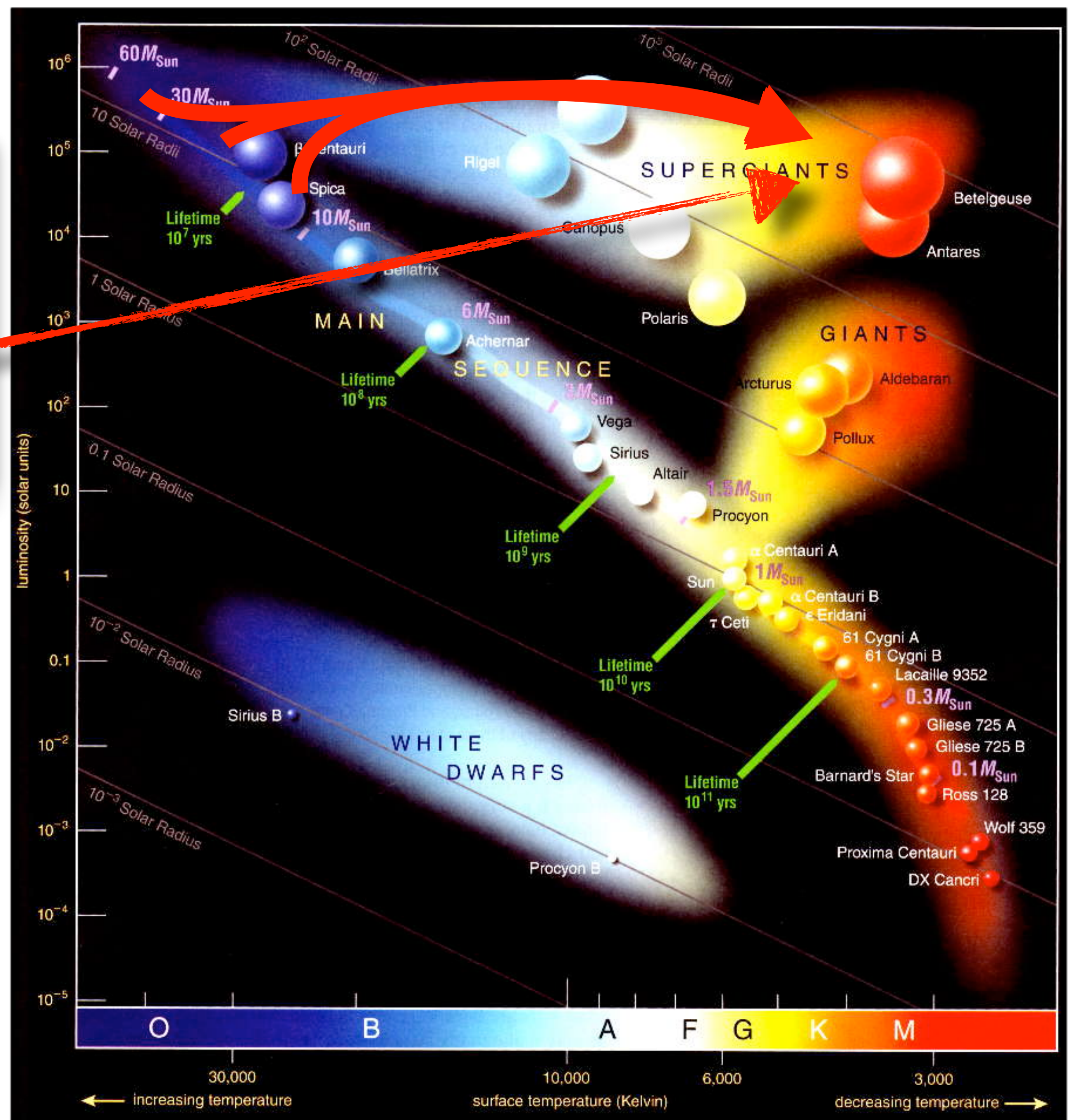
a balancing
act

VERY MASSIVE...

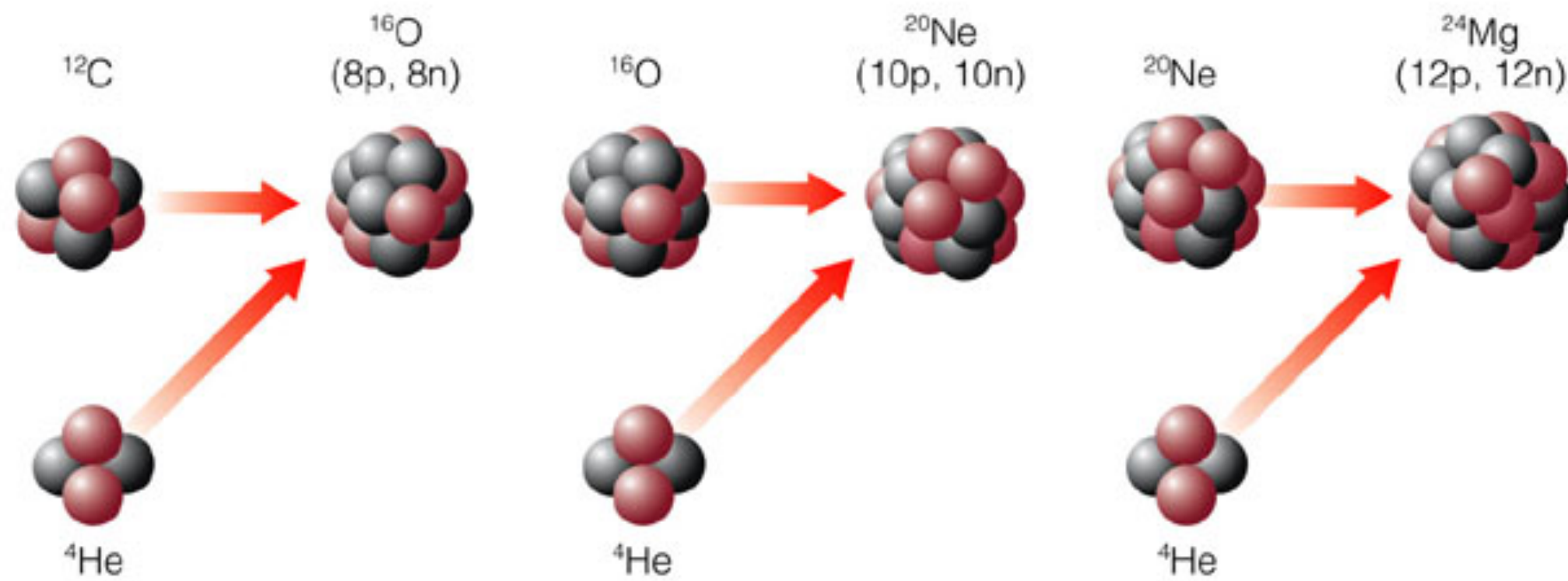
$>1.3 M_{\text{Sun}}$

$\text{H} \rightarrow \text{He} \rightarrow \text{C} \dots$

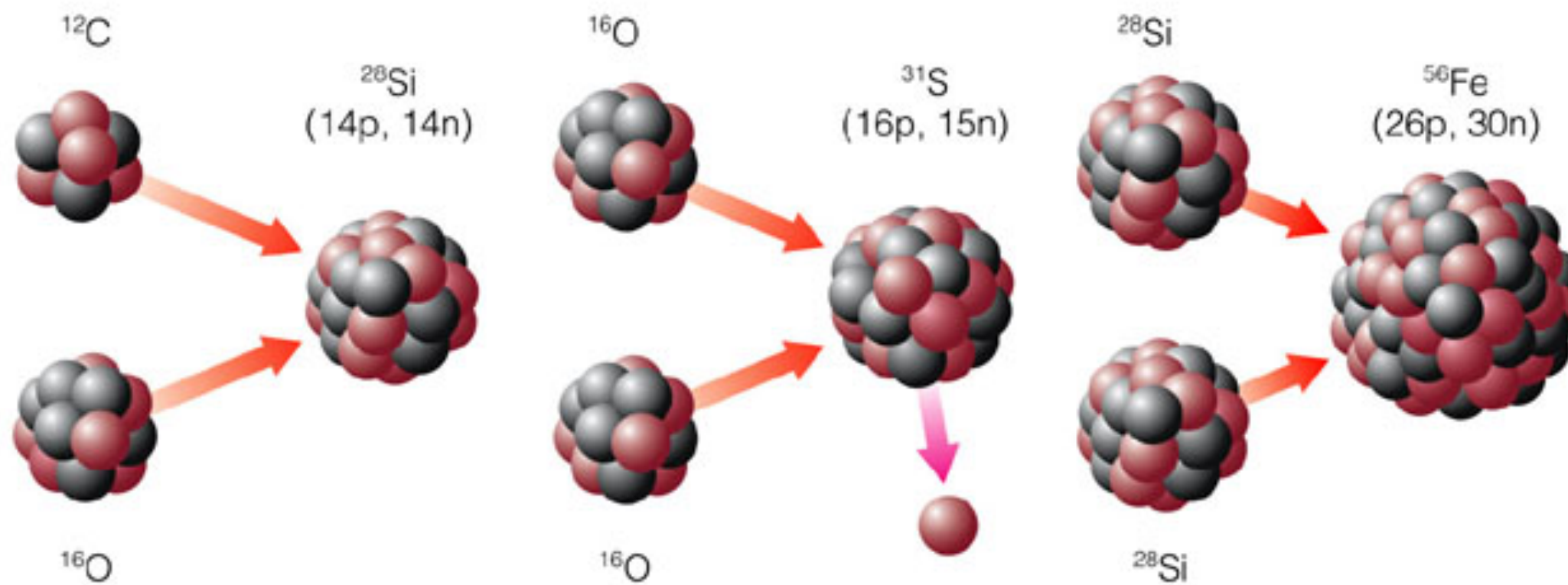
$\dots \rightarrow \text{Fe}$



Helium-capture reactions



Other reactions



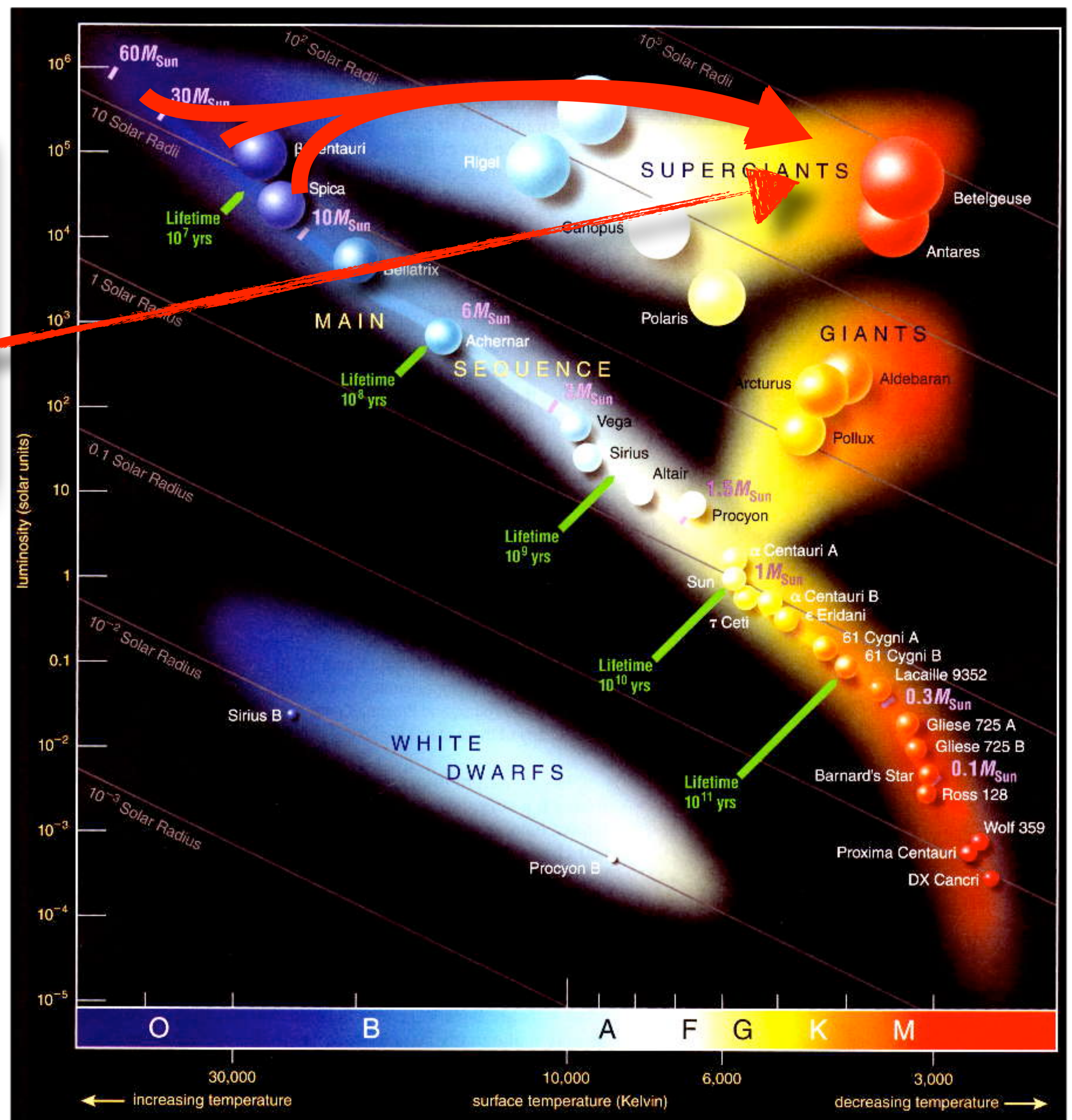
a balancing
act

VERY MASSIVE...

$>1.3 M_{\text{Sun}}$

$\text{H} \rightarrow \text{He} \rightarrow \text{C} \dots$

$\dots \rightarrow \text{Fe}$

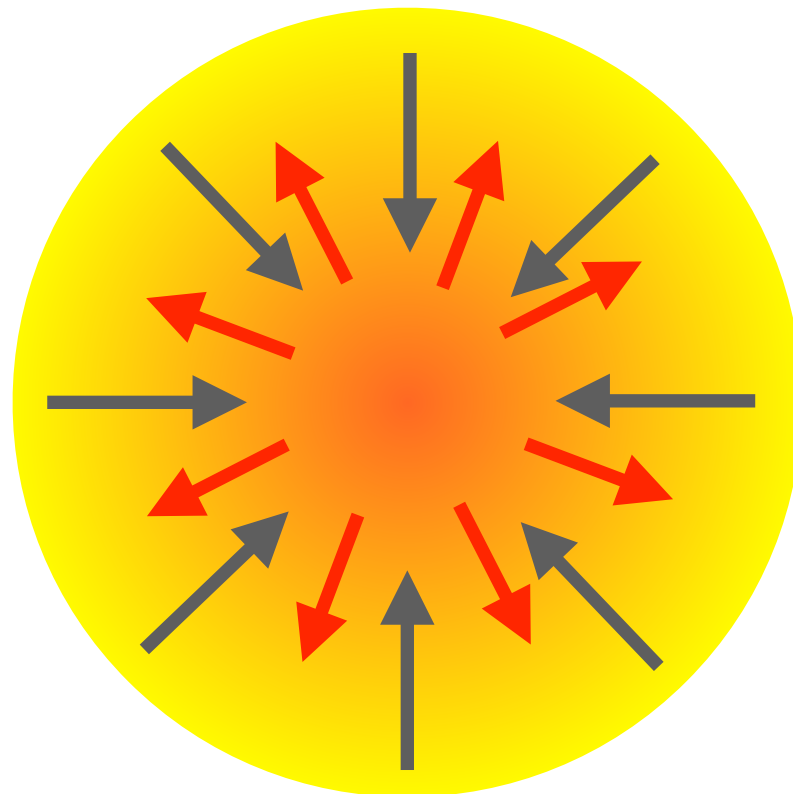


a balancing act

inward pressure
from gravity

vs

outward pressure
from radiation



gravity pulls core/atmosphere: **in**
WINS

Radiation pressure from nuclear
fusion in core: **out**
STOPS

$e + p \rightarrow n + \nu_e$ everywhere...
the star shrinks dramatically



and then a
special effect
takes over:

neutrons cannot all be on top
of one-another

It stops abruptly in seconds

Explosively.

supernova!

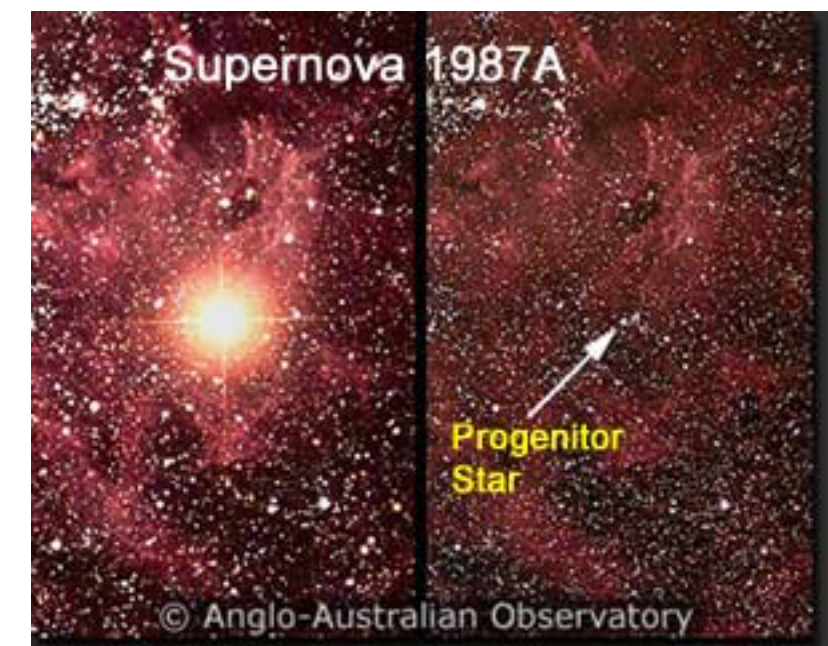
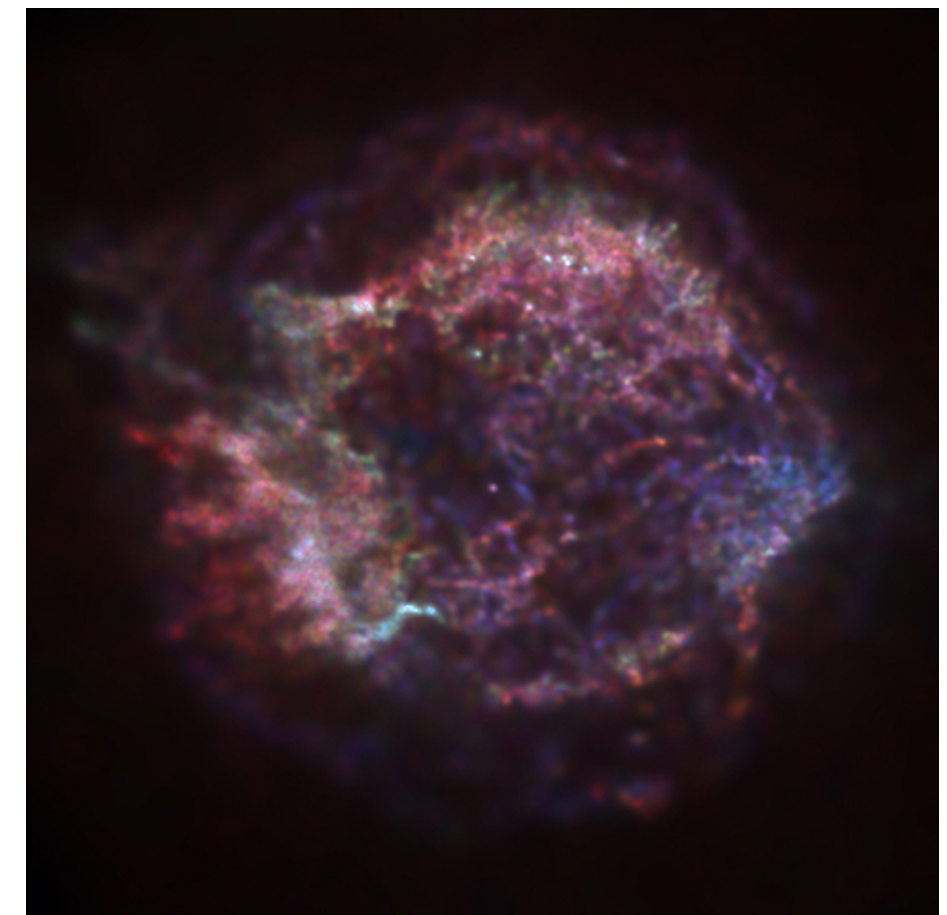


SN 1993J
M81



Crab Nebula...supernova
remnant from 1054 AD

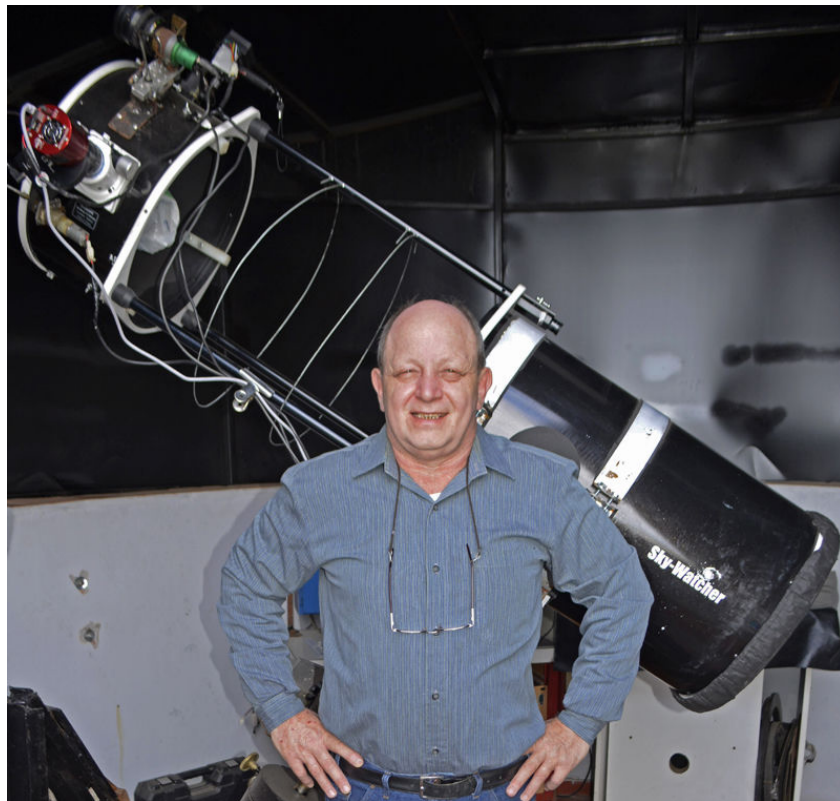
Tycho's
Supernova,
1572



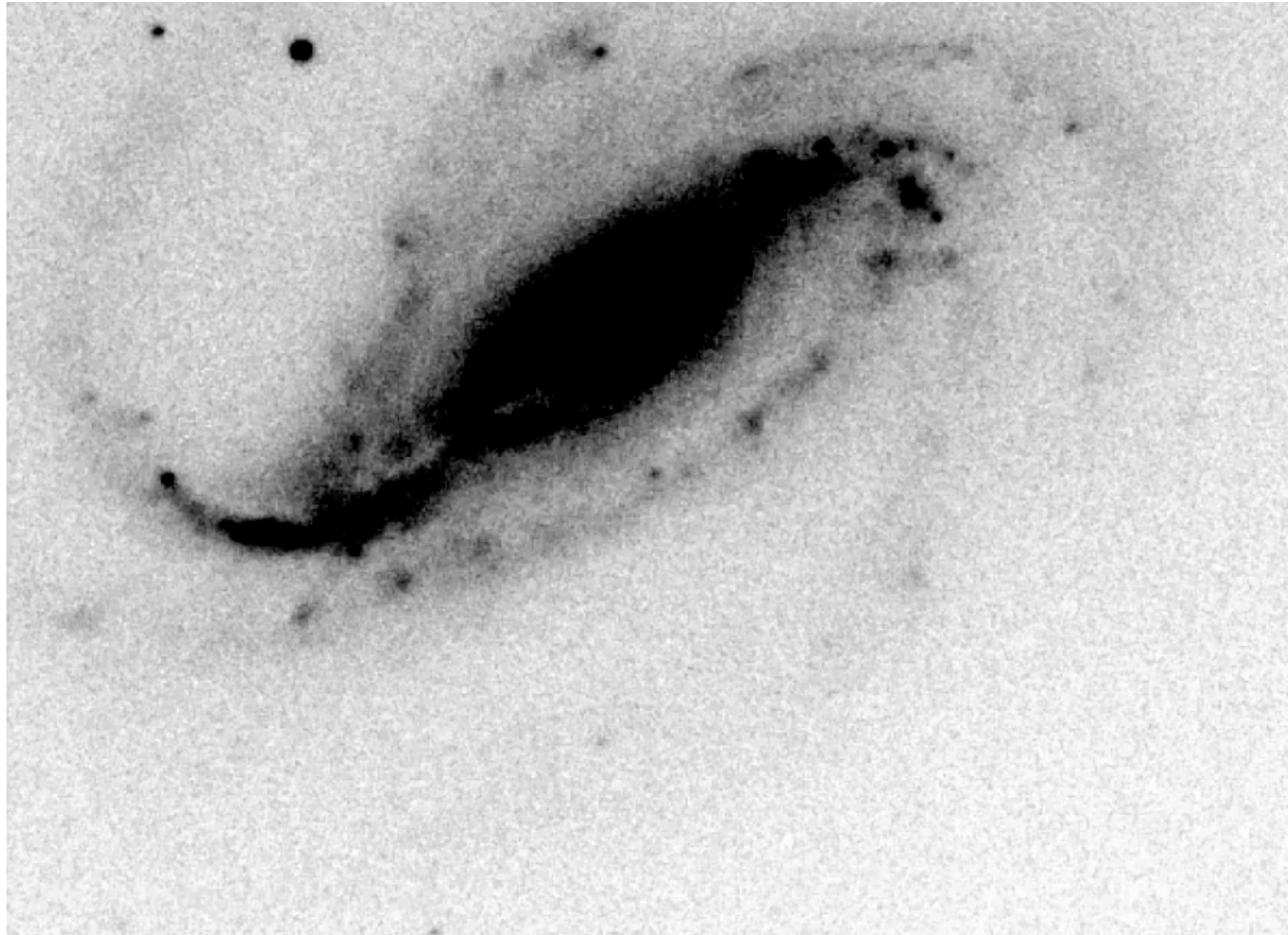
first infant picture of SN

20 September
2016

Victor Buso:

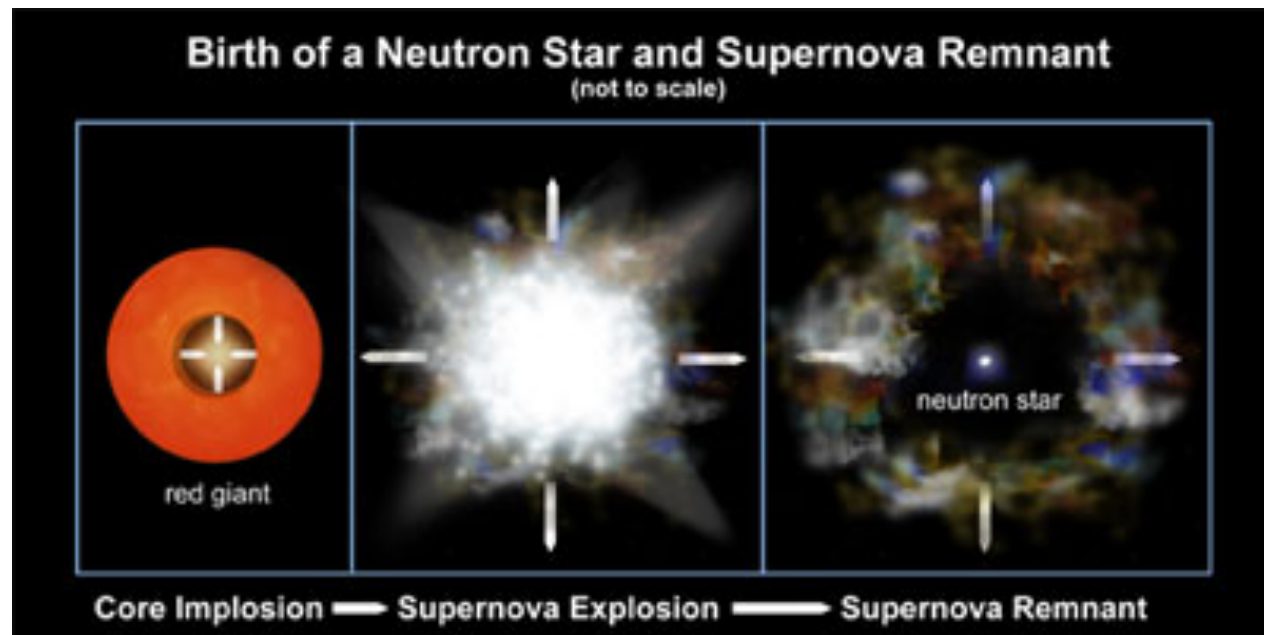


NGC 613
65M ly away

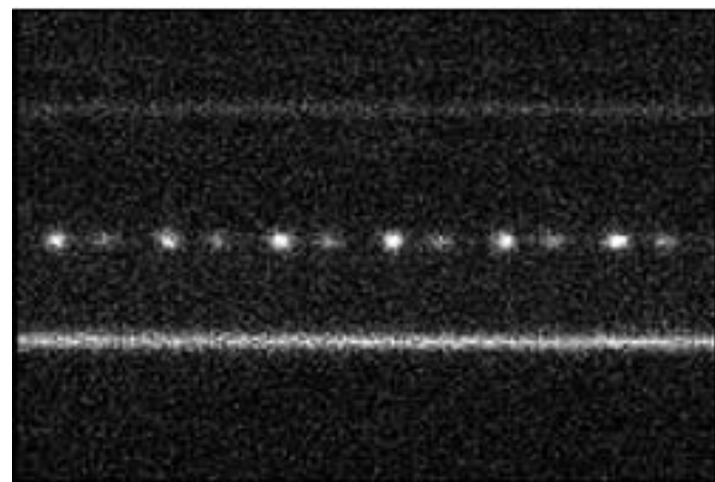


aftermath of a SN

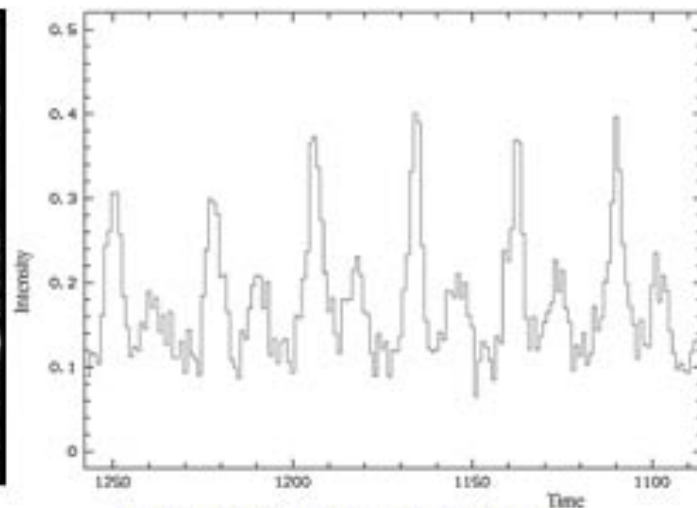
mass-ejection and a neutron star



a star made of only neutrons...sizes 10's km
densities 10^{17} kg/m³

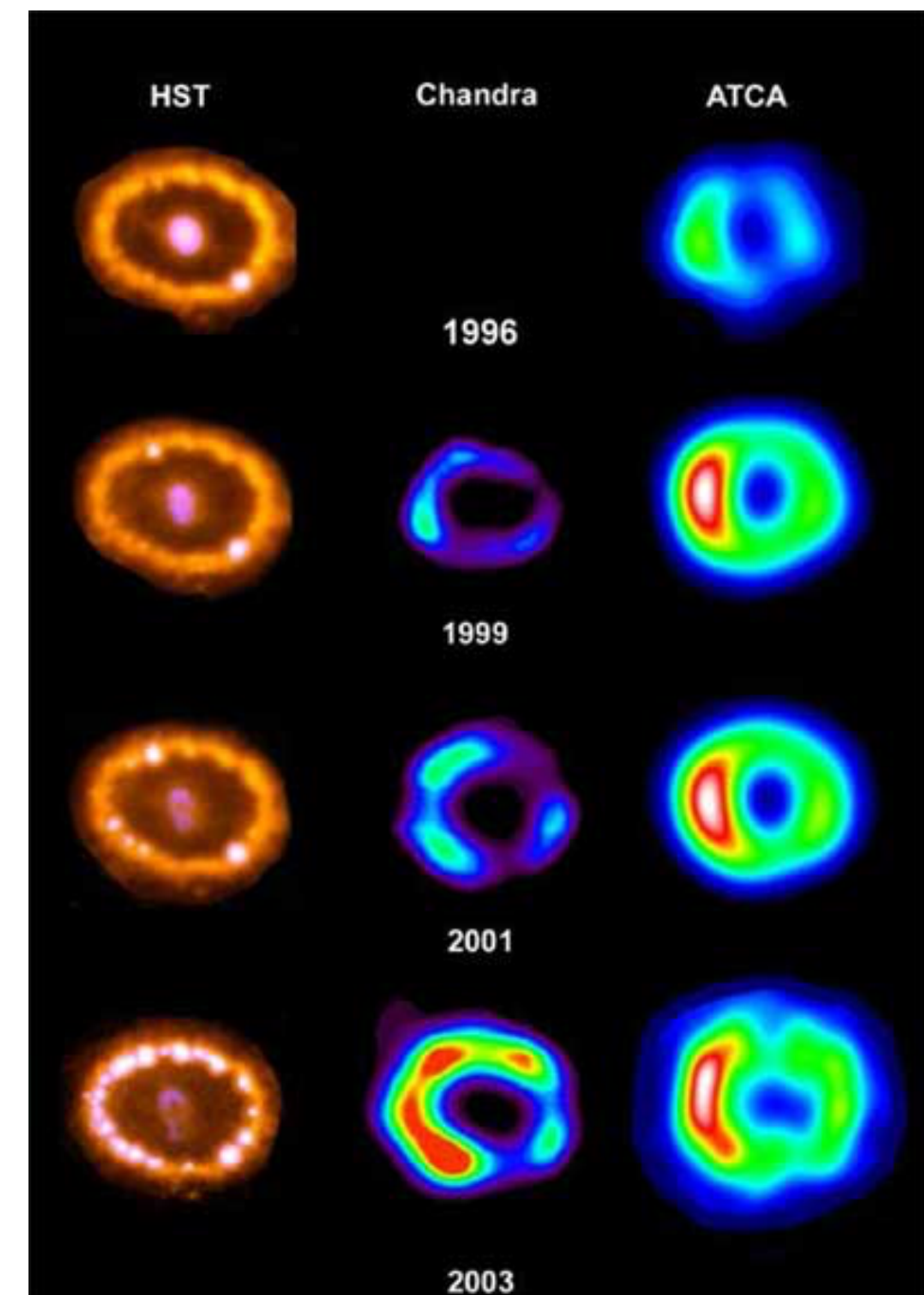


Time Sequence of Crab Pulsar



Light Curve of Crab Pulsar

(VLT KUEYEN + FORS2 + FIERA) © ESO

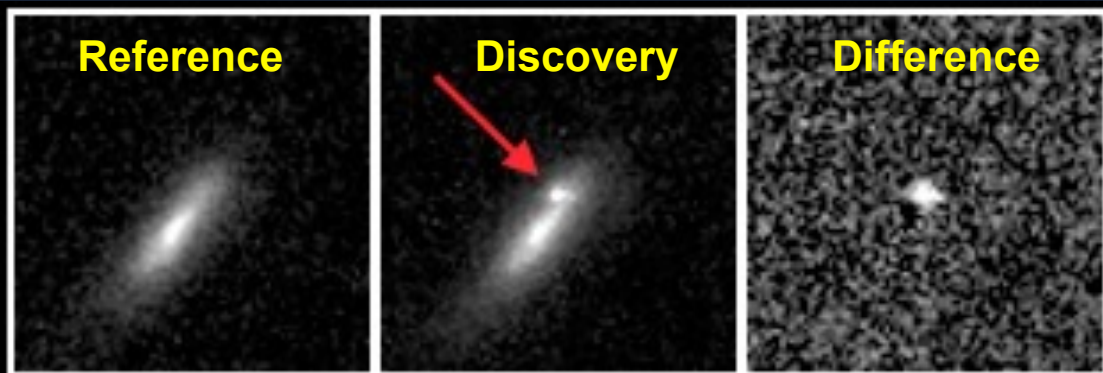


“pulsar”...a rapidly rotating neutron star: few milliseconds to seconds in rotation rate

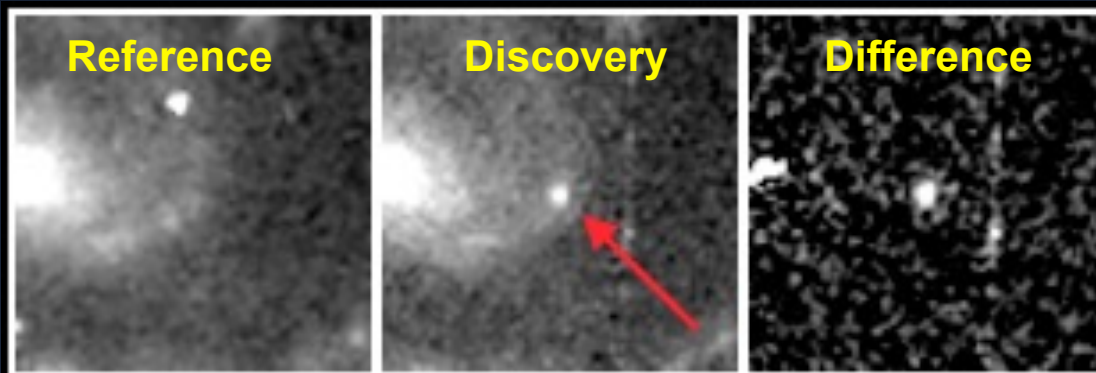
The source of all elements < Fe. We are made of star-stuff

Cluster Lensing And Supernova survey (CLASH) SN Candidates in 25 Clusters (Of the 30, ~30% are Type Ia)

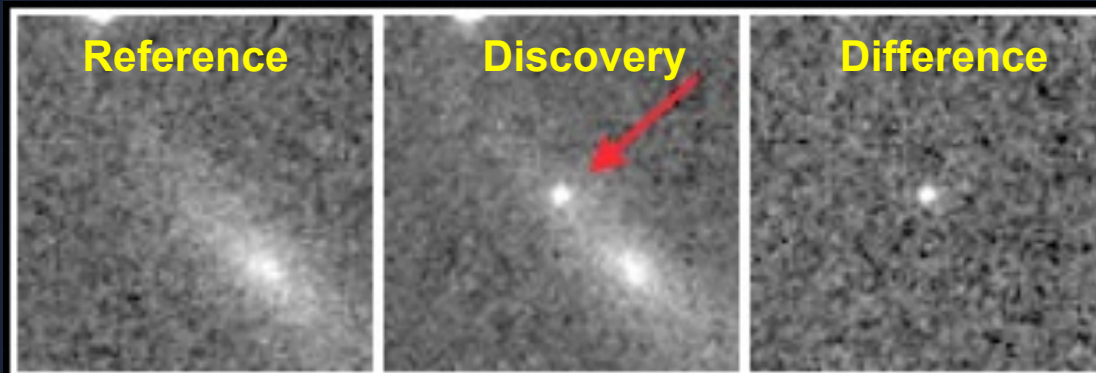
SN "Augustus"



SN "Galba"



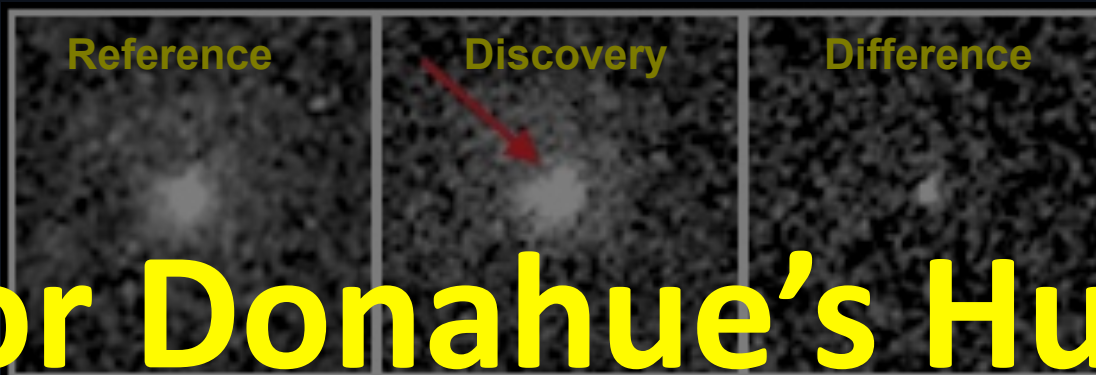
SN "Antonius Pius"



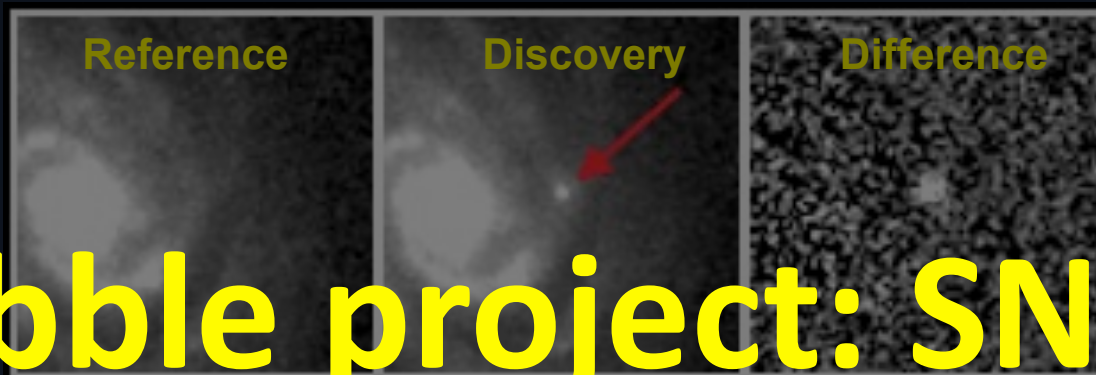
SN "Tiberius"



SN "Otho"



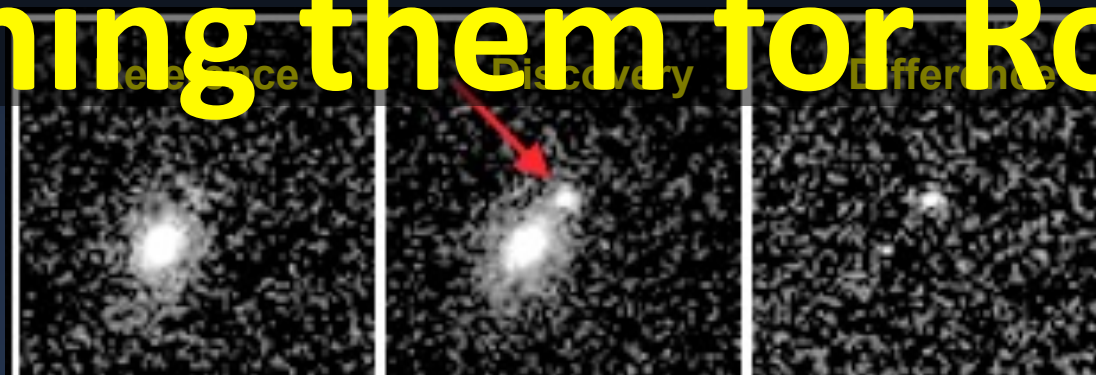
SN "Marcus Aurelius"



SN "Caligula"



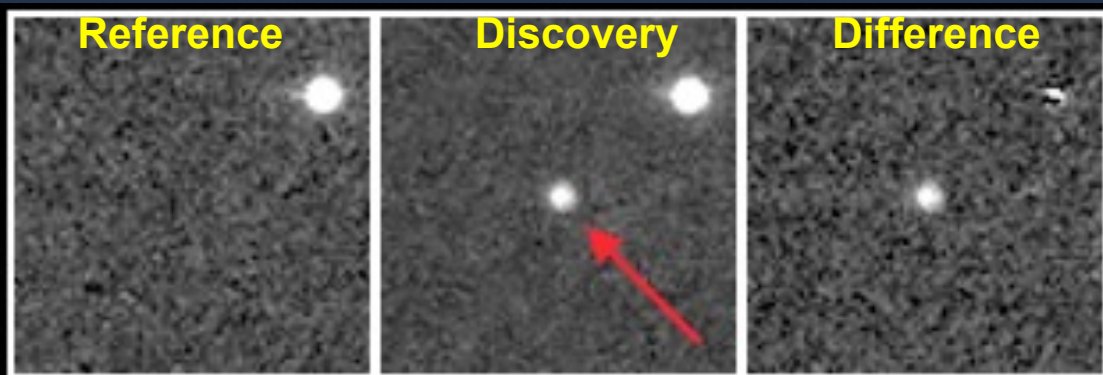
SN "Vespasian"



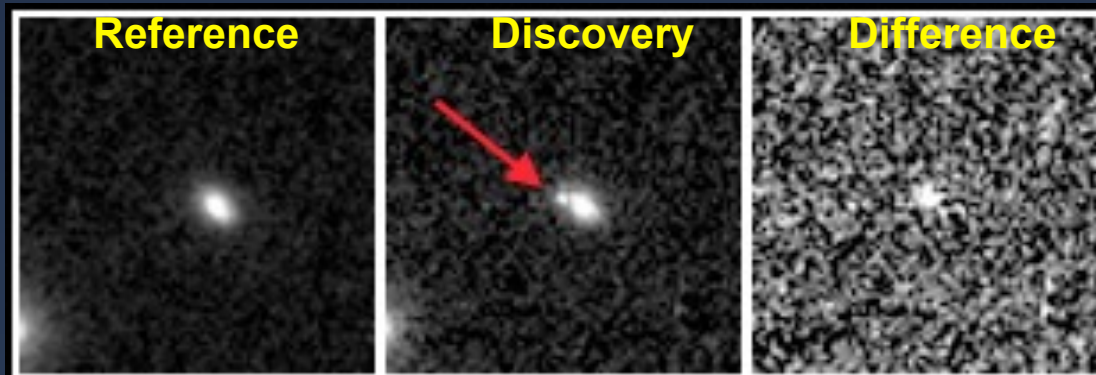
SN "Scarlet"



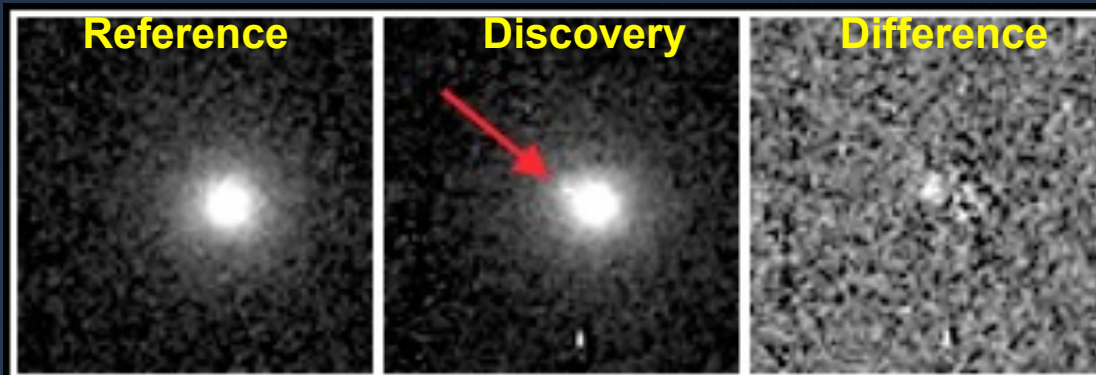
SN "Claudius"



SN "Titus"



SN "Crimson"



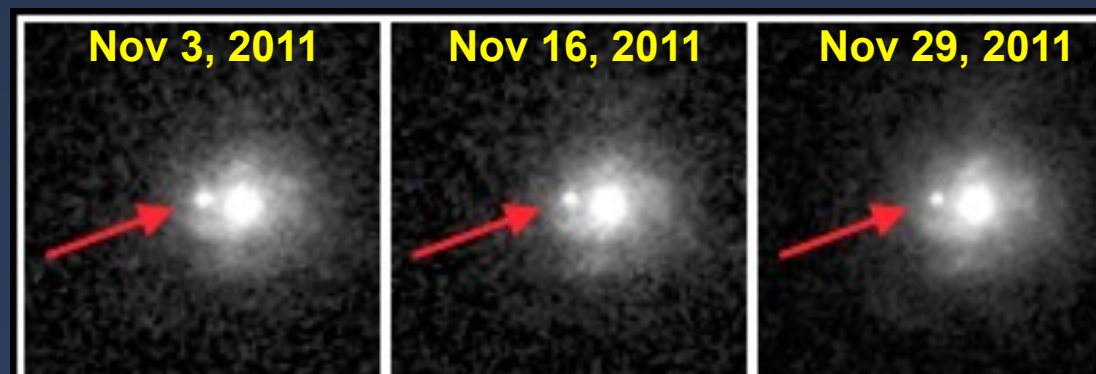
SN "Nero"



SN "Hadrian"



SN "Burgundy"



One of Professor Donahue's Hubble project: SN searches - naming them for Roman Emperors

what if $M > 3-15 \times M_{\text{sun}}$?

Nature turns viscous

very peculiar

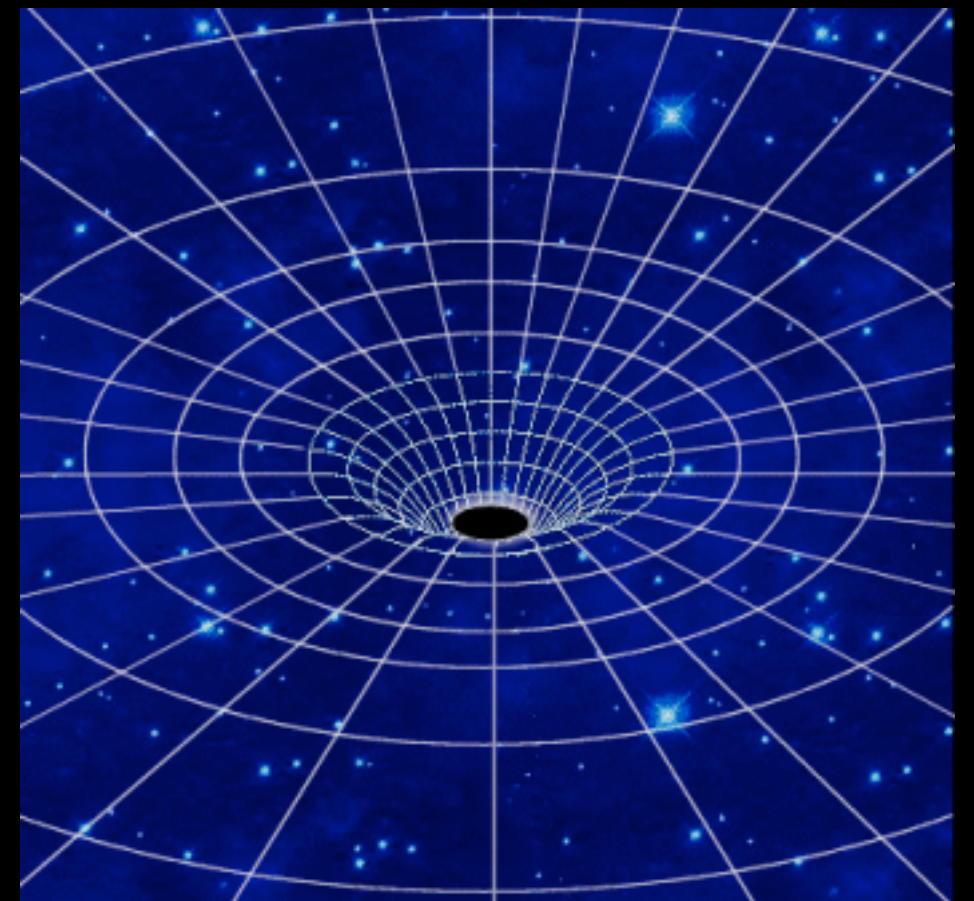
**Gravity wins. Nothing gets
out, not even light:**

BLACK

no light

HOLE

the most extreme
warping of
spacetime in
Nature

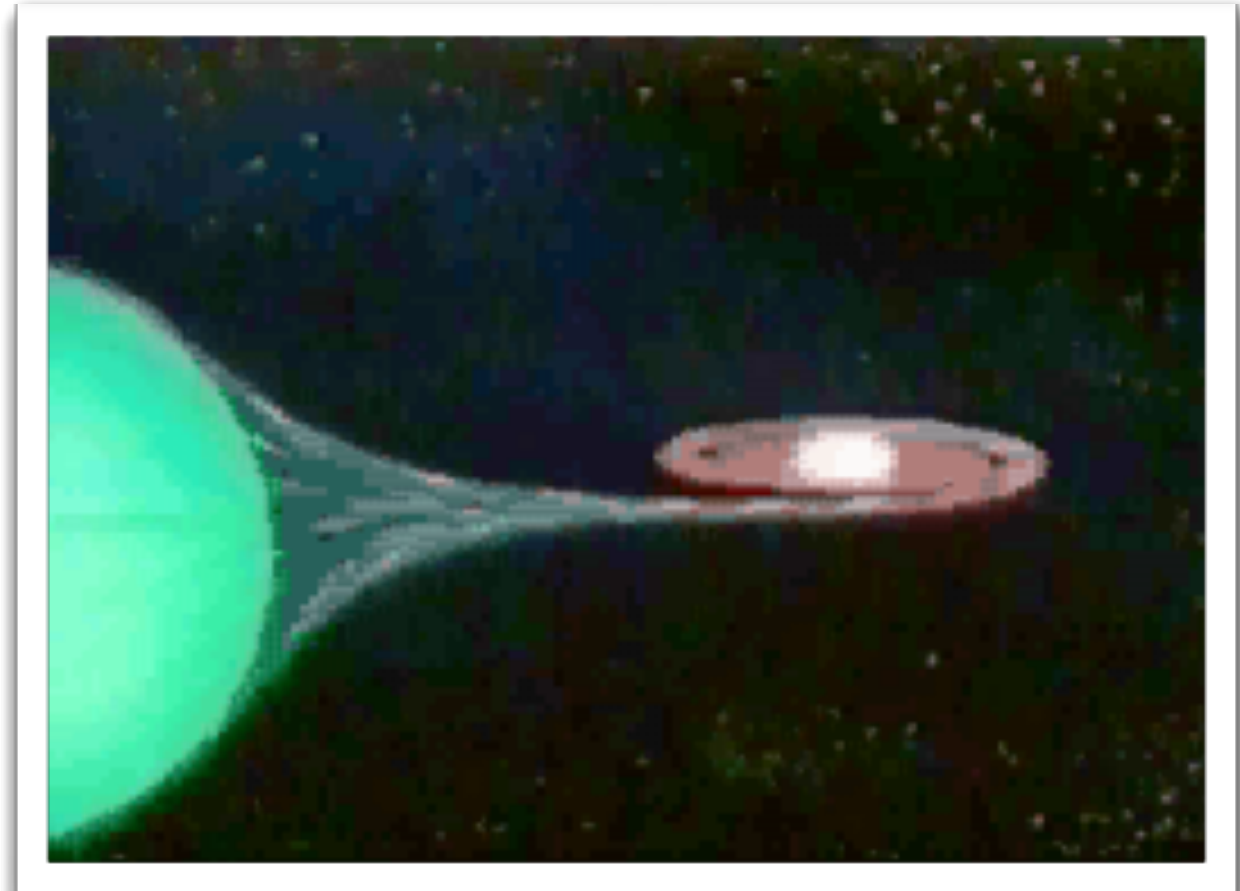


outside
of $\sim 3R_s$

a black hole
behaves like a
normal object
with Newtonian-
like gravity

So, how are they found?

Because they're hungry.



the matter sucked in accelerates...
and accelerating charges do what?

Radiate...**X-Ray, radio frequencies** typically

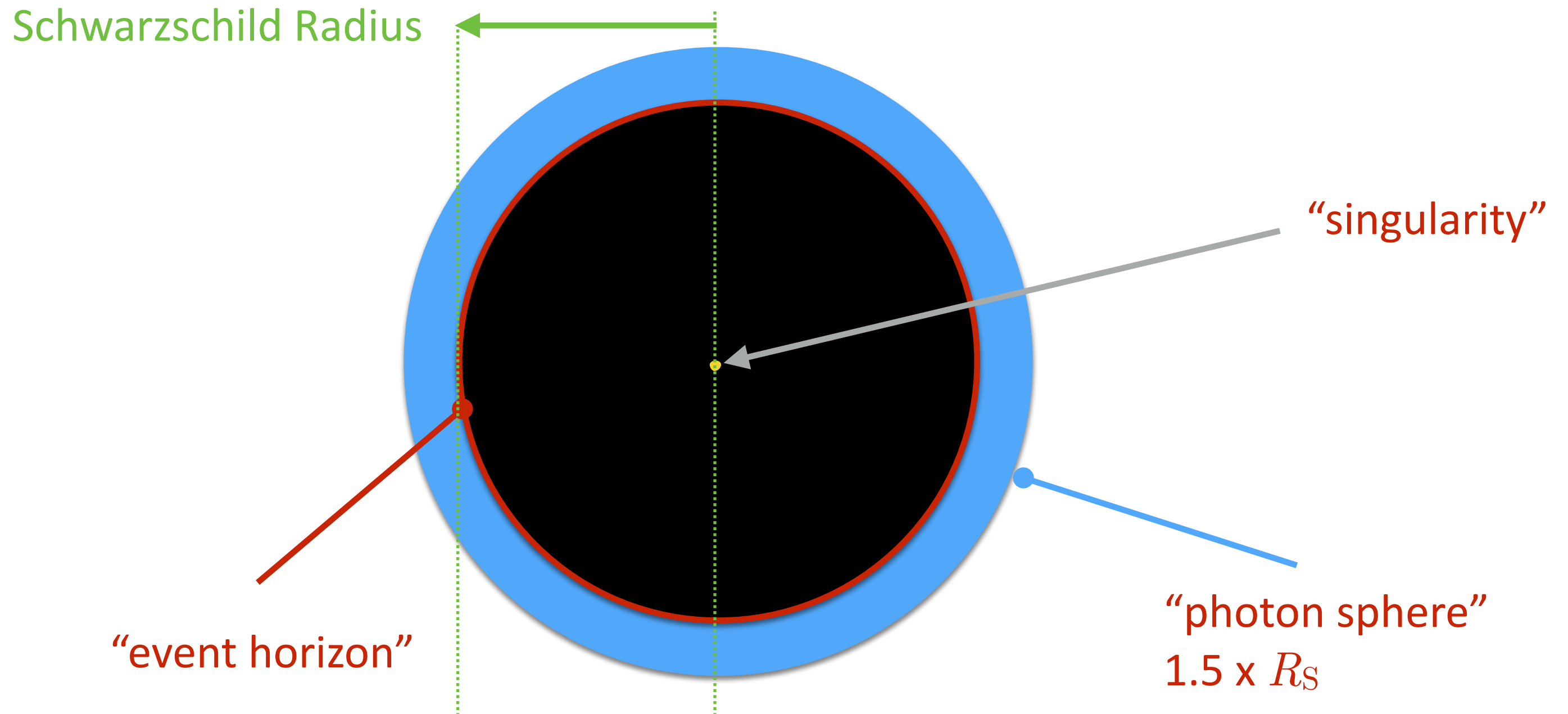
Three kinds:

1. **Stellar black holes** - 100's found with Hubble
2. **Supermassive black holes** - seems that all galaxies have one: billion's of stars' worth
3. **miniature black holes.** - complete speculation, a gleam in some theorists' eyes

Stellar Black Holes

many stars' fate

black hole anatomy



simplest black hole: not rotating and not charged

realistic black hole: rotating...Kerr Black Holes

often in binary systems

with characteristic X-ray emission

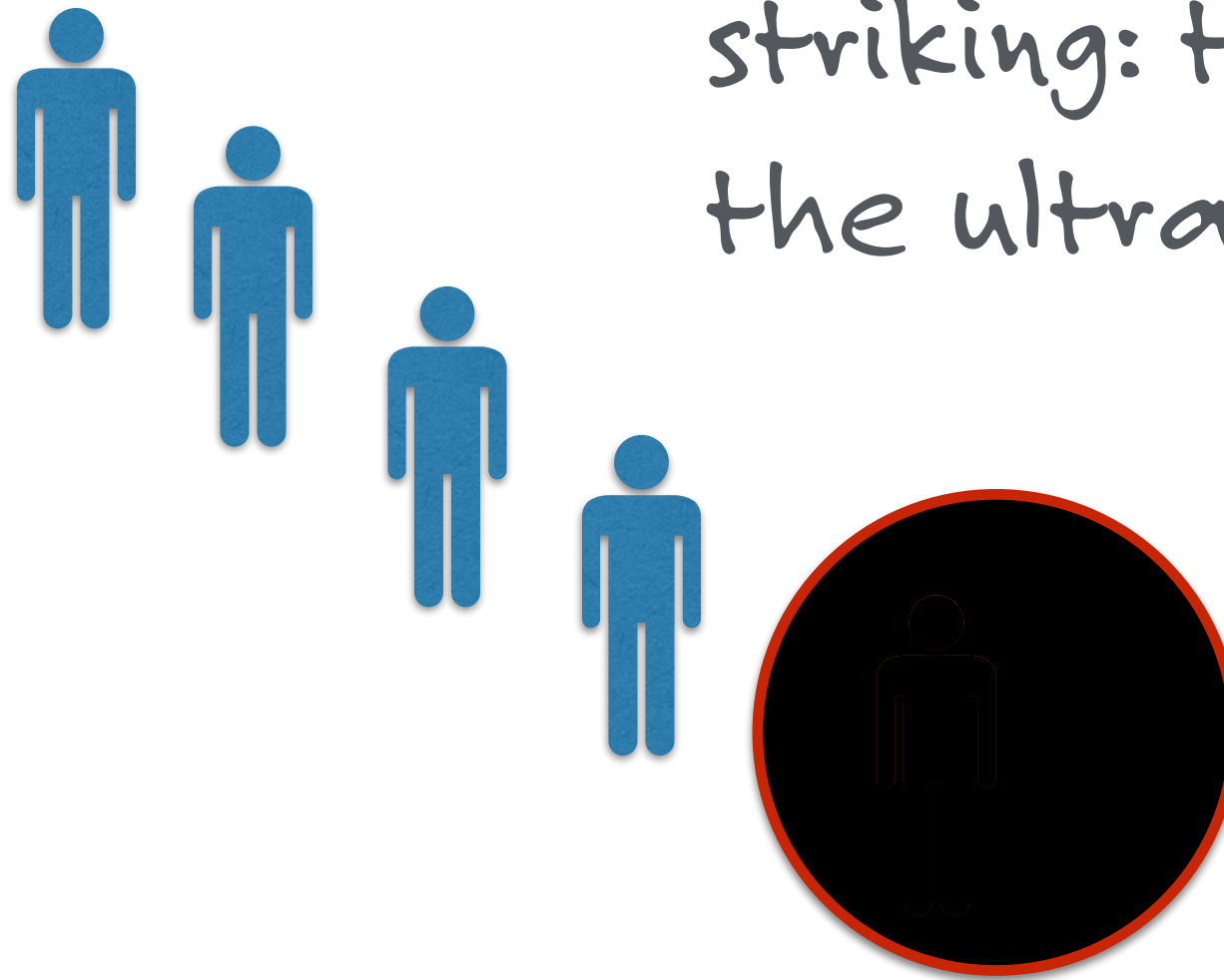
Cygnus X-1/HDE 226868 1972



what if
you fell
in?

everyone asks
this!

from the outside:



striking: time slows near
the ultra strong gravity

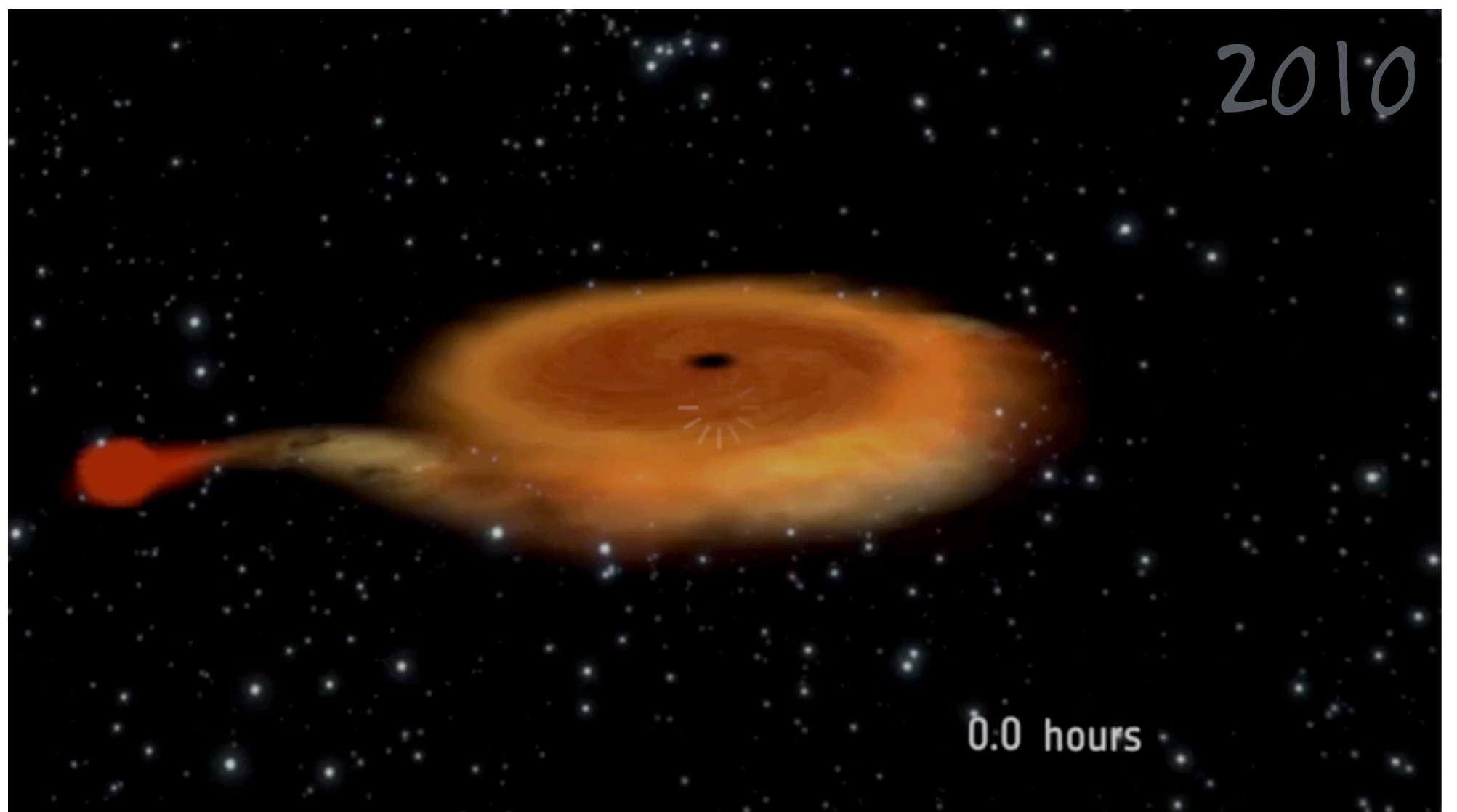
from the inside:



also, atomic spaghetti

black
holes are
in the
news

and on the silver
screen



Watch in: 

[Embed Code](#)

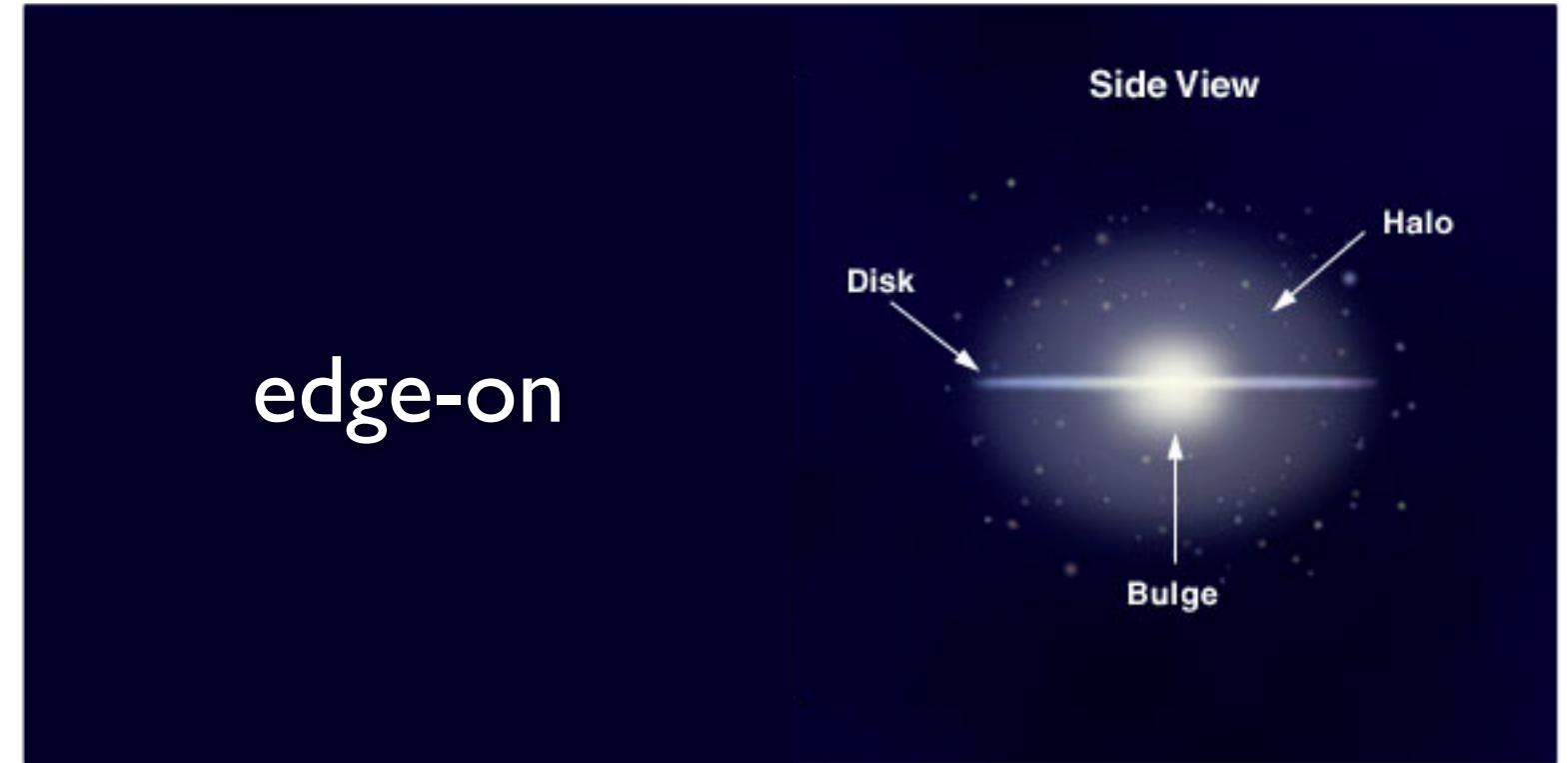


Supermassive

Black Holes

center of every (?) galaxy

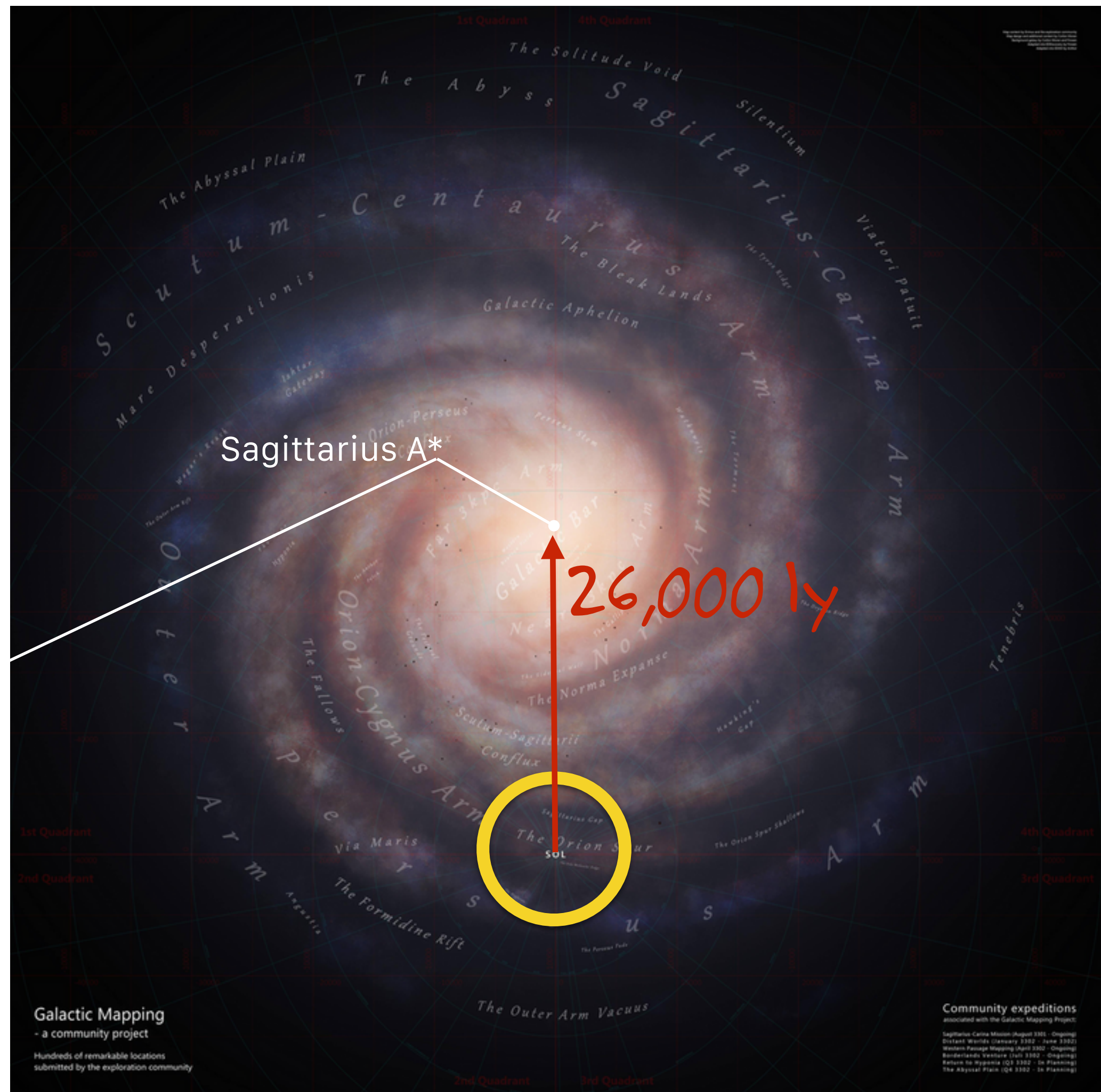
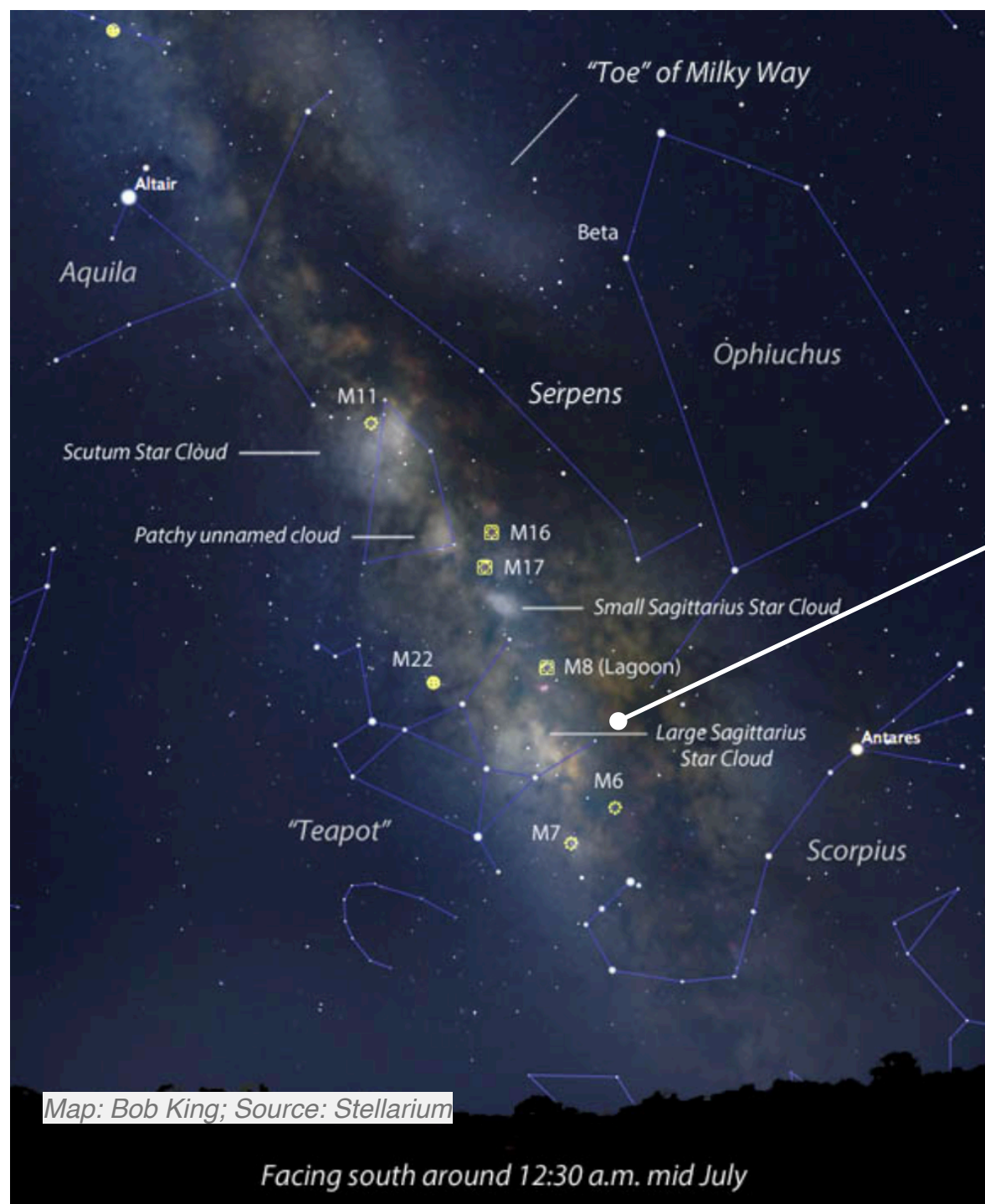
panorama view of the Milky Way from ESO



100,000ly-ish

Let's orient ourselves

Sagittarius A and A*



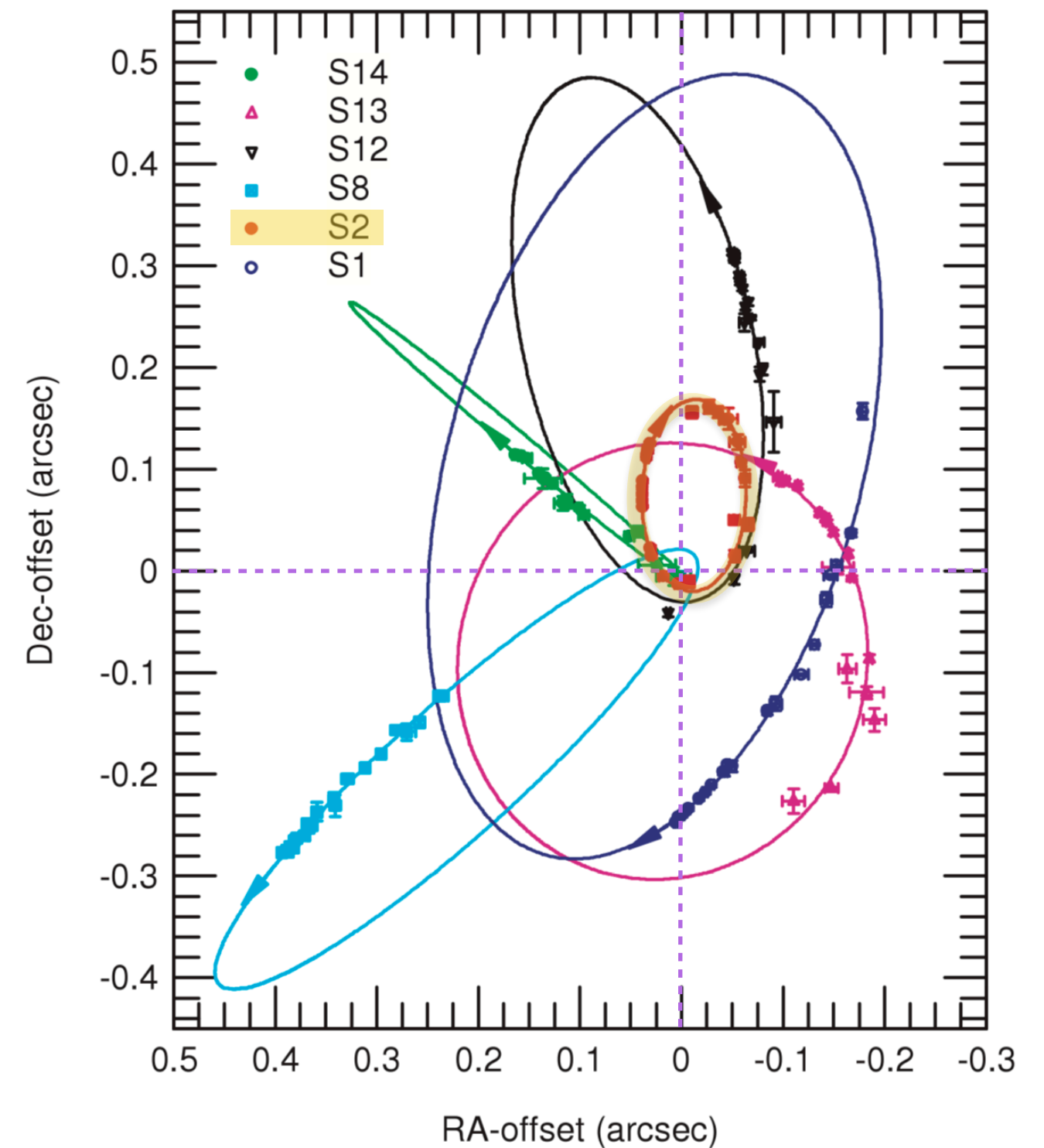
Milky Way in the news

enormous, central
black hole
confirmed



S2:

- has a period of 15 years and comes close - 17 light-hours - so center object is smaller than that
- orbit implies $M(\text{center}) = 4.1M$ solar masses



S14:

- comes closer - 6.25 light-hours - so center object is smaller than that!

Galactic black holes:

Milky Way

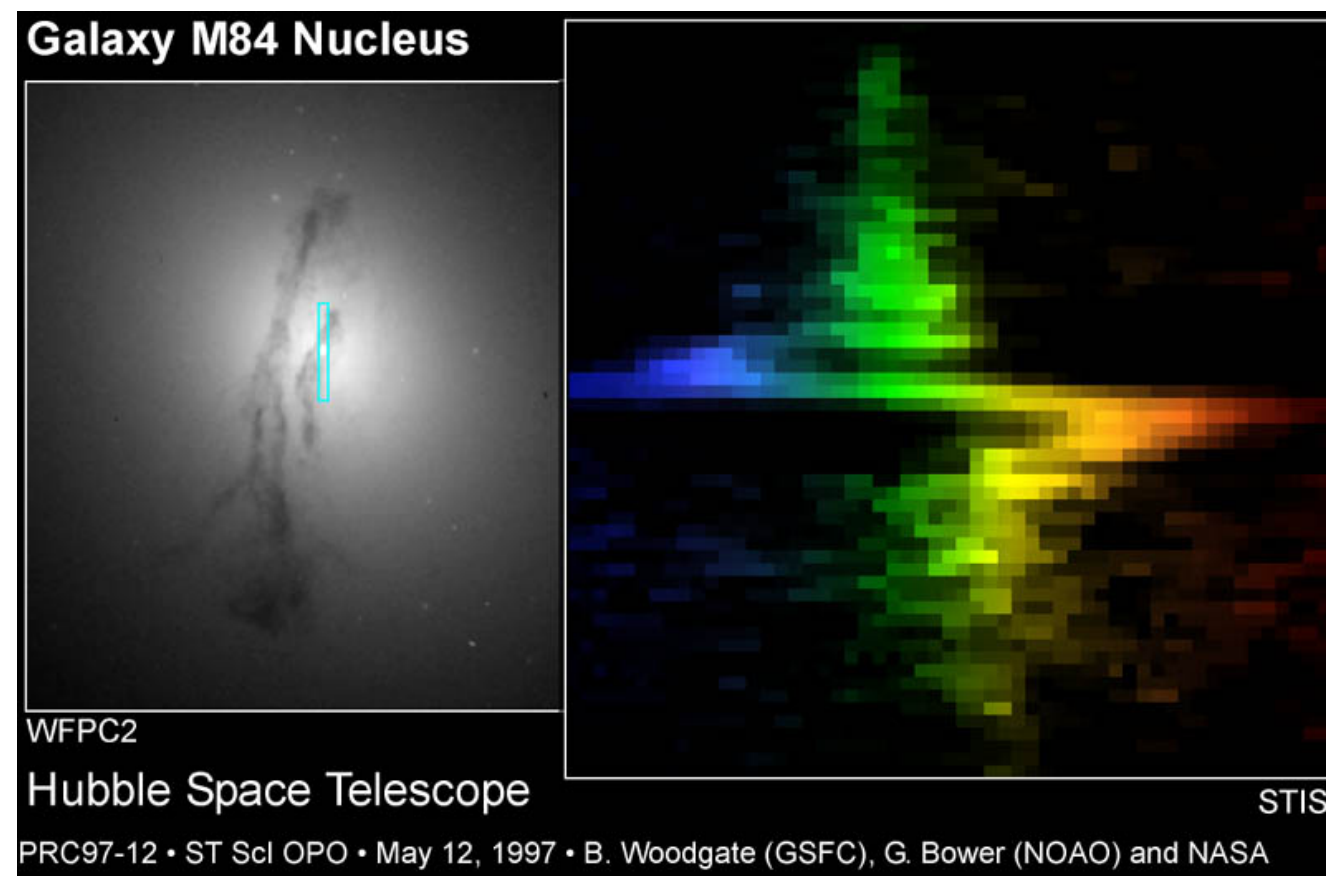
$4 \times 10^6 \times M_{\text{sun}}$

M84

$300 \times 10^6 \times M_{\text{sun}}$

M87

$3.5 \times 10^9 \times M_{\text{sun}}$



M87 Active Galactic Nucleus (AGN)

